What Is the Price for Opportunity? The Effects of Employer Learning on Worker Promotions and Turnover*

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Abstract

This paper identifies the effects of firms on the career advancement of blue-collar workers and interprets these effects through the mechanism of employer learning. I use administrative data on the universe of Brazilian formal employment to study vertical promotions from production jobs to supervisory jobs, which constitute a key component of lifecycle wage growth for most young workers in Brazil. By comparing workers around job-to-job transitions, I show that cross-sectional differences in firms' promotion rates reflect persistent differences in the effects of firms rather than the selection of workers. Workers who move to a high promotion firm become substantially more likely than other job movers to be promoted, but they are even more likely to leave formal employment altogether. Correspondingly, their average long-term wage gains are negligible. I explain these effects using a model where worker ability is initially unobserved and firms differ in their rate of learning about the abilities of employed workers. High learning firms improve the efficiency of matching between workers and jobs, but they also exacerbate the adverse selection of unemployed workers and increase occupational wage inequality. By quantifying the parameters of the model using my estimated effects, I show that skill misallocation remains high and ex-post market power for employers can be large.

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1 Introduction

Research has consistently shown that where you work matters. Across a variety of countries and time periods, the same worker can expect to earn considerably different wages at different employers (Card et al., 2018). Employers, however, influence many aspects of the employment relationship aside from the level of wages, including whether a worker is given the opportunity to advance to more complex and higher paying jobs. In Brazil, the focus of this paper, the average probability that a production worker is promoted to supervisor is nearly zero at most firms, but approximately two percent per year at the top quartile of firms.

Evidence from my setting confirms that promotions are a key channel for worker wage growth and skill accumulation. Direct promotions from production workers to supervisors are accompanied by persistent earnings increases equivalent to the returns to two years of schooling. These promotions also explain five to ten percent of the lifecycle wage profile for young, blue-collar workers. Understanding the employer’s role in creating promotion opportunities, especially for low skill workers, is thus critical to understanding the contribution of firms to economic mobility and inequality.

This paper uses administrative data on the universe of formal employment in Brazil to identify and interpret the effects of firms on the career advancement of blue-collar workers. I show that the unique structure of the occupational data in Brazil allows me to observe direct, vertical promotions for 70% of the formal labor market. By using flexible panel-based identification strategies that compare workers who move to different types of firms, I find that the most upwardly mobile quartile of firms have persistent and large effects on the positive outcome of worker promotion as well as the negative outcome of exit from the formal labor force. I argue that these new facts are most consistent with the interpretation that firms systematically differ in their rate of learning about worker ability. I also show theoretically and empirically that this mechanism has meaningful implications for the equilibrium wage structure and the implied degree of skill misallocation and employer ex-post market power.

A key basis to the paper is the direct measurement of worker promotions using the Brazilian administrative linked employer-employee data. The data are unique in that they clearly distinguish within occupational groups between workers who are focused on production and advanced workers that have supervisory tasks. As a result, I can directly observe when workers are promoted from production jobs to directly related and more advanced supervisor jobs. This is my primary measure of promotions, which is applicable for almost all blue-collar workers that constitute the majority of the Brazilian workforce.

Information about worker ability is initially uncertain for employers, and labor markets are frictional. I establish a conceptual framework for the paper by incorporating these two features into a stylized model of job assignment and highlighting a key testable prediction about the overall effects of employers: under employer learning, firms that promote more often would also fire more often. The model combines a standard learning and job assignment problem (as in Waldman, 1984; Gibbons and Waldman, 1999) with a frictional labor market where asymmetric information between employers results in adverse selection in worker turnover (as in Greenwald, 1986; Acemoglu and Pischke, 1998). In the model, output is complementary in a worker’s unidimensional ability and their job’s complexity. It is efficient to assign high ability workers to a complex job, keep workers of unknown ability in a simple job, and fire low ability workers. I assume that employers are more likely to learn about a worker’s ability when the worker is assigned to the complex job, so high learning employers
are employers that are more willing or able to try out workers of unknown ability in complex jobs. Crucially, the model implies that employers are that are more likely to promote workers due to the realization of positive information are also more likely to fire workers due to the realization of negative information.

I test the predictions of the employer learning model by estimating the effects of high promotion firms on long-term worker outcomes, and my results robustly confirm these predictions. High promotion firms increase the promotion probability for workers who join the firm by an additional 1.2 percentage points relative to an average baseline promotion rate of 1.7 percentage points for similar workers who join other firms. The effects only slightly decay over time and are persistent for at least seven years after moving, including across subsequent moves to other firms. On the other hand, high promotion firms also reduce the long-run formal sector employment rate for their workers by an additional 1.9 percentage points and the effects are similarly persistent, so workers are even more likely to leave formal employment than to become promoted as a result of joining a high promotion firm. Finally, although workers who are promoted experience persistent increases in earnings, the average earnings for workers who moved to high promotion firms are comparable to average earnings for workers who moved to other firms, so most workers do not appear to benefit on net.

The key threats to identifying the effects of employers are that the composition of workers may differ across firms and that firms’ effects may be due to transient shocks rather than systematic differences. I use a two-step estimation strategy to address both concerns. I first define high promotion firms as firms in the top quartile of (composition-adjusted) promotion rates for blue-collar workers using the first four years of my data. I then use the subsequent years of my data to estimate the effects of these firms by comparing workers who move to these high promotion firms to workers who move to other firms. My core identification assumption is that conditional on moving, the identity of the worker’s destination firm is uncorrelated with idiosyncratic changes in workers’ labor market outcomes. This identifying assumption is weaker than the standard assumptions for estimating firm wage effects primarily because I focus on estimating long-term effects, which include any effects stemming from workers’ subsequent mobility. As a result, I do not require that all mobility decisions are as good as random; instead, I assume that the job movers are comparable to each other at the time of the move, which is supported by several falsification exercises.

To further bolster the argument that I am capturing differences in firms’ causal effects, I validate my baseline research design using two additional sources of aggregate variation that shift workers’ job choices. The first approach follows Gibbons and Katz (1992) by using mass layoffs events to purge potential biases arising from workers’ potential selection into moving employers. The second approach follows Oreopoulos et al. (2012) in spirit by instrumenting for the worker’s destination firm with the local hiring share from all high promotion firms (excluding the worker’s destination firm) to purge potential biases arising from workers’ sorting based on idiosyncratic shocks or unobserved trends. My estimates remain similar when using these additional sources of variation for identification, which supports the interpretation that the estimated effects are driven by the impact of firms rather than by worker sorting.

I then use a series of additional empirical exercises to show that the estimated effects are consistent with employer learning and inconsistent with several alternative explanations. Differences in promotions between firms appear to reflect real differences in job assignments and earnings rather than simply differences in the willingness to label otherwise identical workers as supervisors. Simi-
larly, worker exits from formal employment reflect negative employment outcomes that are driven by layoffs or firings rather than workers’ voluntary quits. The negative employment outcomes are also concentrated on workers who are likely to be promoted, which is consistent with learning and inconsistent with firm labor demand volatility. Finally, corroborating survey evidence from managers across a variety of countries supports the interpretation that the effects reflect systematic firm practices rather than any Brazil-specific institutional feature.

After establishing that the direct employer effects are consistent with employer learning, I then explore the effects of high learning employers on all workers in their market in addition to direct effects on their employed workers. I theoretically clarify this indirect mechanism by endogenizing the labor market parameters of my model through an initial vacancy creation stage, and I empirical test the resulting predictions about the overall wage structure. High learning firms exacerbate the adverse selection of workers who change jobs, which softens wage competition and increases the equilibrium wage differential between promoted and non-promoted workers. These additional predictions about occupational wage inequality are also robustly supported by the data. Moving from the 10th to the 90th percentile of municipalities (in terms of the local employment share of high promotion firms) increases the local wage premium for supervisors by an additional 39% over its baseline average.

The model also establishes a framework for quantifying the economic magnitude of the learning mechanism using my estimated employer effects. Although I make strong assumptions on wage setting to close the model in an analytically tractable manner, the basic components of the model that govern job assignment and turnover can be mapped to the estimated effects under a wide range of realistic wage setting mechanisms, including bargaining and binding wage floors. The key restriction for model identification is that workers in the analysis sample do not systematically differ based on their destination firms. This restriction is stronger than the identification assumption used to estimate the employer effects, but it is also consistent with that identification assumption and supported by the data.

Quantifying the model using the estimated employer effects shows that the rate of learning is low on average, including at high promotion firms. As a result, skill misallocation is high – 87% of workers who are suitable for supervisory occupations end up in elementary occupations or outside of formal employment. Nevertheless, the rate of learning is sizable relative to idiosyncratic turnover, so the scope for employer ex-post market power is also substantial. I estimate that job movers are only 71% as likely to be of high ability as the general population, which suppresses outside options for workers and amplifies the value of private information held by employers.

Related Literature

This paper primarily contributes to the literatures on firm heterogeneity in labor market outcomes, worker dynamics within the firm, and firm promotion policies. To my knowledge, it is one of a few papers to focus on occupational outcomes using economy-wide administrative data, and it is the first of those papers to document the firm-level link between promotion opportunity and separation risk. It is also part of a series of papers that combines quasi-experimental estimates of firm heterogeneity with a theoretical framework for quantifying its economic implications, and it is the first within these papers to focus on the implications of employer learning.

A well-established literature has documented that differences between firms pass through to workers. A series of papers use linked employer-employee data and an exogenous movers research
design to estimate the dispersion in the level of firm wage premia (for example, Abowd et al. 1999; Card et al. 2013, 2016; Song et al. 2019), including in the Brazilian context (Alvarez et al. 2018; Gerard et al. 2018). Related papers using worker data have also found that firms experiencing shocks tend to share a portion of the shocks with workers (Kline et al. 2013; Lamadon et al. 2019).

There are relatively fewer papers focusing on firm differences in long run effects, but the ones that do so tend to focus on interpreting long-term wage changes through search, human capital accumulation, or a mixture of the two (Bagger et al. 2014; Herkenhoff et al. 2018; Gregory 2019; Jarosch et al. 2019; Arellano-Bover 2020; Taber and Vejlin 2020; Addario et al. 2021). Notably within this literature, Jarosch (2015) shows that firms differ in layoff risk that erodes workers’ long-term earnings, and Arellano-Bover and Saltiel (2020) shows that firms differ in wage growth that may be correlated with occupational growth. This paper verifies that these two phenomena reflect firms’ causal effects rather than worker sorting. Moreover, this paper argues that the two effects are linked through the mechanism of employer learning.

A similarly rich literature has analyzed the firm’s role in changing a worker’s skill mix. One prominent explanation for workers’ rising task complexity over time is that firms provide workers with either direct or indirect training (Becker 1964; Mincer 1974; Acemoglu and Pischke 1998; Jovanovic and Nyarko 1997; Lazear 2009). An alternative explanation is that information about a worker’s productivity is revealed over time, so tenure profiles reflect selection rather than investment (Jovanovic 1979; Waldman 1984; O’Flaherty and Slow 1995; Farber and Gibbons 1996; Altonji and Pierrel 2001; Golan 2003; Lange 2007). Of course, the two explanations are not mutually exclusive and may interact (Gibbons and Waldman 1999; Autor 2001; Kahn and Lange 2014; Pastorino 2019). This paper shows that learning is relevant even for older production workers and can rationalize the observable trends in workers’ job assignment and turnover. However, my data is not suited to study training directly, and I do not reject the role of either direct training or indirect training (which may be a conduit for learning or promotions). In fact, I find evidence in support of asymmetric information as a meaningful source of labor market frictions, which would imply that firms also benefit from paying for general training.

Finally, there is substantial interest in describing and interpreting firms’ promotions decisions. Case studies have documented that firms commonly draw higher level workers from their pool of lower level workers rather than from external sources (Doeringer and Piore 1971; Baker et al. 1994). Recent studies on white-collar workers also show that although firms attempt to target workers for promotion, such factors are not always efficient or fair (Benson et al. 2019; Cullen and Perez-Truglia 2021). Particularly related is Friedrich (2020), which uses administrative Danish data to show that more productive firms are more likely to use internal labor markets for filling top and middle managerial positions. The paper arrives at similar conclusions that actively promoting firms improve matching efficiency at the cost of higher adverse selection and wage inequality. I additionally provide

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1Note, though, that interpreting wage growth as human capital typically requires making strong assumptions on wage setting, since many mechanisms like job search and dynamic contracting would also generate wage growth without any changes in worker productivity. For example, workers who continue to search for new jobs while employed may receive wage increases whenever they receive a competing outside offer (Postel–Vinay and Robin 2002; Caldwell and Harmon 2019). Models of optimal dynamic contracting often feature increasing wages over a worker’s tenure even if the worker’s productivity is constant or decreasing (Lazear 1979; Burdett and Coles 2003).

2Another strand of the literature seeks to answer whether worker utility is equalized across firms and conclude that non-wage characteristics are dispersed across firms (Sorkin 2012; Maestas et al. 2014). This paper supports their conclusions by showing that career advancement potential is a form of indirect compensation that differs across firms, and it also raises the possibility that workers may be uncertain about employers’ non-wage qualities at the time of hire.
quasi-experimental evidence supporting the causal effects of firms, and I show that these mechanisms are also relevant for the majority of the blue-collar workforce and have long-term consequences on workers’ labor force attachment.

The rest of the paper proceeds as follows. Section 2 establishes a conceptual framework by constructing a model of job assignment and deriving predictions about employers’ effects. Section 3 describes the Brazilian institutional setting and the administrative data. Section 4 discusses the identification assumptions for estimating the effects of employers on workers. Section 5 reports estimates of the effects of high promotion firms. Section 6 rules out potential alternative explanations using a series of additional checks. Section 7 then extends the baseline model to characterize the additional equilibrium effects of high learning firms. Section 8 discusses the structural quantification approach and reports the model’s estimates. Section 9 concludes.

2 Model of promotions and exit under employer learning

To fix ideas about the possible effects of high promotion firms, I begin by characterizing a stylized model of job assignment. I incorporate three critical features that are realistic for my setting. First, firms learn about the quality of their employed workers over time. Second, information about worker quality is asymmetric between firms. Third, labor market matching is frictional and random. The resulting model generates a key prediction – firms that are more likely to promote workers are also more likely to fire workers – which I test in Section 5 by identifying the effects of firms on worker promotions and exit. The model in this section also serves as a basis for exploring the equilibrium effects of employer learning on the regional wage structure in Section 7 and for quantitatively interpreting the estimated employer effects as structural parameters in Section 8.

2.1 Basic setup

I follow the framework of Waldman (1984); Gibbons and Waldman (1999) in modeling vertical job ladders as the optimal matching between workers’ unidimensional ability and jobs’ returns to ability. I assume that workers are one of two types: high ability (θ = θ_H) with probability α, and low ability (θ = θ_L) with probability 1 − α. There are two possible job assignments j ∈ {1, 2} that are supermodular in worker ability and crossing:

\[ f_2(\theta_L) < f_1(\theta_L) < 0 < f_1(\theta_H) < f_2(\theta_H). \]

Figure 1 shows an example of the expected output from each of the two occupations as a function of the probability that the worker is of high ability. The complex job (j = 2) has higher returns to ability but lower output for low ability workers. So expected output is maximized in the high complexity job (j = 2) if beliefs about worker ability is sufficiently high and in the low complexity job otherwise. Moreover, I assume that \( f_j(\theta_L) < 0 \) for \( j \in \{1, 2\} \), so workers who are revealed to be of low ability are not profitable in either job, which introduces a motive for firms to fire workers. Finally, I assume that

\[ \alpha f_1(\theta_H) + (1 - \alpha) f_1(\theta_L) > \alpha f_2(\theta_H) + (1 - \alpha) f_2(\theta_L), \]
so it is output maximizing to assign unknown workers to the low complexity occupation and the promotions problem is not trivial.

The timing of worker and firm actions and the realization of events are summarized in Figure 2. Workers are initially employed at either a high learning firm \((f = H)\) with probability \(\rho\) or a low learning firm \((f = L)\) with probability \(1 - \rho\). At the start of employment, each firm \(f\) randomly assigns each worker to a trial in the complex job \((f_2)\) with probability \(Q_f\) or a trial in the simple job \((f_1)\) with probability \(1 - Q_f\). The firm then observes the worker’s output from the trial and updates its beliefs about the worker’s ability. The complex job always reveals the worker’s ability and the simple job never reveals the worker’s ability. So, a high learning firm is more likely to learn about the ability of each worker because it is more likely to assign them to the more complex job (i.e., \(Q_H > Q_L\)).

Based on its updated beliefs, the firm then decides either to fire the worker or to offer them a wage and job assignment. A fraction \(\delta\) of workers exogenously separate from their employers. The remaining workers choose to either accept the firm’s offer or leave the firm. All workers who separate from their initial employers encounter the secondary market with probability \(g\).

Firms in the secondary market compete by making wage offers to workers. They have access to the same set of production technologies as the incumbent firm, but they do not observe the ability of any worker, so there is asymmetric information. If a worker was offered a promotion at their previous employer, there is a probability \(\kappa\) that they can convince the secondary market of this fact. Firms do not observe any other information about incoming workers, so they do not know whether the worker was fired by their previous employer or they voluntarily quit.

At the end of the period, each firm employing a worker of type \(\theta\) in job \(j\) with wage \(w\) receives \(\pi = f_j(\theta) - w\), while the worker receives \(w\). Workers and firms are risk-neutral, and their outside options are normalized to 0.

### 2.2 Partial equilibrium and direct effects

The partial equilibrium of the model takes the share of high learning firms \((\rho)\) and the secondary market contact rate \((g)\) as given and assumes that workers and firms maximize their expected wages and profits. Since the game is one of imperfect information, I use the Perfect Bayesian equilibrium as my solution concept. The Perfect Bayesian equilibrium in this model is a set of worker and firm strategies such that

1. Workers make turnover decisions that maximize expected wages given the incumbent firm’s wage and job assignment and the expected secondary market wage offers

2. Incumbent firms make wage and job offers that maximize expected profits given the worker’s turnover decision and the expected secondary market wage offers

3. Firms in the secondary market make wage offers that maximize expected profits given their beliefs about the expected ability of each worker in the secondary market

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\(^3\) An equivalent formulation, which generates the same predictions, is to assume that the firm simply learns about the ability of each worker with some probability \(Q_f\) before making job and wage offers. A high learning firm is then a firm that learns about the worker’s ability more often (so \(Q_H > Q_L\)). I use the “trial promotion” formulation because it is more consistent with the dynamics of my estimated promotion effects, as discussed in Section 5. It is also equivalent to assume instead that both jobs are partially informative as long as the complex job is more informative. I make the more stark assumption here to simplify notation.
4. Firms in the secondary market have rational beliefs about the ability of each worker given the turnover decisions of workers and the wage and job assignment decisions of incumbent firms. I consider the primary and economically interesting equilibrium where the incumbent firm promotes workers who are revealed to be of high ability, fires workers who are revealed to be low ability, and retains workers whose ability remains unknown. Working backward, the secondary market is perfectly competitive, so firms offer the expected output for each worker and make zero profits in equilibrium. Any worker that successfully convinces the secondary market that they were previously promoted must have been revealed to be of high ability. Meanwhile, other workers in the secondary market are a combination of high ability workers (who exogenously separated and were not recognized as high ability by the secondary market) or low ability workers (who either exogenously separated or were fired). The probability that an unknown secondary market workers is of high ability is then

$$\alpha' = \frac{\alpha \delta (1 - \bar{Q} \kappa)}{\alpha \delta (1 - Q \kappa) + (1 - \alpha) (\delta + (1 - \delta) \bar{Q})},$$  

(1)

where $\bar{Q} = \rho Q_H + (1 - \rho) Q_L$ is the average rate of learning in the economy. These workers are adversely selected ($\alpha' < \alpha$) both because high ability workers are more likely to enter the secondary market as a promoted worker instead of an unknown worker and because low ability workers are more likely to be fired in addition to being exogenously separated. Secondary market wages $w_j^S$ for each job $j$ are

$$w_1^S = \alpha' f_1 (\theta_H) + (1 - \alpha') f_1 (\theta_L)$$  

$$w_2^S = f_2 (\theta_H),$$  

(2)

where I assume that $\alpha'$ is sufficiently high so that the adversely selected workers are still expected to be productive:

$$E [f_1 (\theta) | \alpha'] > 0.$$  

(3)

Incumbent firms make take-it-or-leave-it offers to workers, so it is sufficient for a firm to offer the expected outside option for the worker to accept the offer. I assume that job take-up decisions are made before the worker makes contact with the secondary market (i.e., there is no on-the-job search), so secondary market wages are discounted by the probability that the worker encounters the secondary market ($g$). Promoted workers run the additional risk that they may not successfully convince the secondary market that they were previously promoted (i.e., $\kappa < 1$). So, optimal incumbent wage offers $w_j^I$ for each job $j$ are

$$w_1^I = gw_1^S$$  

$$w_2^I = g [\kappa w_2^S + (1 - \kappa) w_1^S].$$  

(4)

Notice that even in the case that $g = 1$, so there are no re-employment frictions, the incumbent employer still earns positive profits from each unpromoted worker due to adverse selection in the secondary market, since $w_1^S = E [f_1 (\theta) | \alpha'] < E [f_1 (\theta) | \alpha]$. Meanwhile, $w_2^S$ reflects the true productivity of promoted workers, so the imperfect transmission of information about promoted workers ($\kappa < 1$) ensures that incumbent firms also retain some informational rents from promoted workers.
For the conjectured job assignments to be optimal for incumbents, the following conditions need to hold

\[
E [f_1 (\theta) | \alpha] - w_I^1 \geq 0
\]
\[
f_2 (\theta_H) - w_I^2 \geq f_1 (\theta_H) - w_I^1.
\]

The first condition ensures that the firm will find it profitable to retain workers whose ability remains unknown by offering them the low complexity job with wage \( w_I^1 \). This condition is implied by my assumption that employment in the secondary market is viable for the adversely selected workers (Equation 3). The second condition is an incentive compatibility condition that ensures the firm will find it more profitable to promote high ability workers and pay the higher wage \( w_I^2 \) than to keep the high ability worker in the low complexity occupation and pay the lower wage \( w_I^1 \).

The conditions for the existence and uniqueness of the equilibrium and the characterization of the equilibrium strategies are summarized in the following Proposition 1, and a detailed proof of the proposition is in Appendix B.

**Proposition 1.** If information about job assignments on the secondary market is sufficiently weak (so \( \kappa \) is sufficiently small), then a unique Perfect Bayesian equilibrium exists. In this equilibrium, (i) job assignments for workers are efficient (given firms’ information about workers) (ii) all turnover is involuntary (iii) wages are given by Equations 2 and 4.

To see why the degree of asymmetric information (\( \kappa \)) is key to satisfying the conditions for existence, note that a low \( \kappa \) relaxes the key constraints for both the secondary market and the incumbent firms. A low \( \kappa \) ensures that promoted high ability workers may nevertheless enter the secondary market in the same pool as fired low ability workers, which helps offset the degree of adverse selection in the market. Meanwhile, a low \( \kappa \) also softens wage competition for promoted workers at the incumbent firm, since workers are then less likely to maintain their higher position if they go to the secondary market. This reduces the wage increase necessary to retain a worker upon promotion.

The partial equilibrium setup is sufficient for comparing the outcomes of otherwise identical workers who were initially matched to a high learning firm \((Q_f = Q_H)\) as opposed to a low learning firm \((Q_f = Q_L)\). Since workers may be of either high ability or low ability, being matched to a high learning firm introduces greater opportunities for promotion, but also greater risk of becoming unemployed whenever the probability of re-employment upon separation (\( g \)) is less than 1. Proposition 2 formalizes this comparison and the accompanying proof is also in Appendix B.

**Proposition 2.** In the equilibrium described in Proposition 1, workers initially employed at high learning firms are (i) more likely to be promoted and (ii) more likely to become unemployed than workers initially employed at low learning firms.

Proposition 2 makes the key predictions about the direct effects of firms that I will empirically test in Section 5. Specifically, the testable predictions are that in the presence of systematic differences in employer learning:

1. Some firms will be systematically more likely to promote workers

\[4\] The firm will never find it optimal to offer those workers the high complexity job since under these assumptions, their expected output is lower but the required wages to retain the worker are higher.
2. The firms that are more likely to promote workers are also more likely to fire workers

The model assumes that labor market matching is random, so the workers initially working at high learning firms are comparable to the workers initially working at low learning firms. However, the workers that exit firms are not comparable between high and low learning firms due to firings. In the presence of this selection, simply comparing the cross sectional differences between workers at different firms would overstate the causal effect of high learning firms on worker promotions and understate the causal effect on worker exits. Correspondingly, I focus on testing the model’s predictions by estimating the effect of firm on newly hired workers, and I ensure that the effects are not driven by differences in worker composition.

3 Setting and data

The empirical setting is the Brazilian formal employment sector between 2003 and 2015, which is particularly well suited to examining the effects of employers on workers’ careers for three reasons. First, Brazil’s uniquely detailed administrative data allow researchers to follow approximately 70 percent of the formally employed workforce along direct lines of progression in their occupation groups. Second, although Brazilian labor market institutions have rigid components, employers generally have the flexibility to assign workers in and out of jobs. Finally, the rate of formal higher education in Brazil is low compared to high income countries, so employers can be expected to play a larger role in human capital accumulation or signaling.

3.1 Background on the Brazilian labor market

Brazil’s labor market environment and institutions have been the subject of extensive research. Instead of trying to write a complete account of the Brazilian labor market, I focus on two aspects that are particularly important for the interpretation of my empirical strategy and results. I also briefly summarize several other details that provide additional context.

First, Brazil, like many other developing countries, has a sizable informal sector of the labor market. In Brazil, informal jobs do not have a signed “work card” (Carteira de Trabalho) and consequently are not subject to taxes and labor market regulations. Estimates of the size of the informal sector can vary since informal jobs are by definition missing from official registers. Recent estimates range as high as approximately 50% in metropolitan areas to as low as approximately 20% for all prime age workers; these estimates are comparable to informality rates in other developing economies. Firms in the formal labor market are generally more productive, pay higher wages, employ a greater share of educated workers, and are required to provide legally mandated employment protections and unemployment insurance for their workers. In my data, I can observe whether a worker leaves the formal labor market, but not whether the worker enters the informal labor market versus unemployment. I generally interpret these exits as negative employment outcomes for the worker (and provide supporting evidence for this in Section 6.2), but it is important to note that I do not equate leaving the formal labor market as necessarily reflecting unemployment.

Second, although the Brazilian labor code mandates some employment protections for workers in the formal sector, firms have the latitude to determine both the size and composition of their

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5See, for example, the summary in [Perry et al. (2007)](https://example.com) and estimates in [Gerard et al. (2018)](https://example.com), [Haanwinckel and Soares (2020)](https://example.com), [Dix-Carneiro et al. (2021)](https://example.com).
workforce. Legal protections mandating job security for workers were largely eliminated for employment contracts after 1966, and firms are allowed to dismiss workers without cause as long as they provide notice and severance penalties. The length of notice is typically 30 days (and can be as high as 90 days for workers with long periods of service), and the severance payment is up to 4% of the worker’s total earnings while employed at the firm. Firms are exempt from severance payments for voluntary quits or dismissals with cause (for more details, see Gonzaga et al. 2003, OECD-IDB 2014). By the OECD summary index of employment protections for workers with regular contracts, Brazil is scored as less strict than countries like Denmark, the United Kingdom, and New Zealand. A key aspect of my interpretation is that some firms are more likely to layoff or fire workers after learning new information about the worker, and the relative flexibility afforded to employers is consistent with this interpretation.

Several other factors about the labor market in Brazil provide helpful context but are less central for the interpretation of my results. Labor unions are prominent in Brazil and bargain at the sectoral and the firm level. Firm-level collective bargaining agreements tend to cover all workers at an establishment (rather than varying by occupations or union membership) due to the Brazilian practice of universal coverage. The Brazilian labor code also explicitly prohibits nominal wage reductions, except those that are negotiated through collective bargaining (Lagos, 2019). The rate of tertiary education is generally low but has been experiencing rapid growth from 10% for 25-34 year olds in 2007 to 17% in 2017 (OECD, 2019). Finally, the macroeconomic environment around my period of study is generally stable. Brazil’s period of hyperinflation ended with the introduction of the real in 1994, and inflation during my period of study ranged between 4-9%. While the period that I study straddles the Great Recession, its effects were muted in Brazil; instead, the country experienced a larger and more persistent recession starting in 2014.

### 3.2 Data and sample restrictions

My data on worker outcomes and firm characteristics come from the Brazilian Ministry of Labor’s Relação Anual de Informações Sociais (RAIS), a worker-level dataset containing reporting data on all formal employment contracts. The data are likely to be fairly complete and high quality since the government mandates reporting to RAIS for all formal sector employers and penalizes late or missing filings. The dataset has also been used in several recent studies about the Brazilian labor market (including Menezes-Filho et al. 2008, Dix-Carneiro and Kovak 2017, Alvarez et al. 2018, Gerard et al. 2018, Dix-Carneiro et al. 2021).

I observe key information about each formal employment contract, including its occupation, duration, contracted hours, contracted salary, and average monthly earnings. Furthermore, I observe detailed demographic information about the worker, including their gender, age, educational attainment, and race, as well as basic information about the employer’s industry and location. The records are linked over time by longitudinal identifiers, so I can follow workers over time across different firms. The RAIS separately records each employment contract, and a worker may hold several jobs over a year due to either job transitions or multiple part-time jobs. I construct an annual panel of worker employment histories from the collection of all contracts by selecting the long-term employ-

In the case of dismissals without cause, 80% of the penalty is paid out to workers and 20% is added to the state unemployment insurance fund.
ment contract with the highest average earnings for each worker. Additional details about the data construction are in Appendix C.1.

I consider outcomes between 2003, the first year when worker data are reported under the revised Brazilian occupational codes, and 2015, the last year of my data. For most worker-level analyses (unless otherwise specified), I restrict my sample to prime age workers who are between the ages of 25 and 50, since they have a high attachment to the formal labor force and are less likely to experience formal schooling or retirement. I discuss any additional sample restrictions for the implementation of my identification approaches in the corresponding parts of Section 4.

3.3 Measuring promotions

A distinctive feature of the Brazilian data is that I can observe direct lines of progression from worker to supervisor for most blue-collar occupational groups. Worker occupations are reported under the Classificação Brasileira de Ocupações (CBO) system, which is similar to the International Standard Classification of Occupations (ISCO) in that it groups jobs into a hierarchical structure based primarily on the type and complexity of the tasks involved. However, the Brazilian system, especially after its 2002 revision (CBO-02), is particularly suitable for the measurement of worker promotions for two reasons. First, it organizes occupations into occupational groups by natural lines of progression in addition to task content, so occupations that are often related for workers but do not share narrowly-defined tasks (like loom operators and fabric dyers) are explicitly grouped. Second, it consistently distinguishes between supervisors, who are advanced production workers with additional managerial responsibilities, from more elementary line workers within each occupational group. As a result of these two features, I can interpret changes from production occupations to supervisor occupations within the same general occupational group as reflecting a direct, vertical promotion.

Table 1 shows an example of an occupational group with a directly observable line of progression. The first two digits of the occupation code indicate the main occupational group, a “0” in the third digit indicates the sub-group of supervisory occupations, whereas other codes in the third digit indicate other sub-groups that contain production occupations but do not necessarily have a clear hierarchical structure. This basic structure applies to nearly all of the non-professional occupational groups in the Brazilian data. Figure A.2 shows that around 70% of workers in the formal sector belong to a 2-digit occupational group with a clear supervisor-worker line of progression and that this share is fairly stable over the period that I study.

In this paper, I define a promotion as moving from any production occupation belonging to a supervisor-track occupational group to a supervisor occupation. Figure 3 shows that promotions are reasonably common. Furthermore, around half of promotions are purely vertical moves within the same occupational group. Promotion rates are fairly stable and free of secular trends over my sample, although they did begin to taper around 2014 when Brazil experienced a recession.

Two descriptive facts support the argument that my measure of promotions captures an important source of worker growth. First, promotions are valuable. Table 2 shows the estimated wage premium for supervisors relative to other production workers. The average cross-sectional wage premium is

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7 Defined as a contract that covered at least 6 months out of the year and entailed at least 20 contracted hours per week.
8 A reclassification of the CBO-02 system occurred in 2008 and slightly increased the share of workers that belong to a relevant occupational group, but it does not substantively affect my approach or results.
63 (s.e. 1.8) log points. Controlling for worker characteristics accounts for 39% of this difference and controlling for unobserved differences through worker fixed effects accounts for another 34%, which implies that supervisors are positively selected. Even when I focus on within-worker changes in earnings, however, promotions are accompanied by wage increases of 17 (s.e. 0.35) log points, which is equivalent to the returns to an additional 1.7 years of education in Brazil.

Second, promotions consistently explain part of the lifecycle wage profile for young production workers. Table 3 compares the estimated lifecycle wage profile for workers between the ages 25 and 35 before and after including the promotion measure as an explanatory variable. When controlling for only basic worker characteristics, an extra year in age increases earnings by 1.73 (s.e. 0.03) log points. Adding promotions as an explanatory variable decreases the age coefficient to 1.63 (s.e. 0.03) log points, which implies that promotions explain approximately 5% of the age profile. The estimated age coefficient falls as I add additional controls for occupational characteristics and firm wage premia, but the estimated promotion wage premium stays relatively stable. As a result, the share of the age profile that is explained by promotions increases to 11%.

Although this exercise is descriptive, the results confirm that promotions capture a meaningful change that are distinct from education and employer upgrading.

4 Identifying the effects of firms

My objects of interest are the effects of existing firms on worker promotions and job turnover, so the ideal experiment to randomly assign workers to various firms while taking as a given that those firms are a bundle of underlying practices. As a result, my identification strategy centers around changes in a worker’s firm assignment, rather than changes in a firm’s practices or changes in a worker’s promotion likelihood. The baseline approach compares changes in worker outcomes among job-movers by the type of the destination firm, and two extensions relax the key identification assumptions by using aggregate shifters of workers’ job choices.

My approach is similar to the two-step grouped fixed effects estimator of Bonhomme et al. (2019). I first separate firms into distinct groups using observational data, and I then estimate the effects of each group of firms on workers while allowing for flexible dynamics. However, my identification assumption is weaker than that of Bonhomme et al. (2019) since my estimand of interest is the long-term effect of differences between firms.

Generalizing the movers research design into a two-step event study framework also yields three

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9Controlling for firm-wage premia by subtracting the estimated AKM firm wage fixed effect from worker earnings increases the estimated promotion premium from 17 log points to 20 log points. These estimates are generally larger than the average wage increases accompanying all promotions the literature, but smaller than the large jumps in pay at the top of corporate hierarchies (see, for example, Murphy, 1983; Baker et al., 1994; McCue, 1994; Blau and Devario, 2007).

10My estimate is generally comparable to the estimate from McCue (1994) using self-reported promotions from the U.S. PSID. For comparison, Topel and Ward (1992) estimate that a third of wage growth over the first 10 years of employment in the U.S. is accounted for by wage gains at job changes, which would include promotions, and Bagger et al. (2014) estimate that human capital growth accounts for 20-25% of the life-cycle wage profile for low to medium educated workers in Denmark.

11As a concrete example, suppose firm wages are static and only vary by level. In this setting, firms may have dynamic effects on worker earnings if they disproportionately lead their workers to move to high wage firms. Estimators that seek to identify firms’ wage policies would need to make assumptions about workers’ mobility decisions to net out the contribution of subsequent high wage firms from the dynamic effects of prior firms. On the other hand, I seek to estimate the overall effect of the prior firm, including any effects that arise from workers subsequently moving to high wage firms.
additional benefits. First, I can explicitly separate the timing between the classification of firms and the estimation of employer effects to ensure that the effects reflect permanent differences between firms rather than different realizations of transitory firm shocks. Second, I can follow standard event study methodology in conducting falsification tests of my identifying assumptions through pre-trend and balance tests. Finally, it is straightforward to use flexible estimators that estimate the relevant average treatment effect by combining cohort-level treatment effects with explicit weights.

4.1 Defining high promotion firms

As a first step, I classify firms into two groups using the firm’s composition-adjusted promotion rates between 2004 and 2006. For each year between 2004 and 2006, I estimate the worker-level regression

$$\text{Promoted}_{it} = \beta_t X_{i,t-1} + \gamma_{at} + \eta_{jt} + \varepsilon_{it},$$

(5)

where \(\text{Promoted}_{it} = 1\) if a worker was promoted from production worker to supervisor between years \(t - 1\) and \(t\). \(X_{i,t-1}\) and \(\gamma_{at}\) adjust for differential promotion rates by workers’ observable characteristics (a quadratic in age interacted with gender and indicators for education, race, and state) and the worker’s occupational group, respectively. \(\eta_{jt}\) is the firm’s residualized promotion rate in year \(t\). I average over all three years of estimates for each firm to calculate the firm’s average promotion propensity \(\eta_j = E[\eta_{jt}]\). Firms with fewer than 10 promotion-track workers in at least one of those three years and firms who did not exist in all three years are unlikely to generate precise estimates of \(\eta_j\) or survive through to the movers analysis, so I drop them from the classification sample. I similarly exclude public sector firms, which may have different organizational structures and internal incentives.

Figure A.1 plots the distribution of the average promotion propensity \(\eta_j\) for the remaining sample of firms, winsorized at the 5th and 95th percentiles. The distribution is highly skewed, with a small tail of firms who are highly active in promoting workers and a majority of firms who promote few (if any) workers. Some of the dispersion is mechanical since residualizing promotion rates by worker characteristics can generate dispersion in the firms’ estimated fixed effects even when the firms’ promotion rates were uniformly zero. Splitting firms into two groups based on \(\eta_j\) then ensures that my estimates of differences between firms are not primarily driven by small differences in residualized rates between firms who did not promote any workers.

For the rest of the paper, I define high promotion firms as firms with an average promotion propensity \(\langle \eta_j \rangle\) that is in the top quartile of all firms in this classification sample, and low promotion firms as all other firms in the sample. Table 4 shows the difference in firm characteristics between high and low promotion firms between 2003 and 2006. High promotion firms are larger, higher paying, and have a greater share of supervisors in the relevant occupational groups. They are also responsible for almost the entirety of promotions within this sample of firms, which supports pooling the remaining firms together as one group. Finally, promotion rates may reflect in part the realization of positive firm shocks – high promotion firms are both faster growing and have higher

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12To facilitate interpretation, I restrict the sample to workers who are in the same occupational group in both years. However, the estimates are highly correlated if I additionally include workers who switch occupations or restrict the sample further to only include job stayers. For more details, see Appendix C.1.

13There may be concerns that supervisor shares are mechanically higher at high promotion firms since they were defined by having promoted workers. I also consider the prior year’s supervisor share as a check, and the results are slightly smaller but similar.
wage growth for incumbent workers, which motivates using worker outcomes from later years as the key test for the presence of any persistent differences between firms.

4.2 Baseline research design

Estimating equation and identifying assumption

My baseline research design compares the change in outcomes between workers who move to high promotion firms and workers who move to low promotion firms. The primary identification assumption is that for workers who are making an employer-to-employer transition, the type of the worker’s destination firm is uncorrelated with idiosyncratic changes in the worker’s labor market outcomes. This identification assumption is implied by standard exogenous mobility assumptions that are used in the literature for estimating firm wage effects, but it is strictly weaker. Specifically, I also allow for workers to select into moving based on idiosyncratic worker-level shocks and for firms to have persistent effects on workers after they leave.

To fix ideas, consider workers who make an employer-to-employer move in a single cohort year \( c \). Let \( H_i = 1 \) if worker \( i \) moved to a high promotion firm and \( H_i = 0 \) if they moved to a low promotion firm. My estimation equation for the dynamic effects of the high promotion firm on worker outcome \( y_{it} \) is

\[
y_{it} = \sum_{\tau} \beta_{\tau} (H_i \times I^*_\tau) + \alpha_i + \pi X_{it} + \theta_t B_{i,c-1} + \gamma_{sot} + \epsilon_{it}, \tag{6}
\]

where \( I^*_\tau \) are event-time indicators that equals 1 when \( t - c = \tau \) and 0 otherwise (with \( \tau = -1 \) as the omitted time period). \( \alpha_i \) is a worker fixed effect, \( X_{it} \) is a vector of time-varying worker covariates, and \( B_{i,c-1} \) is a vector of baseline worker covariates from year \( c - 1 \) that may affect worker outcomes in other periods through the time varying coefficients \( \theta_t \). Finally, I saturate the regression with \( \gamma_{sot} \), a set of state-by-baseline-occupational-group-by-time fixed effects that control flexibly for aggregate trends in market conditions or skill prices.

Note that by defining the estimand of interest \( \beta_{\tau} \) as the effect of moving to a high promotion firm after \( \tau \) years, rather than the effect of staying at the high promotion firm for \( \tau \) years, I do not distinguish between workers who remain at the high promotion firm from workers who subsequently left. So, my estimate includes the direct effects of the firm on its stayers as well as the persistent effects of the firm on workers’ mobility decisions and subsequent outcomes at other firms. The reason for this choice is twofold. First, some models of human capital accumulation predict that workers would only realize most of the gains after leaving the employer responsible for providing the human capital, and this estimand ensures that I appropriately capture these channels. Second, I do not need to make any assumptions about the worker’s mobility decisions after the year of the initial move, which itself may be a result of the worker’s destination firm.

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14 In pooled specifications, I collapse event time into two periods – the near term (\( \tau \in [0, 2] \)) and the long-term (\( \tau > 2 \)).
15 In the baseline specification, the time varying covariates \( X_{it} \) are quadratic trends in age that vary by gender and indicators for educational attainment, while the baseline covariate \( B_{i,c-1} \) is the origin firm’s estimated AKM firm effect. These controls explain any differences in baseline characteristics of the high versus low promotion firm movers, as shown in the balance test discussed later in this section.
16 For example, employers that provide training may demand compensating differentials through lower wages (Becker, 1964), or employers may specialize in jobs that are “stepping stones” for more complex jobs at other firms (Jovanovic and Nyarko, 1997).
The key assumption for the identification of $\beta_\tau$ is that
\[ E[\varepsilon_i H_i] = 0. \]

In words, I assume that changes in worker outcomes that are unexplained by my controls are uncorrelated with the type of the worker’s destination firm. Economically, this assumption would be satisfied if high and low promotion firms are observationally indistinguishable to workers at the point of job take-up. This assumption would also be satisfied if firms observationally differ, but workers (with the same covariates) draw offers at random from a common distribution and make the same take-up decisions upon receiving an offer. On the other hand, this assumption would be violated if workers who are more likely to experience a positive shock are also more likely to receive or accept an offer from a high promotion firm.

Although my identifying assumption is about the counterfactual changes in worker outcomes and not directly testable, a related falsification test suggested by Kahn-Lang and Lang (2020) is whether workers moving to high versus low promotion firms are different in levels. Figure 5 plots the difference in baseline covariates between high and low promotion firm movers from the regression
\[ X_{i,c,1} = \beta H_i + \theta M_{i,c,1} + \varepsilon_i, \]

where $X_{i,c,1}$ are worker characteristics from the baseline year, $H_i$ is the indicator for whether the worker moved to a high promotion firm, and $M_{i,c,1}$ are any controls from the baseline year. The raw differences in baseline means between the two groups show that movers to high promotion firms have slightly higher baseline earnings, are more likely to be male, and have fewer years of education. However, most of the differences are explained by the state and occupational group of the worker. Any remaining differences in baseline earnings between the two groups are explained by the fact that movers from high promotion firms are more likely to come from high wage firms (as proxied by the estimated AKM firm fixed effect), and remaining differences in education and gender are quantitatively small.

**Estimation details**

I estimate average employer effects by stacking the five cohorts of workers who make an employer-to-employer transition to a high or low promotion firm between 2008 and 2012. Figure 4 shows a timeline of my approach. Since my data ends in 2015, I observe at least three years of worker outcomes following the move, but any effects for longer-term outcomes are identified by the earlier cohorts only. A recent literature on event studies with staggered treatment timing has cautioned that simply pooling all cohorts and estimating treatment effects by OLS may yield unintuitive and potentially negatively weighted means of the cohort-specific treatment effects (e.g., de Chaisemartin and D’Haultfoeuille, 2020; Goodman-Bacon, 2021; Sun and Abraham, 2021). I avoid this issue by allowing all coefficients in Equation 6 to vary arbitrarily by cohort and then averaging the cohort-specific treatment effects explicitly with uniform weights as $\beta_\tau = E[\beta_\tau]$. This estimation approach also clarifies that the

\[ ^{17} \text{In the cases when the same worker belongs to multiple mover cohorts, I consider the worker’s earliest move. However, the results are similar when I include all moves as separate events.} \]
\[ ^{18} \text{This approach is algebraically identical to estimating Equation 6 separately for each cohort. Estimating the coefficients jointly in this approach ensures that the standard errors are correct when clustering across cohorts.} \]
identification of $\beta_\tau$ comes solely from aggregating comparisons between workers that are in the same cohort. For more details, see Appendix Section C.2.

I make several sample restrictions on the set of movers to ensure that I capture the effect of interest. First, I restrict the estimation sample to workers who were continuously employed for the three years before the move to facilitate the assessment of pre-trends and to ensure that my sample consists of workers with a high degree of attachment to the formal labor force. I additionally restrict the sample to workers who are between the ages of 25 and 50 at the time of moving to ensure that worker outcomes are unlikely to be driven by external shocks like schooling and retirement. Finally, I focus on workers for whom promotions would be relevant – production workers working in an occupational group with a directly observable supervisor track in the year before the move. Some employer-to-employer transitions in the data appear to reflect firm organizations or spinoffs, so I use a worker-flows approach to eliminate employer changes that appear to be spurious. The remaining transitions reflect worker-level variation and do not require higher clustering under the framework of Abadie et al. (2017), but I cluster standard errors conservatively at the destination firm level to allow for arbitrary correlations in outcomes between workers moving to the same firm and over time.

4.3 Extensions incorporating additional variation

The exogenous job movers assumption that is also sufficient for my identification assumption makes strong restrictions on worker mobility. Although the restrictions are generally consistent with the data, researchers have also pointed out that worker sorting can violate the identifying assumptions but generate similar empirical patterns (for example, see Eckhout and Kircher, 2011). To address these concerns, I extend the baseline design to incorporate two sources of aggregate variation that relaxes the two key components of the assumption – that workers separate from their jobs for exogenous reasons, and that conditional on separating, the type of firm the worker moves to is exogenous. In the framework of Abaluck et al. (2021), I test the balance and fallback conditions, respectively. It is worth noting that my approach is not specific to promotions or the Brazilian data, and it may be generally useful as tests for the validity of movers research designs.

To ensure that my effects are not driven by workers’ differential selection into moving employers, I follow Gibbons and Katz (1992) and use mass layoffs as an exogenous shock that separates workers from their current employers. I follow the methodology from Schmieder et al. (2020) to identify mass layoff events as firm events where employment dropped by at least 30% year over year and where no more than 20% of separated employees were re-employed at the same firm. Around 127,000 workers from 16,000 firms in my baseline sample were separated as a result of a mass layoff, which is 12% of the baseline sample. Column 2 of Table 5 summarizes the characteristics of the laid-off workers. Relative to the baseline sample, they are slightly older, have fewer years of education, and lower earnings, but they are more likely to move to a high promotion firm.

I test for whether selection into moving firms is driving my results by estimating the baseline Equation 6 on the sub-sample of exogenously separated workers. It’s worth emphasizing, however, that I compare laid-off workers who move to high promotion firms to laid-off workers who move to low promotion firms. So, I use mass layoffs as a particularly powerful instrument that shifts all affected workers into moving, but I assume that the effects of the mass-lyoff itself are homogeneous.

19 Specifically, I follow the mass layoffs literature (e.g., Schmieder et al., 2020) by dropping any origin firms where at least 20% of exiters went to the same destination firm.
and absorbed by my time-varying controls. This is in contrast to the literature on estimating the effects of mass layoffs by comparing laid-off workers to workers at other, non-layoff firms.\footnote{Of course, a concern with this approach is that mass layoffs themselves differentially affect workers. This concern is mitigated in my setting by the fact that my comparison is within the set of mass layoff workers, and also by the fact that any worker who is included in the employer-to-employer mover sample would have been unemployed for less than 12 months following the mass layoff.}

To ensure that my effects are not driven by workers differentially sorting into high promotion firms based on idiosyncratic shocks, I consider aggregate regional variation in the types of employers who are hiring workers (which is similar in spirit to Oreopoulos et al., 2012). I construct $z_m$ for each cohort as the jack-knife share of hiring at the worker’s municipality that is from high promotion firms rather than low promotion firms while excluding any hires from the worker’s destination firm.\footnote{The workers in my analysis sample contribute to the total number of new hires, which introduces a functional dependence between $H_i$ and the hiring share $z_m$. Although this problem is minor in my setting since municipalities in the sample are generally large, I exclude any hiring from the worker’s destination firm from $z_m$ to avoid the reflection problem that would otherwise arise. Technically, the jack-knife procedure introduces some slight variation in $z_m$ by the worker’s destination firm, but I slightly abuse notation to make the source of identification clear.}

I then instrument $H_i$ with $z_m$ by estimating the following just-identified system of equations using two stage least squares:

\[
H_i \times I_t^\tau = \phi \tau (z_m \times I_t^\tau) + \tilde{\pi} X_{it} + \tilde{\alpha}_i + \tilde{\theta}_t B_{i,c-1} + \tilde{\gamma}_{so} + \eta_{it} \\
y_{it} = \sum_{\tau} \beta_{\tau} (H_i \times I_t^\tau) + \pi X_{it} + \alpha_i + \theta_t B_{i,c-1} + \gamma_{so} + \nu_{it}.
\]

(7)

The second stage equation is identical to the baseline Equation 6, including the use of worker fixed effects and flexible controls for skill prices. Since variation is at the municipality level, I differ from the other specifications by clustering standard errors by the worker’s destination municipality.

Figure A.4 shows graphical intuition for my instrument by plotting the average $H_i$, the probability that a worker moves to a high promotion firm, against binned values of $z_m$, the jack-knifed municipal hiring share, while controlling for observable differences worker characteristics (a quadratic in age interacted with gender along with indicators for the worker’s education, race, and state), the firm wage premia of the worker’s origin firm, and state-by-occupation fixed effects. $z_m$ has clear predictive power and the conditional expectation function is approximately linear. As an additional check, I estimate the cross-sectional regression

\[
H_i = \phi z_m + \tilde{\pi} X_{ic} + \tilde{\theta} B_{i,c-1} + \tilde{\gamma}_{so} + \nu_i
\]

(8)

separately for each cohort. The minimum F-statistic for the instrument across all five cohorts is 627, and the average F-statistic is 1161.

The key identifying assumption for the instrumental variables approach is:

\[
E [\varepsilon_{it} z_m] = 0.
\]

In words, I assume that changes in worker outcomes that are unexplained by my time-varying controls are uncorrelated with the worker’s municipality. This municipality-level assumption substantially relaxes the worker-level assumption in Section 4.2 by allowing workers to sort arbitrarily across firms within municipalities, including in anticipation of worker-level changes. However, this assumption also imposes the additional exclusion restriction that $z_m$ is uncorrelated with any other unobserved
factors that may shift worker outcomes. This concern is mitigated by the rich state-by-occupational-group-by-time fixed effects and testable pre-trends. Moreover, I focus on assessing whether some firms are more likely to generate positive outcomes (promotions) as well as negative outcomes (exits). To the extent to which regions with more hiring by high promotion firms experience different local labor market shocks, these additional shocks are unlikely to increase both worker promotions and formal labor force exits. Nevertheless, potential violations of the exclusion restriction are an important caveat to interpreting the IV results.

5 Direct effects of high promotion firms

My estimates match the model’s predictions on the direct effects of employer learning – high promotion firms have persistently positive effects on worker promotions and negative effects on formal labor market attachment. Consequently, these firms only have negligible long-term effects on average worker earnings. I begin by reporting the estimates from the baseline research design described in Section 4.2, which are my preferred estimates since they most directly reflect the effects for the typical worker making a job-to-job transition. To address any remaining concerns that my results may be driven by unobservable differences between workers, I next discuss the results of a series of robustness checks and alternate identification strategies. I show that including rich time-varying trends by additional worker characteristics or removing most of the controls from the baseline specification has little effect on my estimates. I also show that alternative identification strategies that incorporate quasi-experimental shifters of workers’ firm choices, as discussed in Section 4.3, produce estimates that are quantitatively and qualitatively similar to my baseline results.

5.1 Baseline results

My first result is that differences in firm promotion rates reflects persistent differences in firms’ causal effects on workers. Figure 6 plots the estimates of $\beta_\tau$ from estimating Equation 6 on the outcome of whether a worker is working in a supervisory occupation $\tau$ years after moving. Workers are 1.19 (s.e. .09) percentage points more likely to be working as a supervisor within the first two years after moving to a high promotion firm rather than a low promotion firm. The effects are large relative to the average promotion rate of 1.68 percentage points for movers to low promotion firms over the same period, as well as the overall annual promotion rate of 0.779 percentage points for production workers. Moreover, the effects are persistent. Workers are still 0.936 (s.e. 0.08) percentage points more likely to be working as a supervisor more than two years after initially moving, even though 77% of workers are no longer working at the destination firm by then.

There are two things to note about how this result on promotions affects the interpretation of high promotion firms. First, promotions are not due to the realization of transient firm shocks. Firms are

22For this outcome, I include all workers who leave the formal labor market, and I assume those workers are not working in a supervisory occupation. The effects could be considered a lower bound if high promotion firm movers who leave the formal labor market are also more likely to work as a supervisor in the informal labor market.

23Note, however, that these effects do not necessarily imply that the long term promotion effects are driven by a single group of workers who were immediately promoted. Figure A.5 plots the event study coefficients from the same estimating equation on the outcome of whether a worker was ever promoted by $\tau$ years after moving. Promotions within a year of moving the firm only account for half of the cumulative number of promotions. So, the relative stability of the effects on promotions at $\tau$ masks the fact that workers are entering and exiting the supervisor role at roughly similar rates in the later years.
classified as high or low promotion firms based on their promotion rates for workers between 2004 and 2006, whereas workers in the analysis sample joined the firm between 2008 and 2012. The fact that firms who are active in promotions from the early data also have clear effects on workers who join the firm several years afterward indicates that these effects are driven by persistent differences between firms.\footnote{Moreover, Figure [A.6] shows that these effects are not substantially different between the early and later cohorts.} Second, promotions at high promotion firms cannot be determined by seniority rules alone. My identification strategy relies upon comparing workers around employer transitions, so all workers in the sample would be at the bottom of the seniority ladder. The fact that I detect large effects on promotions immediately after the worker moves firms indicates that firms are willing to consider relatively new workers for more senior positions.

On the other hand, my second result is that high promotion firms are also more likely to lead workers to leave formal employment altogether. Figure [7] plots the baseline event study specification for the outcome of whether the worker is working for any firm in the formal employment sector \(\tau\) years after moving. Workers are 1.93 (s.e. 0.25) percentage points less likely to be found in formal employment more than two years after moving to a high promotion firm rather than a low promotion firm. Although the effects are smaller in relative terms given that 21.4% of workers who move to low promotion firms also leave formal employment over the same period, the differential effect of high promotion firms on exit rates is twice as large as their effect on promotion rates. So, a production worker who joins a high promotion firm is substantially more likely to leave formal employment altogether than to become a supervisor.

The key prediction from Proposition 2 is that workers joining high learning firms are both more likely to be promoted and more likely to become unemployed. The results on employers’ effects in this section confirm this prediction. In other words, high promotion firms seem to be high learning firms. Moreover, the details of the empirical results support the model’s assumptions. I assume in the model that the matching of workers to firms is random. Focusing on a sample where this assumption is plausible (based on the evidence in Figure 5) and additionally isolating the effects of the high promotion firms help ensure that the connection between the model and the empirical support is correspondingly tight. In addition, I model learning as the result of uninformed “trial promotions” that generate information about worker ability. The fact that promotion effects appear immediately after workers move firms and then partially decay over time is consistent with this interpretation.

Finally, high promotion firms have only mixed effects on workers’ long-term earnings. Figure [8] plots the event study estimates for the worker’s average monthly earnings conditional on remaining in formal employment. Workers who move to a high promotion firm earn 1.26 (s.e. 0.51) log points more within the first two years of moving, which is consistent with higher overall wage policies at those firms. However, the short term wage gains dissipate quickly, and those workers earn no more than workers who initially moved to low promotion firms three years after the initial move. Given that earnings are only defined for workers who remain in formal employment, the estimates can be considered an upper bound on the overall effects on earnings, since workers who move to high promotion firms are also more likely to leave formal employment afterward.\footnote{Table [A.2] provides a lower bound on earnings effects by imputing earnings outcomes for workers who leave the formal labor force under the assumption that all workers who leave are unemployed. To implement this, I assume that counterfactual earnings for workers who leave the formal labor market would have grown at the average rate for their baseline occupation-by-state cell, but are discounted by the ratio between the value of non-work time and the market wage (estimated as 0.58 by Mas and Pallais [2019]).} It’s also worth
noting that the event study on earnings is likely to be a particularly sharp test of my identifying assumptions. If workers who move to high promotion firms are more likely to have systematically higher productivity growth, then they are likely to have differentially higher earnings growth in the three years before moving; my results show that this is not the case.

5.2 Robustness of direct effects

Several checks support the interpretation that my estimates reflect high promotion firms’ causal effects rather than differences in worker sorting or market level shocks. The estimated effects remain quantitatively and qualitatively similar when I use a simplified specification with only worker and year fixed effects or a rich specification with time trends that absorb additional differences between workers at baseline. The estimates are also comparable when I use shifters of worker separations or worker destinations, as discussed in Section 4.3, although they are generally less precise. Finally, the effects do not depend on the details of how I classify firms, but the effects of firms who are active in promoting workers are distinct from firms with high wage growth.

Figure 9 compares the pooled estimates of the main outcomes across three different specifications of controls. Compositional differences between high and low promotion firm movers are small in magnitude and become largely indistinguishable from zero conditional on the worker’s baseline geography, firm wage premia, and occupation, which motivated controlling for flexible trends at the state-by-occupation level and by baseline firm wage premia in my main specification. However, dropping these additional controls only slightly decreased the estimated effects on workers’ formal labor market attachment and earnings. Meanwhile, adding additional flexible trends for each gender-by-education cell, the only worker characteristics where the difference between movers was statistically significant, as well as flexible trends by baseline worker earnings did not meaningfully change the estimated effects. The stability of estimates across these controls is reassuring that my identification assumption appears valid.

Meanwhile, Figure 10 compares the pooled estimates of the main outcomes across the three sources of variation. The mass layoff estimates are from estimating Equation 6 on the sub-sample of movers whose baseline firm was experiencing a separation shock that is plausibly exogenous to the worker. The estimates are less precisely estimated than the baseline due to the smaller sample but are otherwise nearly identical. The estimated earnings effects are slightly higher than the baseline estimates, although the two are not statistically distinguishable. Meanwhile, the local hiring estimates are from estimating the instrumental variables Equation 7. Variation is at the municipality level, and the standard errors are correspondingly larger, but the estimates remain comparable to my baseline results. The hiring instrument is strong in the full specification – the F-statistic for the joint significance of the excluded instruments in the pooled IV first stage regression is 119, so I calculate confidence intervals based on the standard asymptotically valid critical values (as suggested by Lee et al., 2021)\(^\text{26}\). The magnitudes of the IV estimates on formal labor market attachment and earnings gains are both larger, and the IV estimate on promotions is again nearly identical to my baseline estimates.

Finally, I find that the results do not depend on the details of how I classify firms based on promotion rates, but the use of actual promotions data is critical. Figures A.9, A.10 and A.11

\(^{26}\)The F-statistic for the earnings outcome is 105. It is slightly different since the sample is conditional on remaining in formal employment.
replicate the event study estimates of the baseline Equation 6 using the continuous measure of the firm’s promotion propensity $\eta_j$ (as defined in Section 4.1 and winsorized at the 5th and 95th percentiles) instead of the discrete high versus low classification. The qualitative patterns are nearly identical when using this continuous measure, and the magnitudes of the estimates are consistent with the overall difference in average promotion rates between high and low promotion firms. Another possible concern is that the classification process includes both external and internal promotions, so the estimated effects are not necessarily representative of firms that focus on developing their workers. I test for this explanation by replicating my baseline empirical strategy on an alternate definition of high and low promotion firms that uses information from internal promotions alone. Figure A.18 compares the pooled estimates from this alternative classification, and the effects are again similar.

To highlight the importance of direct occupational data, I also benchmark the effects of high promotion firms against the effects of high wage growth firms (defined as firms in the top quartile of wage growth for its incumbent workers between 2004-2006) in Figure A.18. Unsurprisingly, firms with high wage growth do increase the earnings of their workers, but they have almost no effect on workers’ career progressions and they have similarly negative effects on the probability that workers remain in formal employment. This suggests that the effects of high wage growth firms may primarily be driven by other channels of wage determination like bargaining, on-the-job search, or seniority pay.

6 Additional evidence for the employer learning mechanism

The analysis in Section 5 shows that the effects of high promotion firms on worker promotions, labor force exit, and earnings are robust to alternate specifications and unlikely to be driven by worker sorting. Furthermore, given the setup of the empirical strategy, the effects are unlikely to be explained by transient shocks or seniority rules at high promotion firms. In this section, I use a variety of additional empirical exercises to show that the effects of high promotion firms are consistent with employer learning and inconsistent with several other alternative explanations.

6.1 Promotion effects reflect positive worker outcomes

I empirically examine whether differences in promotions reflect differences in real outcomes by comparing the promotion wage premium for workers who move to high promotion firms versus low promotion firms. To do so, I extend Equation 6 and estimate

$$y_{it} = \beta_{i}^{HP} (H_{i} \times P_{t,c+1} \times I_{t}^P) + \beta_{i}^{H} (H_{i} \times (1 - P_{t,c+1}) \times I_{t}^P) + \beta_{i}^{P} (P_{t,c+1} \times I_{t}^P) + \pi X_{it} + \alpha_i + \theta_i B_i + \gamma_{sot} + \varepsilon_{it}$$

(9)

where $P_{t,c+1} = 1$ if worker $i$ is working as a supervisor one year after moving firms and $P_{t,c+1} = 0$ otherwise. These estimates are descriptive rather than causal since being promoted is an outcome from moving to high promotion firms, but they are useful for testing for the patterns of selection that would result if high promotion firms are simply more likely to classify workers as supervisors.

The similarity of these two effects is unsurprising since most of the promotions that determined a firm’s promotion propensity were internal promotions. For more details on classification, see Appendix C.1.
Workers who are promoted following a move to a high promotion firm experience persistent increases in earnings that are larger than the promotion wage-premia at low promotion firms. Figure 11 plots the estimates of \((\beta_{HP}, \beta_{H}, \beta_{P})\), the relative wage changes for promoted high promotion firm movers, unpromoted high promotion firm movers, and promoted low promotion firm movers, respectively. The omitted reference group is the unpromoted low promotion firm movers. Promotions are meaningful for these movers – high promotion firm movers who are promoted within a year of moving receive wage increases of 15.6 (s.e. 0.97) log points, while corresponding low promotion firm movers receive wage increases of 11.9 (s.e. 0.66) log points. These effects decay over time, but remain economically and statistically significant even seven years after the move. Meanwhile, high promotion firm movers who were not promoted within a year of moving initially earn slightly more than corresponding low promotion firm movers, but their earnings are nearly identical more than two years after the move.

One alternative explanation for the estimated promotion effects is that firms simply differ in their willingness to classify a worker in the higher occupation without meaningful differences in real outcomes or job assignments.\(^{28}\) Under this hypothesis, both promoted and unpromoted workers at high promotions firms would be more negatively selected than the same groups at low promotions firms. As a concrete example, suppose the distribution of workers’ wage growth \(\Delta w\) is \(F(\Delta w)\) for both high and low promotion firms, and a firm \(f\) simply defines a worker as a supervisor when \(\Delta w > c_f\) for some cutoff \(c_f\). A high promotions firm \(H\) is a firm with a lower cutoff for promoting workers, so \(c_H < c_L\). Then it follows that

\[
E[\Delta w | \Delta w > c_H] < E[\Delta w | \Delta w > c_L]
\]
\[
E[\Delta w | \Delta w \leq c_H] < E[\Delta w | \Delta w \leq c_L] .
\]

My results from Figure 11 are the opposite, which suggests that differences in promotions reflect real differences in job assignments (and corresponding wage structures) rather than differences in the willingness to report similar jobs as supervisory jobs.

### 6.2 Exits from formal labor force are involuntary

The main results in Section 4 show robust evidence that high promotion firms increase the likelihood that workers exit from the formal labor force. Although employer-to-unemployment transitions are a common proxy for involuntary turnover (for example, in Moscarini and Postel-Vinay, 2018; Sorkin, 2018), the large informal sector in Brazil may complicate their interpretation in my setting. I present two additional pieces of evidence that bolster the interpretation that increased exits reflect the higher use of separations by high promotion firms rather than alternate explanations like different outside options or voluntary quits.

The first result is that the higher formal labor force exit effects are consistent with higher firm separations at high promotion firms. Table A.2 presents the pooled effects of high promotion firms on the probability that the worker is still working at the destination firm. Workers are 4.47 (s.e. 0.82) percentage points more likely to leave their destination firm more than two years after moving to a

\(^{28}\)Although the use of administrative data mitigates some of these concerns, worker occupations are self reported by firms, and there may be additional incentives to classify workers differently due to collective bargaining agreements or the use of job titles as status (Baron and Biehl, 1989; Lagos, 2019).
high promotion firm instead of a low promotion firm, which is more than double the effect on formal labor force exit. However, firm exit is a less direct measure of negative employment outcomes than formal labor force exit, so I use it as a supporting fact rather than the main outcome. Nevertheless, it is reassuring that the effects on formal sector exit can be rationalized by effects of separations from the destination firm.

In addition, I directly test for whether high promotion firms affect worker-initiated turnover and find a precise zero effect. A feature of RAIS is that it records the reason why an employment contract is terminated, including whether the termination was initiated by the firm or by the worker. This distinction matters in Brazil because the employer pays higher separation penalties for employer terminations without cause (including layoffs). I classify employer terminations with or without cause (i.e., firings or layoffs) as firm-initiated separations, and I classify voluntary quits as worker-initiated separations.\(^{29}\) I observe reasons for separation preceding around half of spells outside of formal employment, of which 77.6% are firm-initiated and 14.5% are worker-initiated. Figure 12 decomposes the estimated effect of moving to a high promotion firm on the likelihood of each type of exit. Firm-initiated exits account for virtually all of these additional separations, whereas high promotion firms' effects on worker-initiated exits are precisely zero.

6.3 Promotions and exits are both driven by high potential workers

To test whether promotions mediate both positive and negative job outcomes, I compare the effects of high promotion firms for workers who are ex-ante more versus less likely to be promoted. Abadie et al. (2018) cautions that even using prior characteristics to predict subsequent outcomes can introduce potential bias due to overfitting, so I split my analysis sample into a 25% hold-out sample and a 75% estimation sample. I first estimate the equation

\[
\text{Promoted}_{i,c+1} = \theta Z_{i,c-1} + \epsilon_i
\]

(10)
on the 25% hold-out sample of movers. I then rank workers in the 75% estimation sample by their predicted promotion potential \(\hat{\theta} Z_{i,c-1}\), and I separately estimate the baseline event study Equation 6 for the top and bottom tercile of workers by promotion potential.\(^{30}\)

Figure 13 compares the main effects of high promotion firms on worker promotions, formal labor force exit, and average earnings for the baseline, low promotion potential, and high promotion potential samples. The effects of high promotion firms on both promotions and formal labor force exit are largest for the tercile of workers that are most likely to be promoted. Meanwhile, high promotion firms only slightly increase the probability that a worker from the bottom tercile of promotion potential would be promoted or exit the formal labor force.

The fact that the effect of high promotion firms on worker promotions is strongest for the high potential workers is reassuring but unsurprising. On the other hand, the fact that the negative effects of high promotion firms are also particularly relevant for these high potential workers contradicts the alternative explanation that high promotion firms simply have more volatile labor demand. For

\(^{29}\)I combine all other stated reasons into a single category, including contract expirations, transfers, and retirement.

\(^{30}\)Note that by separately estimating the event study for the two samples, rather than simply allowing for different treatment effects by worker potential, I am also allowing for the controls and trends to vary arbitrarily across the two worker groups. So, this exercise also provides additional support that my baseline effects are not driven by differential sorting of workers.
example, firms with “dual labor markets” may offer some workers both job security and promotion opportunities and other workers precarious jobs that are eliminated during demand downturns. My results instead suggest that promotions and exits are related outcomes that are two sides of the same coin, which supports the role of employer learning as the key mechanism.  

6.4 Survey of firm labor practices are consistent with estimated effects

Finally, I validate my worker-level evidence using structured interview data from an internationally comparable survey of manufacturing plants’ human capital management practices. I view these data as supporting evidence that my results about the worker-level effects on promotions and exit are consistent with managers’ actions. Furthermore, the international comparability of the survey allows me to assess the extent to which the patterns are specific to Brazil.

Two questions from the World Management Survey connect to the worker-level outcomes that I study. Table A.3 reports each question from the questionnaire and its corresponding scoring criteria. The question on promotions from the questionnaire is primarily about the reason for promotion rather than the frequency of promotions. However, in my setting, a firm that primarily promotes workers based on tenure should have negligible estimated effects on promotions since my sample focuses on workers who move firms and consequently are at the bottom of the seniority ladder. Meanwhile, the question on firings directly connects to my results on formal labor force exits given the discussion in Section 6.2.

Figure 14 plots the average firings score by firms’ promotions score for three groups of countries. First, I find that firms that are more likely to develop and promote high performing workers are also more likely to fire low performing workers. This is consistent with my baseline empirical results, as well as the general finding in the management literature that the use of “good” management practices tends to be correlated with better management practices (Bloom et al., 2019; Cornwell et al., 2021). Second, the correlations between firms’ promotions practices and firing practices are similar between Brazil, OECD countries, and non-OECD countries. These three groups differ substantially in their labor market institutions, industrial compositions, and the allocation of production factors. The similarity of the relationship across all three settings suggests that my results are driven by a general economic mechanism rather than any features that are specific to Brazil.

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31 In the model, the effects on high potential workers can be rationalized by workers for whom trial promotions are more relevant (so $Q$ is higher). On the other hand, mechanisms without learning (e.g., differences in the selection of workers) would have trouble explaining this pattern given promotions are generally negatively correlated with labor force exit.

32 There are general caveats to interpreting survey responses since managers’ reported promotions practices may reflect over-optimism or worker sorting rather than the firm’s true causal effects. Some of these concerns are mitigated by the survey I use, which comes from a series of structured interviews between MBA students and plant managers that are designed to minimize incentives to misreport firm practices. For more details about the survey, see [Bloom et al. 2014].

33 The correlation between these two practices is also notable since analyses of internal labor markets usually argue that investment is more likely when turnover is low (for example, see Doeringer and Piore, 1971; Prendergast, 1993).

34 The set of OECD countries in the sample are Australia, Canada, Chile, Columbia, France, Germany, Great Britain, Greece, Italy, Japan, New Zealand, Poland, Portugal, Ireland, Spain, Sweden, United Kingdom, and the United States. The set of non-OECD countries in the sample are Argentina, China, Ethiopia, Ghana, India, Kenya, Mexico, Mozambique, Myanmar, Nicaragua, Nigeria, Singapore, Tanzania, Turkey, Vietnam, and Zambia.
7 Equilibrium Effects of Employer Learning

In addition to direct effects on the labor market outcomes of their employed workers, high learning firms also have equilibrium effects on the wage structure for all workers. To explore these implications, I endogenize the employment share of high learning firms and the secondary market contact rate from the partial equilibrium model in Section 2. I follow Lise and Robin (2017) in assuming that firms set the number of vacancies based on expected profits, and the total cost of vacancies is convex. If the vacancy supply function is sufficiently convex (e.g., if it is log-convex), then high learning employers post a proportionately larger share of vacancies in more productive areas. A higher share of high learning employers increases the adverse selection of job movers, which decreases market wages for promoted and especially unpromoted workers. As a result, occupational wage inequality increases. I show that these equilibrium predictions also hold robustly in the data – municipalities with more high learning employers have higher wage differentials between promoted and unpromoted workers even after controlling for a wide range of worker-, job-, and municipality-level characteristics.

7.1 Endogenizing vacancy creation

In addition to the baseline setup, suppose that locations differ in a multiplicative productivity term, \( \psi \), so output in region \( r \) for a worker of type \( \theta_i \) in occupation \( o \) is

\[
 f_{roi} = \psi f_o (\theta_i) .
\]

There is an equal mass of atomistic firms, each choosing a density of vacancies \( v \) at a total cost of \( c(v) \) at the start of the period. The matching technology is constant returns to scale and does not distinguish between the type of firm offering the vacancy or the type of worker. Initial job matches are formed through matching workers with initial vacancies. Similarly, contact with the secondary market is established by matching initially employed workers with initially unfilled vacancies, so the number of workers who will make contact with the secondary market can be written as

\[
 m^s = M (m^I, v - m^I) ,
\]

where \( m^I = M (l, v) \) is the mass of initially employed workers, \( l \) is the total mass of workers, \( v \) is the total mass of vacancies, and \( M \) is the matching function. I assume that conditional on arriving at the secondary market, firms still compete for workers as in Section 2.2.

Implicit in this setup are two simplifying assumptions to ensure the model remains tractable. First, I rule out any subsequently vacated positions (e.g., from a firm that fired its initial worker) from also joining the secondary market so that employment shares always correspond to vacancy shares. Second, I rule out any initially unmatched workers joining the secondary market so the initial level of vacancies will not affect the equilibrium degree of adverse selection.

The Perfect Bayesian equilibrium in this extended model is a set of worker and firm strategies such that firms set the number of vacancies that maximize expected profits given the vacancy setting decisions of other firms, and such that the conditions in the partial equilibrium model in Section 2.2 are also satisfied. Proposition 3 compares the equilibrium differences between regions that only vary in general productivity due to the differential entry of high learning employers.
Proposition 3. Suppose (i) vacancy creation as a function of expected profits is log-convex and (ii) the elasticity of re-employment with respect to the number of high learning employer vacancies exceed the elasticity of expected secondary market worker output. Then, in more productive regions: (i) high learning employers post a greater share of vacancies, (ii) offered wages for incumbent workers are higher (iii) wage differentials between promoted and unpromoted workers are larger.

The full proof for Proposition 3 is in Appendix B and relies on two assumptions. The first assumption ensures that vacancy creation is sufficiently responsive so that increases in the difference in expected profits between high and low learning employers will increase the share of total vacancies created by high learning employers. The second assumption ensures that the net effect of an additional vacancy from high learning firms is positive for workers’ expected wages.

The need for the second assumption highlights the negative equilibrium effects of high learning employers on worker wages in the model. From Equation 4, offered wages at incumbent firms match expected offers in the secondary market. Holding the share of high learning employers equal, increasing the total number of vacancies would stiffen competition from the secondary market and unambiguously increase offered wages. On the other hand, holding the total number of vacancies equal, increasing the share of high learning employers would exacerbate the adverse selection of workers entering the secondary market. Secondary market wages would correspondingly fall, which erodes wages at incumbent firms for promoted and especially unpromoted workers. The assumption ensures that the positive equilibrium effects of the vacancy dominate the negative equilibrium effects of high learning employers, but wage inequality would increase in either case.

35. Although I motivate differences in high learning employer shares as arising from vacancy creation in response to productivity differences, neither of those components are crucial for this mechanism. The equilibrium channel where high learning employers suppress wage competition would exist whenever wages at determined as in the partial equilibrium model.

7.2 Testing for equilibrium effects on occupational wage structure

Proposition 3 yields testable implications about a region’s high learning employer share and its market-level wages. As an empirical analog, I define

$$\bar{H}_m = \frac{\sum Q_j = Q_h L_f}{\sum Q_j = Q_h L_f + \sum Q_j = Q_L L_f}$$

as the (employment-weighted) share of high promotion firms in a municipality, and I estimate the regression

$$y_{int} = \beta_1 \bar{H}_m + \beta_2 [\bar{H}_m \times P_{it}] + \theta_1 X_{it} + \theta_2 (Z_m, Z_{it}) + \gamma_{op} + \psi_f + \tau_{rot} + \epsilon_{it} \quad (11)$$

on a longitudinal 5% sample of all promotion-track workers between the ages of 25 and 50 in Brazil. $P_{it}$ is an indicator for whether the worker is in a supervisory role, $X_{it}$ controls for worker characteristics (a quadratic in age interacted with gender along with indicators for the worker’s education, race, and state), and $Z_m$ controls for region size. Finally, $\gamma_{op}$ is a full set of occupational-group-by-superior fixed effects, $\psi_f$ are firm fixed effects, and $\tau_{rot}$ are state-by-occupational-group trends.

Table 6 reports the estimates of $\beta_1, \beta_2$, the correlation between regional wages and the high promotion employment share, as I progressively add the controls in Equation (11). Both $\beta_1$ and
\( \beta_2 \) are positive and substantial in the basic specification that only controls for flexible trends in wages at the state-by-occupation level. Adding additional controls generally have little effect on the estimates despite their substantial explanatory power on the variance in wages, which suggests that the estimates of \((\beta_1, \beta_2)\) are not driven by observable differences between the types of jobs, workers, or the size of the municipalities. The one exception is that the estimate of \(\beta_1\), the overall regional wage premium, becomes small and insignificant upon the inclusion of firm fixed effects, but the regional supervisor wage premia remain substantial. Under my preferred specification that controls flexibly for worker characteristics and different wage structures within occupations (column 3), moving from the 10th to the 90th percentile in the population-weighted municipal high promotion firm share (from 17.3\% to 50.8\%) increases regional wages for production workers by 4.69 log points and the region wage premium for supervisors by an additional 6.57 log points, which is 39\% of the average supervisor wage premium from Table 2.

8 Structural quantification

The model in Section 2 and its extension in Section 7 are both highly stylized to clarify the mechanism of employer learning and characterize its equilibrium implications. However, the model’s basic components governing learning and job assignment also have empirical content, and they can be mapped to the data under minimal assumptions about wage setting or the labor market parameters. In this section, I show how those key parameters can be identified using the employer effects estimates under internally consistent model restrictions. The resulting estimates allow me to quantify the degree of employer learning by high and low promotion firms as well as the implied degree of skill misallocation and adverse selection in my setting.

8.1 Model identification and estimation

The partial equilibrium model in Section 2 can be separated into two parts. The first half of the model characterizes the incumbent employer’s learning and job assignment decision while taking market wages as given. The second half of the model specifies the equilibrium wage from the secondary market. This separability between the two parts is crucial for transparently mapping my estimates to the learning and job assignment problem while remaining agnostic about the exact form of wage setting. The key condition is that employers must find the efficient assignment of jobs to workers to be incentive compatible. In other words, employers must find it optimal to promote workers of known high ability, fire workers of known low ability, and retain workers of unknown ability. This incentive compatibility condition would be satisfied under a variety of wage setting institutions that would be relevant in Brazil, including rent sharing, wage bargaining, wage floors, or firm-wide wage schedules. As a result, predictions from the learning and job assignment problems are particularly likely to be robust to departures from the stylized setting of the model, and I focus on quantifying their relevant parameters.

To further bolster the transparency and robustness of the quantification exercise, I use a methods of moments approach for estimation. The approach allows me to be explicit about the exact moments from the data that identify the parameters and the relationship between the two (Andrews et al., 2020). I can also choose the moments to reflect the model’s assumptions about timing and heterogeneity (similar to the approach from Lamadon et al., 2019). Table 7 summarizes the parameters of
interest and the moments used to identify the parameters.

I first calibrate two moments “outside” of the model. I use the probability that a promoted worker remains a supervisor upon moving employers to calibrate the asymmetric information parameter $\kappa$. I also use the average job destruction rate estimated in Dix-Carneiro et al. (2021), aggregated to the average length of the outcome period in the sample, to calibrate the exogenous separation rate $\delta$. Since there is greater uncertainty in these moments, I systematically vary the calibrated values to ensure that my conclusions are not sensitive to the choice of these values.

I jointly identify the remaining parameters governing job assignment and turnover $(\bar{Q}_H, \bar{Q}_L, \alpha, g)$ by matching the sample means and treatment effects from the movers analysis using classical minimum distance. The key model restriction that allows me to identify the model is that I assume movers to high versus low promotion firms differ only in the rate of learning at their destination firms. This restriction ensures that the model analogs for the means and treatment effects estimates for promotions and formal labor force exit are determined by the four parameters alone. In theory, I can calibrate the model using observational data from all workers in my sample. However, the comparability of baseline characteristics and the absence of systematic pre-trends in earnings between high promotion firm and low promotion firm movers (as discussed in Sections 4.2 and 5) suggests that the model restriction is most plausible in the movers analysis. I use the sample means and treatment effects from at least two years after workers initially move firms to allow enough time for learning and turnover to take place.

It is straightforward to implement the quantification approach using a minimum distance estimator since the model-implied analogs of the moments can be computed in closed form. The estimate $\hat{\theta} = (\bar{Q}_H, \bar{Q}_L, \alpha, g)$ is defined as

$$\hat{\theta} = \arg \min_{\theta} (\hat{\pi} - h(\theta))^T W (\hat{\pi} - h(\theta)),$$  \hspace{1cm} (12)

where $\hat{\pi}$ is the vector of empirical moments, $h(\theta)$ is the vector of corresponding model outcomes (given $\theta$), and $W$ is a positive definite weighting matrix. Since $\hat{\pi}$ comes directly from sample calculations, I calculate its full cluster-robust variance-covariance matrix $\hat{\Omega}$ by stacking the estimation equations and clustering the stacked equation by the worker’s destination firm. I use the inverse of the variance-covariance matrix as my weighting matrix (so $W = \hat{\Omega}^{-1}$), although I can generally match the empirical moments exactly so the choice of the weighting matrix only affects the efficiency of my estimator. Asymptotically valid standard errors for $\hat{\theta}$ also follow from $\hat{\Omega}$ using the sandwich estimator from Newey and McFadden (1994). For more details, see Appendix C.3.

### 8.2 Parameter estimates

Table 8 summarizes the parameter estimates under my baseline calibration, which have intuitive interpretations given the simple structure of the model. I estimate from $\alpha$ that 21.5% of workers in

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36As an example, suppose that both sample means and treatment effects on promotions are large, but sample means and treatment effects on labor force exit are small. The moments on promotions would imply that the relative difference in learning between high and low employers is large, overall learning is sufficiently high, and the share of high ability workers in the population is large. The moments on employment would then distinguish between a high overall rate of learning versus a large share of high ability workers and pinpoint the implied re-employment rate.

37This approach does ignore the uncertainty due to the calibrated parameters, as discussed by Cocci and Plagborg-Møller (2019). I assess the sensitivity of $\hat{\theta}$ to calibrated values by explicitly assuming alternative calibrations to account for model uncertainty in addition to the (known) sampling uncertainty of the sample means.
the sample are of high ability. Given that the average share of workers who are in supervisory roles at least two years after initially moving firms is only 2.3%, my estimate implies that 87.1% of high ability workers are mismatched in low complexity roles or unemployment. Part of the reason for the misallocation is because turnover is reasonably high, and information about worker quality is likely to be lost when workers change firms. Under the estimated parameters, a worker who is promoted by their incumbent employer only has a 75.3% chance of remaining in the supervisor position after potential separation shocks and secondary market matching are realized.

But the primary reason for the high rate of mismatch is that the estimated rate of learning for even high promotion employers is only 20.5%, so most workers’ abilities remain unknown to employers. Although learning is generally low in this setting, it is still substantial compared to the overall rate of worker turnover. As a result, I estimate that adverse selection can be a meaningful source of ex-post market power – workers who change employers are only 71.3% as likely to be of high ability as the overall population of workers in this sample.

Finally, the structural model also gives me a framework to quantitatively assess the overall degree to which high and low promotion firms differ. I estimate that high promotion firms, on average, are 5.8 percentage points more likely than low promotion firms to learn about the ability of their workers. This difference is larger than the treatment effects on either promotions or formal labor force exit, as well as the naive sum of the two effects. Intuitively, the estimated long run effects on promotions and exit are attenuated by worker turnover and re-employment. The structural model provides a principled approach to adjust for this attenuation using the labor market parameters, which allows me to map differences in long run outcomes to differences in firm behavior.

Finally, Figure A.19 shows how the main conclusions change when I vary the two calibrated parameters by 50% to 150% of the assumed baseline values. The assumed value for the asymmetric information parameter \( \kappa \) has a quantitatively small effect on my estimates. On the other hand, the assumed rate of exogenous separations \( \delta \) is important for inferring whether a job mover is a low ability worker who was previously fired or a high ability worker who exogenously separated. Moreover, at 50% of the baseline assumed value for \( \delta \), my model can no longer exactly fit the sample means and treatment effect estimates, so those estimates should be interpreted with caution. For all other assumed values of \( \delta \), my estimates for skill misallocation and adverse selection remain similar. Since the baseline assumed value of \( \delta \) is likely a lower bound, the robustness of my conclusions to higher values of \( \delta \) is particularly reassuring.\(^{38}\)

9 Conclusion

I show that employers do influence production workers’ subsequent careers, but the overall effects of these firms are more mixed than what anecdotal “rags to riches” stories may suggest. Production workers who join high promotion firms are more likely to eventually be working as a supervisor, but they are also more likely to leave formal employment altogether, and they do not earn more on average. I argue that these results are most consistent with the explanation that employers’ information about worker ability at the time of hiring is imperfect, and that employers vary systematically in the

\(^{38}\)The external estimate for \( \delta \) is the estimated firm destruction rate from Dix-Carneiro et al. [2021], whereas the parameter in the model is the exogenous worker separation rate. If workers have a positive probability of exogenously separating without the job itself disappearing (e.g., if a worker leaves due to geographic reasons or idiosyncratic preference shocks), then the firm destruction rate would be an underestimate of the exogenous separation rate.
degree to which they learn about the abilities of their workers. Both the treatment effects estimates and a structural quantification show that employer learning is key to rationalizing the effects of employers on worker promotion and exit.

More generally, this paper highlights the role of information, particularly asymmetric information, in determining worker outcomes. Firms acting on information revealed after hiring introduce worker-level risk in employment that is separate from firm-level or market-level risks and has implications for the design of employment protection and unemployment insurance. The adverse selection in the pool of job movers also suppresses workers’ outside options, implying that asymmetric information can be a substantial source of ex-post market power for employers. Finally, my model provides an example where the increase in information about workers exacerbates labor market frictions when that information is privately held, raising a cautionary note about the overall effects of increasingly sophisticated employment practices.

There are also limitations to this paper that would be fruitful avenues for future research. I do not observe information on firm accounts, which would be important for credibly characterizing the magnitude and distribution of rents generated by employer learning and for exploring more general implications of organizational design. Similarly, I do not explicitly model the informal sector, and a full accounting of the employment outcomes for those workers using survey evidence would help inform the overall welfare trade-offs. In addition, unions are prominent institutions in Brazil, and it would be useful to assess the degree to which collective bargaining contracts mediate firm practices. Finally, there may be gender and racial differences in the overall effects of firms in my setting; these questions are outside of the scope of this paper, but they are important for understanding who is benefiting from good opportunities and who is getting shaken off the career ladder.

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Tables and Figures

Figure 1: Example of job output functions

Note: The figure shows an example of two job output functions that generate a motive for promotions. Workers who are believed to be of high ability have higher expected output in the high risk occupation (job 2), whereas workers who are believed to be of low ability have higher expected outcomes in the low risk occupation (job 1). Both occupations provide negative output when workers are sufficiently likely to be of low ability, so the outside option is preferred.

Figure 2: Model Timeline

Exogenous events

* worker’s matched firm is high learning w/ prob \( \rho \)
* firm observes worker quality w/ prob \( Q_f \)
* worker realizes separation shocks w/ prob \( \delta \)

Worker and firm actions

* firm makes job and wage offers
* worker accepts offer or exits
* separated workers find market w/ prob \( g \)
* market observes prior promotion w/ prob \( \kappa \)
* market makes competitive job and wage offers

Production occurs at incumbent firm

Production occurs at secondary market

36
Figure 3: Prevalence of Promotions for Production Workers

Note: The figure plots the share of workers each year that advanced from an elementary production occupation in the previous year to a supervisor occupation in the current year. Within occupation promotions further restricts promotions to changes within the same occupational group. The sample is all workers in the Brazilian formal sector between the ages of 25 and 50. For more details, see Section 3.3.

Figure 4: Timeline of empirical approach

Note: The figure describes the years of data used in each section of the empirical approach. The first four years of data (2003-2006) are reserved for estimating firms’ promotion propensities (see Section 4.1). The analysis sample consists of workers who moved firms between 2008 and 2012 and have three years of pre-move data (see Section 4.2). My data ends in 2015, so the length of post-move outcomes ranges from 4 years (for the 2012 cohort) to 8 years (for the 2008 cohort).
Figure 5: Test for movers balance

Note: The figure plots the difference in average worker characteristics between those that moved to high promotion firms and those that moved to low promotion firms. Age and years of schooling are both scaled by their overall means, so the coefficients are interpreted as relative differences. The first set of estimates are the raw differences across all worker cohorts and only controls for possible differences in composition across worker cohorts. The second set of estimates adds state-by-occupation-by-cohort fixed effects. The final set of estimates also controls for the estimated firm wage premium at the worker’s origin firm. Standard errors are clustered by the worker’s destination firm, and lines indicate the 95% confidence interval.
Figure 6: Impact of high promotion firms on worker promotions

Note: The figure plots event study coefficients from estimating Equation 6 on the baseline sample of all promotion track workers between the ages of 25 and 50 that made an employer-to-employer transition to a high or low promotion firm. The coefficients are the estimated yearly differences in the outcomes of workers who moved to a high promotion relative to workers who moved to a low promotion firm, averaged across all five cohorts of movers. The outcome is whether the worker is working in a supervisor occupation and includes workers who have left formal employment (assumed to not be working as supervisors). Standard errors are clustered by the worker’s destination firm, and lines indicate the 95% confidence interval.
Figure 7: Impact of high promotion firms on formal labor market attachment

Note: The figure plots event study coefficients from estimating Equation 6 on the baseline sample of all promotion track workers between the ages of 25 and 50 that made an employer-to-employer transition to a high or low promotion firm. The coefficients are the estimated yearly differences in the outcomes of workers who moved to a high promotion relative to workers who moved to a low promotion firm, averaged across all five cohorts of movers. The outcome is whether a worker is working in formal employment. Standard errors are clustered by the worker’s destination firm, and lines indicate the 95% confidence interval.
Figure 8: Impact of high promotion firms on log earnings for employed workers

Note: The figure plots event study coefficients from estimating Equation 6 on the baseline sample of all promotion track workers between the ages of 25 and 50 that made an employer-to-employer transition to a high or low promotion firm. The coefficients are the estimated yearly differences in the outcomes of workers who moved to a high promotion relative to workers who moved to a low promotion firm, averaged across all five cohorts of movers. The outcome is log earnings and is only defined for workers in formal employment. Standard errors are clustered by the worker’s destination firm, and lines indicate the 95% confidence interval.
Figure 9: Robustness of main estimates to controls

(a) Effects within 2 years of move

Pooled Short-run Effects
Comparing across controls

(b) Effects more than 2 years after move

Pooled Long-run Effects
Comparing across controls

Note: The figures compare pooled event study coefficients from estimating variations of Equation 6 on the baseline sample. The top panel plots the pooled effects within two years of moving, and the bottom panel plots the pooled effects more than two years after the move. The outcomes are whether the worker is working in a supervisor position, whether the worker is working in any job in formal employment, and the worker’s log earnings conditional on being in formal employment. Basic controls only include age, gender, education controls, and two-way worker and year fixed effects. Extended controls include all of the baseline controls, and additionally include flexible trends based on workers’ baseline earnings as well as time-varying changes to the gender and educational wage structure. Standard errors are clustered by the worker’s destination firm, and lines indicate the 95% confidence interval.
Figure 10: Comparison of main effects between identification strategies

(a) Effects within 2 years of move

Pooled Short-run Effects
Comparing across empirical strategies

(b) Effects more than 2 years after move

Pooled Long-run Effects
Comparing across empirical strategies

Note: The figures compare pooled event study estimates from the baseline research design in Section 4.2 to estimates from the extensions in Section 4.3 that incorporate additional sources of variation. The top panel plots the pooled effects within two years of moving, and the bottom panel plots the pooled effects more than two years after the move. The outcomes are whether the worker is working in a supervisor position, whether the worker is working in any job in formal employment, and the worker’s log earnings conditional on being in formal employment. The mass layoff estimates restrict the sample to workers whose origin firm experienced a mass layoff at the time of the worker’s move. The local hiring estimates are the instrumental variables estimates from using the jack-knifed municipal hiring share as an instrument for the worker’s destination firm. Standard errors are clustered by the worker’s destination firm for the mass layoff estimates and by the destination municipality for the local hiring estimates, and lines indicate the 95% confidence interval.
Figure 11: Differential impact of high promotion firms by worker job levels

Note: The figure plots event study coefficients from estimating Equation 9 on the baseline sample. Workers are split into four groups based on the type of their destination firm as well as whether they were promoted within a year of moving. The plotted groups are high promotion firm movers who were not promoted, high promotion firm movers who were promoted, and low promotion firm movers who were promoted, respectively. The reference group is low promotion firm movers who were not promoted. The outcome is log earnings conditional on being in formal employment. Standard errors are clustered by the worker’s destination firm, and lines indicate the 95% confidence interval.
Note: The figure decomposes the baseline estimate of the effects of high promotion firms on formal labor market attachment by estimating Equation 6 on various types of worker separations. The coefficients are the estimated difference in the outcomes of workers who moved to a high promotion relative to workers who moved to a low promotion firm, averaged across all five cohorts of movers. The first outcome is whether the worker is observed to be outside of formal employment following any recorded reason for separating from their previous employer. The second outcome is whether the worker is observed to be outside of formal employment following an employer-initiated separation. The third outcome is whether the worker is observed to be outside of formal employment following a worker-initiated separation. Standard errors are clustered by the worker’s destination firm, and lines indicate the 95% confidence interval.
Figure 13: Comparison of main effects by worker potential

(a) Effects within 2 years of move

Pooled Short-run Effects
Comparing across worker types

(b) Effects more than 2 years after move

Pooled Long-run Effects
Comparing across worker types

Note: The figures compare pooled event study coefficients from separately estimating Equation 6 on high and low potential workers from the baseline sample. The top panel plots the pooled effects within two years of moving, and the bottom panel plots the pooled effects more than two years after the move. The outcomes are whether the worker is working in a supervisor position, whether the worker is working in any job in formal employment, and the worker’s log earnings conditional on being in formal employment. Worker potential is defined as the worker’s predicted likelihood of being promoted within a year after moving firms based on their characteristics before moving firms (estimated from Equation 10 using a holdout sample of workers). High potential workers are workers in the top tercile of worker potential, and low potential workers are workers in the bottom tercile. Standard errors are clustered by the worker’s destination firm, and lines indicate the 95% confidence interval.
Figure 14: Correlation in firm practices

Note: The figure plots the correlation between the plant’s willingness to promote high performing workers and the plant’s willingness to fire low performing workers, as scored from structured interviews from the World Management Survey. Scores range from 1 to 5 on each question, with 5 as reflecting the most active worker management practices and 1 as reflecting the least active. For more details, see Section 6.4.
Table 1: Example of occupational group with observable line of progression

<table>
<thead>
<tr>
<th>Occupation Code</th>
<th>Title</th>
</tr>
</thead>
<tbody>
<tr>
<td>7601XX</td>
<td>Supervisors of the textile industry</td>
</tr>
<tr>
<td>7610XX</td>
<td>Multipurpose workers in the textile industry</td>
</tr>
<tr>
<td>7611XX</td>
<td>Workers in the classification and washing of fibers</td>
</tr>
<tr>
<td>7612XX</td>
<td>Operators of spinning machines</td>
</tr>
<tr>
<td>7613XX</td>
<td>Operators of looms</td>
</tr>
<tr>
<td>7614XX</td>
<td>Workers in finishing, dying, and stamping</td>
</tr>
<tr>
<td>7618XX</td>
<td>Inspectors and reviewers of textile production</td>
</tr>
</tbody>
</table>

Table 2: Estimates of promotion wage premia

<table>
<thead>
<tr>
<th></th>
<th>Outcome: Log Earnings</th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
<th>(5)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Supervisor</td>
<td></td>
<td>0.628***</td>
<td>0.520***</td>
<td>0.384***</td>
<td>0.170***</td>
<td>0.200***</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.0180)</td>
<td>(0.0185)</td>
<td>(0.0191)</td>
<td>(0.00347)</td>
<td>(0.00309)</td>
</tr>
<tr>
<td>Number of observations</td>
<td>11581373</td>
<td>11581278</td>
<td>11581208</td>
<td>11092695</td>
<td>5616458</td>
<td></td>
</tr>
<tr>
<td>Number of workers</td>
<td>2473852</td>
<td>2473850</td>
<td>2473846</td>
<td>1985349</td>
<td>1071791</td>
<td></td>
</tr>
<tr>
<td>Adjusted $R^2$</td>
<td>0.234</td>
<td>0.407</td>
<td>0.520</td>
<td>0.890</td>
<td>0.874</td>
<td></td>
</tr>
</tbody>
</table>

Controls:
- State-occupation-year FE: Y Y Y Y Y
- Worker controls: Y Y Y
- Worker FE: Y Y
- Firm wage premia: Y

Note: The table reports estimates for the average supervisor wage premium in the Brazilian formal employment sector. The sample is a 5% sample of all workers between the ages of 25 and 50 that work in occupational groups with a well-defined supervisor role. The first column reports the bivariate wage premium and controls only for year fixed effects. Worker controls are a quadratic in age interacted with gender along with indicators for the worker’s education, race, and state. Firm wage premia controls net out the estimated AKM firm fixed effect from worker earnings. Standard errors are two-way clustered at the worker and firm level. Stars indicate the level of significance: * 5%, ** 1%, and *** 0.1%.
Table 3: Role of promotions in lifecycle wage profile

<table>
<thead>
<tr>
<th></th>
<th>Outcome: Log Earnings</th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
<th>(5)</th>
<th>(6)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Age</td>
<td></td>
<td>0.0173***</td>
<td>0.0163***</td>
<td>0.0115***</td>
<td>0.0105***</td>
<td>0.0133***</td>
<td>0.0118***</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.000294)</td>
<td>(0.000321)</td>
<td>(0.000185)</td>
<td>(0.000195)</td>
<td>(0.000238)</td>
<td>(0.000258)</td>
</tr>
<tr>
<td>Supervisor</td>
<td></td>
<td>0.412***</td>
<td>0.393***</td>
<td>0.434***</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.0130)</td>
<td>(0.0112)</td>
<td>(0.0135)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Share of age</td>
<td>explained</td>
<td>0.0547</td>
<td>0.0880</td>
<td>0.111</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Number of obs.</td>
<td>6056674</td>
<td>6056674</td>
<td>6056525</td>
<td>6056525</td>
<td>3217367</td>
<td>3217367</td>
<td></td>
</tr>
<tr>
<td>Number of workers</td>
<td>1697830</td>
<td>1697830</td>
<td>1697814</td>
<td>1697814</td>
<td>978304</td>
<td>978304</td>
<td></td>
</tr>
<tr>
<td>Adjusted $R^2$</td>
<td>0.474</td>
<td>0.489</td>
<td>0.538</td>
<td>0.551</td>
<td>0.483</td>
<td>0.504</td>
<td></td>
</tr>
</tbody>
</table>

Controls:

Worker controls       | Y         | Y         | Y         | Y         | Y         | Y         |
Occupation controls    | Y         | Y         | Y         | Y         | Y         | Y         |
Firm wage premia       |           |           |           |           | Y         | Y         |

Note: The table reports estimates of the average lifecycle wage profile with and without controlling for the average supervisor wage premium in the Brazilian formal employment sector. The sample is a 5% sample of all workers between the ages of 25 and 35 that work in occupational groups with a well-defined supervisor role. The share of age coefficient explained is the relative decrease in the age coefficient after adding an indicator for whether the worker is working as supervisor. Worker controls are indicators for gender, worker education, and race as well as state-by-year fixed effects. Occupational controls are the worker’s occupational tenure and state-by-occupational-group-by-year fixed effects. Firm wage premia controls net out the estimated AKM firm fixed effect from worker earnings. Standard errors are two-way clustered at the worker and firm level. Stars indicate the level of significance: * 5%, ** 1%, and *** 0.1%.
Table 4: Differences between high and low promotion firms

<table>
<thead>
<tr>
<th>Outcome:</th>
<th>Difference</th>
<th>Standard errors</th>
<th>Low prom. firm mean</th>
<th>Adj. $R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Promotions</td>
<td>0.0172***</td>
<td>(0.000152)</td>
<td>0.000159</td>
<td>0.354</td>
</tr>
<tr>
<td>Exit Formal Employment</td>
<td>0.0165***</td>
<td>(0.000744)</td>
<td>0.165</td>
<td>0.00740</td>
</tr>
<tr>
<td>Log Employment</td>
<td>0.490***</td>
<td>(0.00934)</td>
<td>3.584</td>
<td>0.0415</td>
</tr>
<tr>
<td>Age</td>
<td>-0.310***</td>
<td>(0.0186)</td>
<td>35.27</td>
<td>0.00376</td>
</tr>
<tr>
<td>Log Earnings</td>
<td>0.0900***</td>
<td>(0.00417)</td>
<td>6.462</td>
<td>0.00677</td>
</tr>
<tr>
<td>AKM Firm FE</td>
<td>0.0542***</td>
<td>(0.00346)</td>
<td>-</td>
<td>0.00443</td>
</tr>
<tr>
<td>Supervisor Share</td>
<td>0.0392***</td>
<td>(0.000612)</td>
<td>0.0302</td>
<td>0.0789</td>
</tr>
<tr>
<td>Log Earnings Growth</td>
<td>0.00990***</td>
<td>(0.000424)</td>
<td>-</td>
<td>0.00869</td>
</tr>
<tr>
<td>Log Employment Growth</td>
<td>0.0338***</td>
<td>(0.00162)</td>
<td>0.0355</td>
<td>0.00746</td>
</tr>
</tbody>
</table>

Number of firms 69417

Note: The table reports the difference between high and low promotion firms in average firm characteristics between 2004-2006, as well as the means for low promotion firms in each relevant category. The adjusted $R^2$ reports the share of firm-level variation in each outcome that is explained by the firm’s high versus low promotion status. Stars indicate the level of significance: * 5%, ** 1%, and *** 0.1%.
### Table 5: Analysis sample summary statistics

<table>
<thead>
<tr>
<th></th>
<th>Baseline</th>
<th>Mass layoffs</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of workers</td>
<td>1100590</td>
<td>127058</td>
</tr>
<tr>
<td>Number of origin firms</td>
<td>162573</td>
<td>16103</td>
</tr>
<tr>
<td>Number of destination firms</td>
<td>49785</td>
<td>21170</td>
</tr>
</tbody>
</table>

Worker characteristics before move:

- **Age**: 32.94, 33.89
  - [6.761], [7.007]
- **Female**: 0.262, 0.241
  - [0.439], [0.428]
- **Years of schooling**: 10.50, 9.866
  - [2.941], [3.033]
- **Monthly earnings (2010 Reals)**: 1242.9, 1186.4
  - [900.4], [831.7]
- **Share to high promotion firm**: 0.417, 0.442

Worker outcomes > 2 years following move:

- In formal employment: 0.786, 0.765
- At destination firm: 0.326, 0.277
- In supervisor occupation: 0.0231, 0.0349

Note: The table reports summary statistics about the job-to-job movers in the baseline sample and the mass-layoffs subsample. Pre-move worker characteristics refer to the snapshot of worker data from the year before the job-to-job transition ($t = b - 1$). Outcomes more than two years following the move are averaged over all relevant years where the data are available. All statistics on characteristics and outcomes are in means, and standard deviations for continuous measures are in brackets.
Table 6: Estimates of regional wage premia

<table>
<thead>
<tr>
<th></th>
<th>Outcome: Log Earnings</th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
<th>(5)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>High Firm Share (β₁)</strong></td>
<td></td>
<td>0.132***</td>
<td>0.140***</td>
<td>0.140***</td>
<td>0.0397**</td>
<td>0.00850</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.0162)</td>
<td>(0.0151)</td>
<td>(0.0152)</td>
<td>(0.0134)</td>
<td>(0.00544)</td>
</tr>
<tr>
<td><strong>High Firm Share × Super. (β₂)</strong></td>
<td></td>
<td>0.244***</td>
<td>0.237***</td>
<td>0.196***</td>
<td>0.106***</td>
<td>0.159***</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.0423)</td>
<td>(0.0405)</td>
<td>(0.0334)</td>
<td>(0.0287)</td>
<td>(0.0306)</td>
</tr>
<tr>
<td>Number of observations</td>
<td>11569458</td>
<td>11569388</td>
<td>11569388</td>
<td>11569388</td>
<td>11187050</td>
<td></td>
</tr>
<tr>
<td>Number of municipalities</td>
<td>5500</td>
<td>5500</td>
<td>5500</td>
<td>5500</td>
<td>5499</td>
<td></td>
</tr>
<tr>
<td>Adjusted R²</td>
<td>0.408</td>
<td>0.521</td>
<td>0.523</td>
<td>0.539</td>
<td>0.771</td>
<td></td>
</tr>
<tr>
<td>Controls:</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>State-occupation-year FE</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td></td>
</tr>
<tr>
<td>Worker controls</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td></td>
</tr>
<tr>
<td>Occupation-super.-year FEs</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Municipality controls</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Firm FEs</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Note: The table reports estimates for municipal differences in wages and supervisor wage premia in the Brazilian formal employment sector (estimated using Equation [11]). The sample is a 5% sample of all workers between the ages of 25 and 50 that work in occupational groups with a well-defined supervisor track in municipalities with at least 100 workers. The estimands of interest are the wage premium for all workers in municipalities with a high share of high promotion employers (β₁) as well as the differential wage premium for promoted workers in municipalities with a high share of high promotion employers (β₂). Worker controls are a quadratic in age interacted with gender along with indicators for the worker’s education, race, and state. Municipality controls are controls for log employment and the overall hiring share of either high or low promotion firms that enter both linearly and as interactions with supervisor status. Standard errors are clustered by municipality. Stars indicate the level of significance: * 5%, ** 1%, and *** 0.1%.
Table 7: Summary of parameters and moments for identification

<table>
<thead>
<tr>
<th>Description</th>
<th>Moments</th>
<th>Assumptions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calibrated parameters:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \kappa ) Degree of asymmetric information</td>
<td>Share of job changers that remain supervisors</td>
<td>Calibrated from movers data</td>
</tr>
<tr>
<td>( \delta ) Prob. of exogenous separation</td>
<td>Estimated job destruction rate</td>
<td>From Dix-Carneiro et al. (2021)</td>
</tr>
<tr>
<td>Jointly estimated parameters:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \bar{Q}_H ) Rate of learning for high promotion firms</td>
<td>Average share promoted</td>
<td>Constrained efficient promotions + firings</td>
</tr>
<tr>
<td>( \bar{Q}_L ) Rate of learning for low promotion firms</td>
<td>Average share in formal labor market attachment</td>
<td>Random labor market matching</td>
</tr>
<tr>
<td>( \alpha ) Share of high ability workers</td>
<td>Effect of high prom. firms on promotions</td>
<td></td>
</tr>
<tr>
<td>( g ) Prob. of re-employment upon separation</td>
<td>Effect of high prom. firms on formal labor market attachment</td>
<td></td>
</tr>
</tbody>
</table>

Note: The table summarizes the moments and assumptions required to identify the parameters in the partial equilibrium model of employer learning and job assignment. Two parameters - the degree of asymmetric information \( \kappa \) and the probability of exogenous separation \( \delta \) are directly calibrated. The remaining parameters are jointly identified from the means and treatment effects from the baseline movers analysis. The identifying assumptions and model restrictions are discussed in more detail in Section 8.1.
Table 8: Baseline model estimates

<table>
<thead>
<tr>
<th>Definition</th>
<th>Description</th>
<th>Estimate</th>
<th>S.E.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameters:</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\kappa$</td>
<td>Degree of asymmetric information</td>
<td>0.300</td>
<td>-</td>
</tr>
<tr>
<td>$\delta$</td>
<td>Prob. of exogenous separation</td>
<td>0.282</td>
<td>-</td>
</tr>
<tr>
<td>$Q_H$</td>
<td>Rate of learning for high promotion firms</td>
<td>0.205</td>
<td>(0.028)</td>
</tr>
<tr>
<td>$Q_L$</td>
<td>Rate of learning for low promotion firms</td>
<td>0.147</td>
<td>(0.021)</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Share of high ability workers</td>
<td>0.215</td>
<td>(0.031)</td>
</tr>
<tr>
<td>$g$</td>
<td>Prob. of re-employment upon separation</td>
<td>0.410</td>
<td>(0.027)</td>
</tr>
<tr>
<td>Implied measures:</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$(\alpha - \alpha^{'})/\alpha$</td>
<td>Degree of adverse selection in job movers</td>
<td>0.287</td>
<td>(0.038)</td>
</tr>
<tr>
<td>$(\alpha - \mathbb{E}[P])/\alpha$</td>
<td>Share of high ability workers not in supervisor role</td>
<td>0.871</td>
<td>(0.019)</td>
</tr>
</tbody>
</table>

Note: The table reports the estimates from quantifying the partial equilibrium model of employer learning and job assignment. The quantification approach is described in Section 8.1. The definition of high and low promotion firms match the classification used for the estimation of treatment effects, as described in Section 4.1, and the resulting estimates quantify the difference in economic behavior between the two groups. The degree of adverse selection in job movers is the relative decrease in the likelihood that a job mover is of high ability as compared to the general population. Meanwhile, the share of high ability workers is in a lower production role or outside of formal employment, rather than in a supervisory position, reflects skill misallocation. Standard errors are calculated from the joint variance-covariance matrix of empirical moments, which are clustered by the worker’s destination firm.
A  Additional Tables and Figures

Figure A.1: Distribution of firm promotion propensities

Note: The figure plots a kernel density estimate of the distribution of firm promotion propensities ($\eta_j$) between 2004 and 2006. Each firm’s promotion propensity is calculated as the residual firm promotion rates after controlling for differences in worker characteristics and occupational groups and averaged over the three years. Estimates in the figure have been winsorized at the 5th and 95th percentiles. For more details, see Section 4.1.

Figure A.2: Prevalence of Occupations with Clear Promotion Tracks
Figure A.3: Age profile of supervisors and promotions

Figure A.4: Visual intuition for IV first stage
Figure A.5: Impact of high promotion firms on a worker ever being promoted

Figure A.6: Impact of high promotion firms on worker promotions (by cohort)
Figure A.7: Impact of high promotion firms on formal labor market attachment (by cohort)

Figure A.8: Impact of high promotion firms on log earnings for employed workers (by cohort)
Figure A.9: Impact of high promotion firms on worker promotions (continuous measure)

Figure A.10: Impact of high promotion firms on formal labor market attachment (continuous measure)
Figure A.11: Impact of high promotion firms on log earnings for employed workers (continuous measure)

Figure A.12: Impact of high promotion firms on worker promotions (mass layoffs)
Figure A.13: Impact of high promotion firms on formal labor market attachment (mass layoffs)

![Graph of Effect of High Opp. Firm: Formal Employment](image1)

Figure A.14: Impact of high promotion firms on log earnings for employed workers (mass layoffs)

![Graph of Effect of High Opp. Firm: Log Earnings](image2)
Figure A.15: Impact of high promotion firms on worker promotions (local hiring IV)

Figure A.16: Impact of high promotion firms on formal labor market attachment (local hiring IV)
Figure A.17: Impact of high promotion firms on log earnings for employed workers (local hiring IV)
Figure A.18: Comparison of main effects between alternative firm types

(a) Effects within 2 years of move

(b) Effects more than 2 years after move
Figure A.19: Robustness of model estimates to alternate assumptions

Note: The figure shows the model estimates under alternative assumed values on $\kappa$, the degree of asymmetric information on the secondary market, and on $\delta$, the exogenous job separation rate. Adverse selection refers to the relative share of high ability workers in the pool of job-movers compared to the population share of high ability workers. Misallocation refers to the likelihood that a high ability worker is in a lower production role or outside of formal employment, rather than in a supervisory position. The model can no longer exactly fit the sample means and treatment effect estimates at 50% of the baseline assumed value for $\delta$, so those estimates should be interpreted with some caution. The estimates under the baseline assumed value are indicated by dashed lines.
Table A.1: Correlation between measures of firm promotions

<table>
<thead>
<tr>
<th>Measure</th>
<th>Correlation Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline measure</td>
<td>1</td>
</tr>
<tr>
<td>Stayers only</td>
<td>0.925 1</td>
</tr>
<tr>
<td>No controls</td>
<td>0.947 0.885 1</td>
</tr>
<tr>
<td>All promotions</td>
<td>0.731 0.673 0.700 1</td>
</tr>
</tbody>
</table>

Note: This table reports the correlation matrix between the baseline measure of the firm’s promotion propensity $\eta_j$ and alternate measures. All measures reflect the firm’s average $\eta_{jt}$ over 2004-2006 and are winsorized at the 5th and 95th percentiles. The “stayers only” measure restricts the sample to workers who remained in the same firm, so the estimate reflects firms’ internal promotion rates. The “no controls” measure removes any controls and only considers the firms’ raw promotion rate. “All promotions” expands the baseline sample to also include workers who changed occupation groups.

Table A.2: Pooled estimates on the impact of high promotion firms on other worker outcomes

<table>
<thead>
<tr>
<th>Outcome:</th>
<th>(1) Employed at destination firm</th>
<th>(2) Promoted (cond. on formal emp.)</th>
<th>(3) Earnings net of firm wage premia</th>
<th>(4) Contractual salary</th>
<th>(5) Earnings (adjusted for U.E.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Effects within 2 years of moving</td>
<td>-0.0263*** (0.0041)</td>
<td>0.0136*** (0.00097)</td>
<td>-0.00625 (0.0036)</td>
<td>0.00964 (0.0071)</td>
<td>0.00799 (0.0055)</td>
</tr>
<tr>
<td>Effects more than 2 years after moving</td>
<td>-0.0447*** (0.0082)</td>
<td>0.0132*** (0.0010)</td>
<td>-0.00745 (0.0043)</td>
<td>0.0119* (0.0060)</td>
<td>-0.00665 (0.0058)</td>
</tr>
</tbody>
</table>

Number of observations | 8279318 | 7378436 | 6640880 | 6390190 | 8279252 |
Number of dest. firms  | 45870   | 45870   | 45654   | 45496   | 45870  |
Adjusted $R^2$         | 0.617   | 0.304   | 0.795   | 0.776   | 0.775  |

Note: The table reports additional pooled event study coefficients from estimating Equation 6 on the baseline sample. The outcomes are whether the worker is employed at their original destination firm, whether the worker is promoted (conditional on the worker remaining in formal employment), the worker’s log earnings after netting out the AKM firm effect, the worker’s contractual salary, and a lower bound for worker earnings that include exiters (adjusting for the value of non-work time). Standard errors are clustered by the worker’s destination firm. Stars indicate the level of significance: * 5%, ** 1%, and *** 0.1%.
Table A.3: World Management Survey questions and scoring criteria

<table>
<thead>
<tr>
<th>Question</th>
<th>Score</th>
<th>Criteria</th>
</tr>
</thead>
<tbody>
<tr>
<td>Developing Talent and</td>
<td>1</td>
<td>People are promoted primarily upon the basis of tenure</td>
</tr>
<tr>
<td>Promoting High Performers</td>
<td>5</td>
<td>We actively identify, develop and promote our top performers</td>
</tr>
<tr>
<td>Removing Poor Performers/Making</td>
<td>1</td>
<td>Poor performers are rarely removed from their positions</td>
</tr>
<tr>
<td>Room for Talent</td>
<td>5</td>
<td>We move poor performers out of the company or to less critical roles as soon as a weakness is identified</td>
</tr>
</tbody>
</table>

Note: The table reproduces the question and scoring rubric for the promotion and firing practice questions from the World Management Survey. All survey responses range from 1 to 5, with 5 indicating the most active firm practice and 1 indicating the least active. For more details, see Section 6.4.
Table A.4: Estimates of regional differences in labor market attachment

<table>
<thead>
<tr>
<th></th>
<th>Outcome: Leave formal labor market (next year)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(1)</td>
</tr>
<tr>
<td>High Firm Share ($\beta_1$)</td>
<td>0.0294***</td>
</tr>
<tr>
<td></td>
<td>(0.00315)</td>
</tr>
<tr>
<td>High Firm Share $\times$ Super. ($\beta_2$)</td>
<td>-0.0385***</td>
</tr>
<tr>
<td></td>
<td>(0.00620)</td>
</tr>
<tr>
<td>Number of observations</td>
<td>10489980</td>
</tr>
<tr>
<td>Number of municipalities</td>
<td>5489</td>
</tr>
<tr>
<td>Adjusted $R^2$</td>
<td>0.0233</td>
</tr>
</tbody>
</table>

Controls:
- State-occupation-year FE: Y Y Y Y Y
- Worker controls: Y Y Y Y Y
- Occupation-super.-year FEs: Y Y Y
- Municipality controls: Y
- Firm FEs: Y

Note: The table reports estimates for municipal differences formal labor market attachment in the Brazilian formal employment sector (estimated using Equation (11)). The sample is a 5% sample of all workers between the ages of 25 and 50 that work in occupational groups with a well-defined supervisor track in municipalities with at least 100 workers. The estimands of interest are the likelihood of leaving formal employment for all workers in municipalities with a high share of high promotion employers ($\beta_1$) as well as the differential likelihood for promoted workers in municipalities with a high share of high promotion employers ($\beta_2$). Worker controls are a quadratic in age interacted with gender along with indicators for the worker’s education, race, and state. Municipality controls are controls for log employment and the overall hiring share of either high or low promotion firms that enter both linearly and as interactions with supervisor status. Standard errors are clustered by municipality. Stars indicate the level of significance: * 5%, ** 1%, and *** 0.1%.
Table A.5: Sensitivity of model parameters to empirical moments (Λ)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Sensitivity to η</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\bar{Q}_H$</td>
<td>8.13 0.95 -19.32 -11.14</td>
</tr>
<tr>
<td>$\bar{Q}_L$</td>
<td>7.58 0.68 -19.02 -7.99</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>-2.23 -1.08 24.59 11.96</td>
</tr>
<tr>
<td>$g$</td>
<td>7.31 3.55 -21.58 -10.49</td>
</tr>
</tbody>
</table>

Note: The ordering of the empirical moments are the average share of workers promoted, the average share of workers in formal employment, the effect of high promotion firms on worker promotions, and the effect of high promotion firms on formal employment. The interpretation of the sensitivity matrix is that for a local perturbation of the empirical moments that converges to $\eta$, the first-order asymptotic bias in the parameter estimates are $\Lambda \eta$. For more details, see Section C.3.2.
B Proofs of Propositions

B.1 Partial Equilibrium Model

**Proposition.** If information about job assignments on the secondary market is sufficiently weak (so \( \kappa \) is sufficiently small), then a unique Perfect Bayesian equilibrium exists. In this equilibrium, (i) job assignments for workers are efficient (given firms’ information about workers) (ii) all turnover is involuntary (iii) wages are given by Equations 2 and 4.

**Proof.** I characterize the equilibrium by solving the problem backward. I conjecture that the incumbent firms will promote workers that are revealed to be high ability, fire workers that are revealed to be low ability, and retain all workers whose abilities are still unobserved, and I show that this conjectured behavior is optimal given secondary market wages. I then prove uniqueness by showing that this conjectured behavior is the only one consistent with an equilibrium.

For separated workers who successfully convinced the secondary market that they were previously promoted, the secondary market will infer that they were high ability and offer the expected output

\[ w^S_2 = f_2(\theta_H). \]

Meanwhile, the likelihood that a low ability worker enters the unknown secondary market workers pool is

\[ \delta + (1 - \delta) \left( \frac{\rho Q_H + (1 - \rho) Q_L}{\text{prob. fired}} \right) \equiv \delta + (1 - \delta) \bar{Q}, \]

whereas the likelihood that a high ability worker enters the unknown worker pool is \( \delta (1 - \bar{Q} \kappa) \). By Bayes’ rule,

\[
\alpha' \equiv Pr(\theta = \theta_H | \text{unknown quality}) \\
= \frac{\alpha \delta (1 - \bar{Q} \kappa)}{\alpha \delta (1 - \bar{Q} \kappa) + (1 - \alpha) \left( \delta + (1 - \delta) \bar{Q} \right)} \\
< \alpha.
\]

Since low ability workers are both more likely to be fired and less likely to convince new employers that they are high ability, they are going to comprise a higher share of the secondary market workers of unknown quality than in the general population. So the secondary market is adversely selected. The degree of adverse selection is higher when there is greater learning by initial employers (\( \bar{Q} \)) or by the secondary market (\( \kappa \)), and lower when there are more exogenous separations (\( \delta \)). Assuming that it is still optimal for secondary market firms to assign workers of unknown quality to the low complexity occupation, offered wages for these workers will be their expected output, so

\[ w^S_1 = \alpha' f_1(\theta_H) + (1 - \alpha') f_1(\theta_L). \]

Next, I can then verify that the conjectured job assignment by incumbent firms is indeed optimal given the secondary market offers \( w^S_1, w^S_2 \) and characterize the incumbent firms’ wage offers.

The incumbent firms earn positive profits from promoted workers of known high ability regardless
of $g$ because the worker is not guaranteed to remain promoted in the secondary market. So, the incumbent firm only needs to offer a promoted worker their expected outside wage to retain them:

$$w_I^2 = g \left[ \kappa w_S^2 + (1 - \kappa) w_I^S \right] < g f_2(\theta_H).$$

Similarly, the incumbent firm also benefits by retaining the workers whose ability it did not observe since the firm has private information that those workers are not adversely selected. For those workers, the probability that they are the high type is still $\alpha$, so the firm makes positive profits by retaining those unknown workers and offering them the expected outside wage for workers of unknown ability:

$$w_I^1 = g \left[ \alpha' f_1(\theta_H) + (1 - \alpha') f_1(\theta_L) \right] < g E[f_1(\theta)|\alpha].$$

Finally, for workers who are observed to be low ability, $f_2(\theta_L) < f_1(\theta_L) < 0$, so the firm is better off firing them rather than retaining them with any positive wage.

For this equilibrium to exist, two conditions need to hold. First, the expected productivity for unknown workers in the secondary market needs to be positive, so

$$\frac{\alpha' f_1(\theta_H) + (1 - \alpha') f_1(\theta_L)}{= E[f_1(\theta)|\alpha']} \geq 0.$$

This condition also implies that the incumbent firm will also find it optimal to retain workers whose ability is unobserved, since $\alpha > \alpha'$. In addition, the wage gain upon promotion needs to be sufficiently low for the incumbent firm to still prefer to promote workers of high ability, so

$$f_2(\theta_H) - w_I^2 \geq f_1(\theta_H) - w_I^1.$$

Rearranging using the expression for wages,

$$f_2(\theta_H) - f_1(\theta_H) \geq w_I^2 - w_I^1 = g \left[ \kappa w_S^2 + (1 - \kappa) w_I^S - w_I^S \right] = g \kappa (f_2(\theta_H) - E[f_1(\theta)|\alpha']).$$

$\alpha'$ is decreasing in $\kappa$ (since increasing the informativeness of job assignments reduces the likelihood that a high ability worker joins the unknown workers pool), so the right hand side of the inequality is also decreasing in $\kappa$. So, decreasing $\kappa$ relaxes both inequality constraints, and both conditions clearly hold when $\kappa \to 0$ as long as

$$E[f_1(\theta)|\alpha' = \alpha \delta / (\delta + (1 - \alpha) (1 - \delta) \bar{Q})] \geq 0,$$

so the equilibrium exists whenever $\kappa$ is sufficiently small.

Finally, I show that if $\kappa$ is sufficiently small such that the equilibrium exists, it is also the unique equilibrium. To do so, it suffices to show that for the incumbent firm, firing low ability workers, promoting high ability workers, and retaining unknown workers is the only strategy that is consistent with an equilibrium.

Clearly, there can be no equilibrium that exists where the incumbent firm retains all workers
since the output of workers with $\theta = \theta_L$ is strictly less than the outside option. The firm will also never retain low ability workers but fire unknown workers, since the market wages for those two types are identical and the expected productivity of the latter strictly dominates the former.

Similarly, there can be no equilibrium where the incumbent firm retains high ability workers only. Suppose the incumbent firms retain high ability workers and fire all other workers. This implies that expected outside wages exceed expected productivity for workers whose ability is unknown, which cannot be consistent with the competitive secondary market since the secondary market is adversely selected.

So, it suffices to consider whether an equilibrium exists where the incumbent firm treats high ability workers differently. There can be no equilibrium where the incumbent firm will fire high ability workers, since their expected outside wage will always be weakly less than $f_2(\theta_H)$. Similarly, if the incumbent firm keeps all high ability workers in the low complexity job, secondary market wages for workers of unknown quality, $w^S_1$, rises, while secondary market wages for any promoted workers would remain the same. This strictly relaxes the incentive compatibility problem for promotions, so the incumbent firm would profitably deviate by promoting high ability workers instead.

It then follows that under the conditions where the conjectured equilibrium exists, the equilibrium where the incumbent firm promotes high ability workers, fires low ability workers, and retains workers of unknown ability in the low complexity job is also the unique equilibrium. □

**Proposition.** In the equilibrium described in Proposition 1, workers initially employed at high learning firms are (i) more likely to be promoted and (ii) more likely to become unemployed than workers initially employed at low learning firms.

**Proof.** This follows directly from the characterization of the equilibrium. The incumbent firm will promote all high ability workers and fire all low ability workers. Since the composition of workers and labor market parameters are the same between high and low learning firms, the results follow from differences in learning rates.

Specifically, the likelihood that a worker starting at firm $f$ will be promoted by the end of the period is

$$\Pr(\text{Promoted}|Q_f) = \alpha Q_f (1 - \delta + \delta g \kappa),$$

and the likelihood that a worker will be be unemployed is

$$\Pr(\text{Unemployed}|Q_f) = (1 - g) [\delta + (1 - \alpha) (1 - \delta) Q_f].$$

Both likelihoods are increasing in $Q_f$. □

**B.2 General Equilibrium Model**

**Proposition.** Suppose (i) the marginal cost for vacancies $c'(v)$ is log-concave and (ii) the elasticity of re-employment with respect to the number of high learning employer vacancies exceed the elasticity of expected secondary market worker output. Then, in more productive regions: (i) high learning employers post a greater share of vacancies, (ii) offered wages for incumbent workers are higher (iii) wage differentials between promoted and unpromoted workers are larger.

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1. So, the firm's expected profits from a vacancy filled with a new worker is

\[ \Delta \pi = V M \begin{cases} \frac{V_H}{V_H + V_L} & \text{if } \lambda > \psi, \\ M \left( m^f, V_H + V_L - m^f \right) & \text{for all } \lambda > \psi. \end{cases} \]

where \( M \) is the reduced form matching function that relates the level of job matches to the number of workers \( l \) and vacancies \( v \), and \( m^f = (l, V_H + V_L) \) is the number of initially matched workers. Conditional on the number of vacancies (and their implied labor market parameters), the job assignment, offer, and secondary market decisions will follow the characterization in Proposition 1. So, the firm’s expected profits from a vacancy filled with a new worker is

\[
E[\pi_f | V_H, V_L] = (1 - \delta) \left\{ Q_f \alpha \left( \frac{f_2 (\theta_H) - w_h^f}{\text{profits from promoted}} \right) + (1 - Q_f) \left( \frac{E[V f_1 (\theta_H) | \alpha] - w_v^f}{\text{profits from unpromoted}} \right) \right\},
\]

where \( V_H, V_L \) are the total high and low learning firm vacancies in the market, respectively, and all other objects match their definition from Proposition 1. The firm only profits upon successfully retaining an initially assigned worker. Any possibility that a vacancy is filled in the secondary market is irrelevant since the secondary market is competitive.

In the vacancy creation problem, the firm solves

\[
max_v h (V_H, V_L) E[\pi_f | V_H, V_L] v - c (v),
\]

where \( h \) is the probability that a vacancy will be initially matched with a worker. Note that the firm’s choice of \( v \) does not affect \( h (V_H, V_L) E[\pi_f | V_H, V_L] \) under the assumption that each firm is atomistic. The first order condition to the vacancy problem equates the marginal cost of the vacancy to the expected equilibrium profits:

\[
c' (v) = h E[\pi_f | V_H, V_L],
\]

so the equilibrium share of vacancies from high learning firms is:

\[
s = \frac{v \left( h E[\pi_H | V_H, V_L] \right)}{v \left( h E[\pi_H | V_H, V_L] \right) + v \left( h E[\pi_L | V_H, V_L] \right)},
\]

where \( v (\pi) \) is the vacancy supply function given (expected) profits \( \pi \). \( s \) is always increasing in \( \psi \) if and only if

\[
\frac{v' (\lambda \psi) \lambda}{v (\lambda \psi)} > \frac{v' (\psi)}{v (\psi)}
\]

for all \( \lambda > 1 \). A sufficient (but not necessary) condition for this is if \( v \) is log-convex, which is satisfied if \( v = e^x \) (i.e., \( c' \) is log), or if \( v (\pi) = \pi^{-a} \) for some \( a > 0 \).

Define firm’s solution to the optimal vacancy problem as \( v^*_f (V_H, V_L) \), where \( V_H, V_L \) are the total number of vacancies posted by high learning and low learning firms in the market. The equilibrium is the fixed point where \( v^*_f (v_H, v_L) = v_f \) \( \forall f \in \{H, L\} \). To see that this fixed point exists under my

\[ \text{Proof.} \] Under the assumptions on labor market matching, the market level of high learning firm vacancies \( V_H \) and low learning firm vacancies \( V_L \) imply the labor market parameters \( \rho \) and \( g \) as:

\[
\rho = \frac{V_H}{V_H + V_L}, \quad g = M \left( m^f, V_H + V_L - m^f \right),
\]

where \( M \) is the reduced form matching function that relates the level of job matches to the number of workers \( l \) and vacancies \( v \), and \( m^f = (l, V_H + V_L) \) is the number of initially matched workers. Conditional on the number of vacancies (and their implied labor market parameters), the job assignment, offer, and secondary market decisions will follow the characterization in Proposition 1. So, the firm’s expected profits from a vacancy filled with a new worker is

\[
E[\pi_f | V_H, V_L] = (1 - \delta) \left\{ Q_f \alpha \left( \frac{f_2 (\theta_H) - w_h^f}{\text{profits from promoted}} \right) + (1 - Q_f) \left( \frac{E[V f_1 (\theta_H) | \alpha] - w_v^f}{\text{profits from unpromoted}} \right) \right\},
\]

where \( V_H, V_L \) are the total high and low learning firm vacancies in the market, respectively, and all other objects match their definition from Proposition 1. The firm only profits upon successfully retaining an initially assigned worker. Any possibility that a vacancy is filled in the secondary market is irrelevant since the secondary market is competitive.
assumptions, I can rewrite the maximization problem as

$$
\max_v h (v_H + v_L) E [\pi (v_H, v_L)] v - c(v),
$$

noting that the market level of vacancies imposes two negative externalities for the firm. First, excess vacancies increase the match rate on the secondary market, which drives up wage competition for incumbent workers. Second, excess vacancies lower the initial fill rate for new workers. There is also an offsetting force, where the share of firms that are high-learning determine the degree of adverse selection on the secondary market. Expected profits are clearly decreasing in the total number of vacancies due to the first two mechanisms, so it suffices to ensure that the net effect of adding high learning employer vacancies does not induce unraveling (e.g., the adverse selection effect is not so strong as to push the slope of the best response curve for high learning vacancies above 1).

To be precise about this condition, notice that clearly 

$$
\frac{\partial E [\pi (v_H, v_L)]}{\partial v_H} \leq 0.
$$

Since the expected profits for each filled vacancy is the weighted average of the profits from a worker of known high ability and the profits from the average worker (and neither \( \alpha \) or the firm-level \( Q \) depends on the market characteristics), it suffices to consider whether

$$
\frac{\partial \pi_1}{\partial v_H} \frac{\partial \pi_2}{\partial v_H} \leq 0 \iff \frac{\partial w_1}{\partial v_H} \frac{\partial w_2}{\partial v_H} \geq 0.
$$

Secondary market profits are zero in any equilibrium, so the conditions that ensure firm profits are sufficiently well behaved are also exactly the conditions that ensure offered wages are increasing. Now,

$$
\begin{align*}
\frac{\partial w_1}{\partial v_H} &= \frac{\partial g}{\partial v_H} E_{\alpha'} [f_1 (\theta)] + g \frac{\partial E [f_1 (\theta) | \alpha']}{\partial v_H}, \\
\frac{\partial w_2}{\partial v_H} &= \frac{\partial g}{\partial v_H} [\kappa f_2 (\theta_H) + (1 - \kappa) E [f_1 (\theta) | \alpha']] + g (1 - \kappa) \frac{\partial E [f_1 (\theta) | \alpha']}{\partial v_H}.
\end{align*}
$$

Observe that the wages of promoted workers will be more insulated from adverse selection in secondary market than the wages of unknown workers since their expected outside option includes the possibility of obtaining their true product, so a sufficient condition for both derivatives to be positive is for \( \frac{\partial w_1}{\partial v_H} \). A simple rearrangement of the derivative then yields the assumed condition in the proposition:

$$
-\frac{\partial E [f_1 (\theta) | \alpha']}{\partial v_H}/E [f_1 (\theta) | \alpha'] \leq \frac{\partial g}{\partial v_H}/g.
$$

Conditional on the equilibrium existing, it’s straightforward to show that increasing the productivity term \( \psi \) increases the best response to any market-level vacancy, so the equilibrium number of vacancies will increase as well.

Similarly, the assumptions on secondary market matching are sufficient to ensure that the probability of receiving a secondary market offer, \( g \), is increasing in the number of initial vacancies. So clearly, workers’ likelihood of re-employment is higher in more productive regions. Meanwhile, incumbent wages increasing with high learning employer vacancies is exactly the sufficient condition

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that guarantees \( \partial E[\pi(v_H,v_L)] / \partial v_H \leq 0 \), so it follows that the same conditions that ensure the existence of the vacancy creation problem also ensures that occupational wages at the incumbent employers are weakly increasing as well.

C Additional Empirical Details

C.1 Data Construction

C.1.1 Annual worker panel

My primary data on worker earnings, job characteristics, and employer characteristics come from the universe of formal employment contracts in the RAIS data. Each observation in the raw data is a single employment contract within a state and year, so my first step is to construct an annual panel of workers’ employment histories. Each observation in the annual panel is a worker’s primary employment contract for that year, and the resulting dataset serves as the basis for all sub-samples and derived measures in my project.

To construct the unique worker-by-year panel of primary employment, I consider all employment contracts that covered at least six months over the year, entailed at least 20 contracted hours of work per week, and paid non-zero earnings. In the cases when there are multiple recorded employment contracts for the same worker and year that satisfy these selection criteria, I choose the employment contract covering the longest duration (in months), and I break any subsequent ties by selecting the contract with the highest average monthly earnings.

My preferred earnings measure is the average nominal monthly earnings over the employment contract. Where defined, this measure is highly correlated with the December monthly earnings measure that has been used in the literature (the correlation coefficient between these measures in logs is above .97), but average monthly earnings the additional advantage of being defined for partial employment spells in a year that ended before December.

I classify any years when a worker is not in the annual panel as years when the worker is out of the formal labor market. Correspondingly, I consider the worker to not be working as a supervisor in those years. I impute worker characteristics in years when the worker is not in the annual panel by using the last known observation (for gender, education, state, race, and birth year). Meanwhile, I impute a worker’s counterfactual earnings by annually compounding the worker’s last known earnings by the average wage growth for the worker’s last known state-by-baseline-occupation-group. Finally, I assign a reason for separation to the out-of-formal-labor-market spell using the reason for separation field of the most recent employment contract. Employer-initiated separations are employer terminations with or without just cause (excluding contract expirations). Worker-initiated separations are voluntary worker separations. I combine separations for any other known reason (including contract expirations) into a single category.

C.1.2 Classifying promotions

I use the CBO-02 occupation codes recorded in the RAIS for each employment contract from 2003 onwards to define promotions. The occupation codes follow a consistent hierarchical structure, so I can define supervisory jobs from the structure of the occupation codes themselves. As a check, I can also define supervisor jobs from the text of the job titles (by finding all job titles that contain
the term *supervisores*). The results from these two classification methods are identical, which is reassuring about the consistency of the occupation classification system.

The CBO-02 system classifies all occupations into a 6-digit occupational code. The first two digits of the occupation code indicate the main occupation group, which are generally broad classes of jobs like metalworkers, textile workers, or public services workers. Within production-level occupational groups, a third digit of “0” in the occupation code is reserved for the supervisors in the occupational group, whereas all other values refer to other sub-groups within the occupation that do not necessarily have a clear vertical interpretation relative to each other. Individual occupations are further differentiated by the three additional digits following these three base digits.

Within production-level occupation groups (CBO-02 codes starting with 41-99), all but four occupational groups contain supervisor occupations. On the other hand, none of the civil, managerial, professional, or technical-level occupational groups (CBO-02 codes starting with 01-39) contain supervisor occupations. So, occupational groups with observable lines of progression can be considered to be a proper (but nearly complete) subset of the production worker-level (*trabalhadores*) occupation groups.

### C.1.3 Estimating promotion propensity

As discussed in Section 4.1, I classify firms as high or low promotion firms based on their composition-adjusted promotion rates between 2004 and 2006. Specifically, for each of the three years $t$, I consider all workers from the annual panel between the ages of 25 and 50 who were in formal employment at a non-public sector firm in years $t - 1$ and $t$. I further restrict the sample to all workers who remained in the same broad occupation group in both years, which bolsters the interpretation that these promotions reflect vertical job changes. I estimate $\eta_{jt}$ on the sample using Equation 5 as the residual promotion rate for firm $j$ at time $t$ after adjusting for worker characteristics and differences in promotion rates in different occupation groups. Finally, to minimize measurement error or the contribution of year-specific shocks, I restrict the set of firms to those that had at least 10 workers in the estimation sample for each of the three years, and I define $\eta_j = E[\eta_{jt}]$ as the firm’s average promotion residual over those three years.

It’s worth noting two additional details implicit in the baseline approach. I do not restrict the sample to workers who are at the same firm in both years, so some promotions in the data are external promotions where a worker was working as a line worker in a firm in year $t - 1$ and as a supervisor in a different firm in year $t$. Furthermore, in the case of these external promotions, I attribute the promotion to the firm where the worker received the promotion (i.e., the firm in year $t$), which is consistent with my interpretation and model. However, although the inclusion of external promotions slightly increases power, these two details are inconsequential for my results. Table A.1 compares the correlation in firms’ promotion rates across a variety of alternate classification methods. The measures are highly correlated with each other. As an additional check, Figure A.18 compares the treatment effect estimates when I classify firms based on internal promotion rates only – the effects on promotions and turnover are slightly attenuated but otherwise similar.

### C.1.4 Measuring mass layoffs

I follow the literature on using linked employer-employee data to identify mass-layoff events. I first compile a firm-level panel of employment counts by aggregating the worker-level annual panel to
the firm-year level, and I identify large employment drops or firm closures using the criteria from Schmieder et al. (2020). Mass-layoff events are when a firm with at least 50 employees experience at least a 30 percent drop in employment or disappear from the data altogether in the following year. Firm identifiers are not always longitudinally consistent, so reorganizations or spinoffs may be mistakenly classified as layoff events. I follow the literature to exclude these alternate scenarios by dropping any layoff event where at least 20% of displaced workers go to the same firm in the following year.

C.1.5 Constructing the local hiring IV

I construct a panel of total employment and new hiring at the firm-by-municipality level by aggregating the worker-level annual panel. Since employment contracts specify both the firm and location of the employment establishment, the mapping from workers to the firm-municipality is clear. New hires are defined as the total number of workers who are working in the firm-municipality and were working at a different firm in the year prior. So, this measure excludes within firm transfers across municipalities, as well as any brief employment spells that would not be classified as the worker’s primary employment for the year. To ensure that the hiring shares are informative, I restrict my attention to municipalities that have at least 1000 workers and at least 200 new hires each year.

For a worker $i$ in mover cohort $c$ and municipality $m$, I calculate their jack-knife local hiring share instrument as

$$z_{mc} = \frac{G^H_{mc} - \sum J(i') = J(i) H^{i'}}{G^H_{mc} + G^L_{mc} - \sum J(i') = J(i) 1},$$

where $G^H_{mc}, G^L_{mc}$ are the total new hires by high and low promotion firms, respectively, and $i'$ are other movers in the same cohort. Since workers in my analysis sample are included in the new hire totals, I avoid the reflection problem that would arise from this functional dependence by excluding all new hires from worker $i$’s destination firm from the numerator and denominator. As a result, the interpretation of $z_{mc}$ is the local hiring share by high promotion firms excluding the worker’s destination firm. Technically, $z_{mc}$ varies by destination firm due to the jack-knife procedure. However, this variation is minor, so I slightly abuse notation to focus on the main source of variation.

C.2 Calculating Average Treatment Effects

I combine workers from multiple cohorts to increase the precision of my estimates and to ensure that I am capturing an average treatment effect that is representative across cohorts. However, researchers have cautioned that pooling treatment effects in designs with staggered treatment timing may yield unintuitive and potentially negative weighting of the underlying treatment effects.

To address these concerns and make the relevant comparisons clear, I allow all coefficients in the estimation equation to vary arbitrarily with the worker’s cohort. This clearly emphasizes that all identification of treatment effects over time come solely from comparisons between workers who are in the same cohort (e.g., I only compare workers who moved to a high promotion firm in 2009 to workers who moved to a low promotion firm in 2009). Furthermore, I can combine estimated treatment effects across cohorts using explicitly specified weights to estimate an average treatment effect across all mover cohorts.

I define my estimand of interest as the average effect across all cohorts. Correspondingly, the
combined estimate of the cohort specific treatment effect $\beta_{c\tau}$ at event time $\tau$ is

$$\beta_{\tau} = \left[ \sum_{c=2008}^{2012} \beta_{c\tau} \right]/5.$$ 

In the data, the number of workers in each cohort varies slightly, so an alternative is to weigh each cohort’s treatment effect by the number of workers in the cohort. However, using uniform weighting across cohort years is more straightforward, and ensures that any differences in estimates across subgroups are not driven by any differences in the composition of workers across cohorts.

In practice, the difference between all of the possible approaches is small. Estimating Equation 6 by allowing only controls to vary by cohort and pooling the treatment effect coefficients yield similar estimates. This is due to two reasons. First, cohort-specific treatment effects are already reasonably similar. In addition, the share of workers moving to high versus low promotion firms each year is also stable, so the OLS weights are roughly comparable to the uniform weights.

C.3 Structural Quantification

C.3.1 Estimation method

The model yields nonlinear expressions for the means and treatment effects of high learning firms on promotions and turnover. I match these expressions to their empirical analogs using classical minimum distance, which requires numerically optimizing the nonlinear objective function in Equation 12. The objective function is straightforward to compute given that the model expressions are in closed form, yet numerical optimization can run the risk of hitting local rather than the global minima of the objective function.

I use the following algorithm to calculate my model parameters. First, I draw a starting guess for the parameters $\theta = (\bar{Q}_H, \bar{Q}_L, \alpha, g)$ randomly from a uniform distribution. I then numerically minimize the objective function using the Nelder Mead algorithm from the R package nloptr with a stopping criterion for the relative change of $10^{-12}$ and a constraint that each parameter lies on the interior between 0 and 1. I repeat the process 100 times, drawing a new random starting value each time, and I select the solution with the smallest objective across all the starting value draws.

The nonlinear model performs reasonably well in my setting. Across the 100 different starting values, the numerical algorithm reaches an objective below $10^{-5}$ in 68 cases. The maximum standard deviation for any parameter estimate across these 68 cases is approximately $10^{-13}$ and the mean objective is approximately $10^{-22}$.

C.3.2 Sensitivity of parameter estimates to moments ($\Lambda$)

Although the estimation of the parameters requires optimizing a nonlinear function, the choice of the minimum distance estimator ensures that all identification for the model parameters ultimately comes from the four empirical moments (conditional on the calibrated parameters). To help increase the transparency of the model estimates, I report the sensitivity of the model parameters to the matched moments, as defined by Andrews et al. (2017), in Table A.5.

Formally, the sensitivity measure in the classical minimum distance estimator is

$$\Lambda = (G'WG)^{-1} G'W,$$
where $W$ is the chosen weighting matrix and $G$ is the Jacobian of the model equations $h(\theta)$ from Equation 12. The interpretation is that for a local perturbation of the empirical moments that converges to $\eta$, the first-order asymptotic bias in the estimated parameters is

$$E[\tilde{\theta}] = \Lambda \eta.$$

For more details, see Proposition 2 of Andrews et al. (2017). As expected, the estimated parameters are most sensitive to the treatment effect estimates of high promotion firms, particularly their effects on promotions.