Lecture 8. Institutional Change and Democratization

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Introduction

- Differences between political regimes in terms of distribution of resources and economic performance.
- What determines the equilibrium political regime?
- Why do some societies undergo institutional change?
- More concretely: why did many Western countries become democratic during the 19th century?
- Why did many Latin American countries become democratic but failed to consolidate democracy throughout the 20th century?
Patterns of Political Development

- Britain in the 19th century; democratization and democratic consolidation
- Argentina in the 20th century; democracy-coup cycles
- Singapore; persistent nondemocracy with limited repression
- South Africa until the end of Apartheid; persistent nondemocracy with repression
- What accounts for this diversity?
Unsatisfactory Answers

- One set of answers to these questions are related to “enlightenment”.
  - Societies become enlightened and wiser, and that's when they become democratic
  - This view does not seem to receive widespread support from the data (democracy arises in the midst of intense conflict, not generally a consensual move)
  - It does not explain why democratization took place in some places during sometimes, and why it succeeded in some instances and not in others.

- Another set of answers about “equilibrium institutions” related to behind the veil arguments
  - Compare “expected utility” under different regimes
  - Not a useful perspective (people are *not* behind a veil of ignorance)
  - Does not explain why democratization happens during some episodes
This Lecture

- A baseline framework for analysis of institutional change and emergence of democracy.
- Also use this framework analyze whether democracy will consolidate once it emerges.
- Comparative statics about likelihood of democracy versus persistence of nondemocratic regime (possibly under repression).
Let us start with a simple model of nondemocratic politics.

This model will provide many of the insights that will be crucial in understanding why democratic regimes emerge.

Key idea:

- political power in the hands of an elite
- but “citizens” excluded from formal, *de jure* power still have a say in politics because of their *de facto* power to undertake collective action, unrest, revolution...
- → (no) revolution constraint
Preferences

- Suppose that there are two classes, the elite (the rich) with fixed income $y^r$ and the poor citizens with income $y^p < y^r$.
- Total population is normalized to 1, a fraction $1 - \delta > 1/2$ of the agents are poor, with income $y^p$, and the remaining fraction $\delta$ are rich with income $y^r$.
- Mean income is denoted by $\bar{y}$.
- Let $\theta$ be the share of total income accruing to the rich:

\[
y^p = \frac{(1 - \theta)\bar{y}}{1 - \delta} \quad \text{and} \quad y^r = \frac{\theta\bar{y}}{\delta}.
\]

(1)

- Also assume

\[
\frac{(1 - \theta)\bar{y}}{1 - \delta} < \frac{\theta\bar{y}}{\delta} \quad \text{or} \quad \theta > \delta,
\]

to ensure that $y^p < \bar{y} < y^r$. 

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Taxation

- Only fiscal instruments, linear tax $\tau \geq 0$ and lump-sum transfer $T$.
- Taxation is distortionary, with cost of taxation $C(\tau)\bar{y}$ as a function of the tax rate is $\tau$, where $C$ is increasing and strictly convex.
- Then the government budget constraint is therefore

$$T = \tau ((1 - \delta)y^p + \delta y^r) - C(\tau)\bar{y} = (\tau - C(\tau))\bar{y}. \quad (2)$$

- The most preferred tax rate of poor agents is given by

$$\left(\frac{\theta - \delta}{1 - \delta}\right) = C'(\tau^p). \quad (3)$$

- In contrast, the rich elite’s political bliss point is $\tau^r = 0$. 
Preferences

- Individual utility is defined over the discounted sum of post-tax incomes with discount factor $\beta \in (0, 1)$, so for individual $i$ at time $t = 0$, it is

\[
U^i = \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \hat{y}_t^i,
\]

where $\hat{y}_t^i$ denotes after-tax income.

- We are in a non-democratic environment, so policy is determined by rich agents.

- The only influence of poor agents is through their de facto power, the threat of revolution.

- The rich will choose policy subject to a revolution constraint.

- Along the equilibrium path where revolution does not take place:

\[
U^i = \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left( (1 - \tau_t) y^i + (\tau_t - C(\tau_t)) \bar{y} \right).
\]
Revolution

- If a revolution is attempted, it always succeeds but a fraction $\mu_t$ of the productive capacity of the economy is destroyed forever in the process.
- After a revolution, citizens receive all output.
- Therefore, if there is a revolution at time $t$, each citizen receives a per period return of
  \[
  \frac{(1 - \mu^S)\bar{y}}{(1 - \delta)}.
  \]
- In all future periods: total income in the economy is $(1 - \mu^S)\bar{y}$ and is shared between $1 - \delta$ agents.
- $\mu^S$ is the value of $\mu_t$ at the date when the revolution took place.
- Suppose that $\mu_t$ is equal to $\mu^H = \mu$ with probability $q$ and to $\mu^L = 1$ with probability $1 - q$. 
Revolution and Collective Action

- Fluctuations in $\mu$ due to ability to solve the collective action problem among the citizens.
- It will be the source of *commitment problems*.
- A change in $\mu$ corresponds to a change in the underlying environment, so the elite, who hold political power in nondemocracy, will optimize again.
- As a result, their promise to redistribute today may not materialize due to changes in circumstances tomorrow.
Timing of Events

At each $t$, the timing of events is as follows:

- $\mu_t$ is revealed.
- The elite set the tax rate $\tau^N_t$.
- The citizens decide whether or not to initiate a revolution, denoted by $\rho_t$ with $\rho_t = 1$ corresponding to a revolution at time $t$. If there is a revolution, they obtain the remaining $1 - \mu_t$ share of output in all future periods.
Equilibrium Concept

- Let us start with the pure strategy Markov Perfect Equilibria of this game
- Strategies only depend on the current state of the world.
- For the elite the strategy is the tax rate:
  \[ \tau^N : \{\mu^L, \mu^H\} \rightarrow [0, 1]. \]
- For the citizens, it is the revolution decision
  \[ \rho : \{\mu^L, \mu^H\} \times [0, 1] \rightarrow \{0, 1\}. \]
Payoffs after Revolution

- Define $V^p(R, \mu^S)$ as the return to citizens if there is a revolution starting in threat state $\mu^S \in \{\mu, 1\}$. Then,
  
  $$V^p(R, \mu^S) = \frac{(1 - \mu^S)\bar{y}}{(1 - \delta) (1 - \beta)}.$$  

- Equal sharing of gains from revolution to avoid the free rider problem.
- For the rich elite:
  
  $$V^r(R, \mu^S) = 0.$$  

- Since $\mu^L = 1$, the citizens will never attempt a revolution when $\mu_t = \mu^L$.
- Thus, the only relevant value is the one starting in the state $\mu^H = \mu$:

  $$V^p(R, \mu^H) = \frac{(1 - \mu)\bar{y}}{(1 - \delta) (1 - \beta)}. \quad (6)$$
Payoffs in Nondemocracy

- Now consider nondemocracy in the state $\mu_t = \mu^L$, where there is no threat of revolution.
- Denote the relevant values by $V^r(N, \mu^L)$ and $V^p(N, \mu^L)$.
- Since there is no threat of revolution in this state, the MPE tax choice for the elite is
  \[ \tau^N = \tau^r = 0. \]
- Therefore,
  \begin{align*}
  V^r(N, \mu^L) &= y^r + \beta \left[ qV^r(N, \mu^H) + (1 - q)V^r(N, \mu^L) \right] \quad (7) \\
  V^p(N, \mu^L) &= y^p + \beta \left[ qV^p(N, \mu^H) + (1 - q)V^p(N, \mu^L) \right].
  \end{align*}
Values in Nondemocracy (continued)

- What about in state $\mu_t = \mu^H$?
- First, suppose that in this state the elite also set $\tau_N = \tau^r$.
- Then, there is never any redistribution, and the values are

\[
V^r(N) = \frac{y^r}{1 - \beta},
\]

\[
V^p(N) = \frac{y^p}{1 - \beta}
\]  

regardless of the state.
The Revolution Constraint

- The *revolution constraint* binds if the poor citizens prefer a revolution in the state $\mu_t = \mu^H$ rather than to live in nondemocracy without any redistribution, i.e., if

$$V^p(R, \mu^H) > V^p(N)$$

where $V^p(R, \mu^H)$ is given by (6).

- Using the definitions in (1), the revolution constraint is equivalent to

$$\theta > \mu.$$  \hspace{1cm} (9)

- In other words, inequality needs to be sufficiently high, i.e., $\theta$ sufficiently high, for the revolution constraint to bind.

- If inequality is not that high, so that we have $\theta \leq \mu$, there is no threat of revolution even in the state $\mu_t = \mu^H$, even with no redistribution ever.

- In this case, the elite will always set their unconstrained best tax rate, $\tau^N = \tau^r$, and we have no revolution along the equilibrium path.
When the Revolution Constraints Binds

- Suppose that the revolution constraint (9) binds.
- If in this case, the elite set $\tau^N = \tau^r$ in the threat state $\mu_t = \mu^H$, there will be a revolution.
- So the elite need to make some concessions by setting a tax rate $\tau^N = \hat{\tau} > 0$.
- Let us denote the values to the elite and the citizens in the state $\mu_t = \mu^H$ when the elite set a tax rate $\hat{\tau}$ and are expected to do so in the future, and there is no revolution, by $V^r(N, \mu^H, \tau^N = \hat{\tau})$ and $V^p(N, \mu^H, \tau^N = \hat{\tau})$.
- At this tax rate, we have that an agent of type $i$ has net income of $(1 - \hat{\tau}) y^i$, plus he receives a lump sum transfer of $\hat{T}$.
- From the government budget constraint, this lump-sum transfer is $\hat{T} = (\hat{\tau} - C(\hat{\tau})) \bar{y}$, where $\hat{\tau} \bar{y}$ is total tax revenue, and $C(\hat{\tau}) \bar{y}$ is the cost of taxation.
In this case, the value functions are given by

$$V^r(N, \mu^H, \tau^N = \hat{\tau}) =$$

$$y^r + (\hat{\tau}(\bar{y} - y^r) - C(\hat{\tau})\bar{y})$$

$$+ \beta \left[ qV^r(N, \mu^H, \tau^N = \hat{\tau}) + (1 - q)V^r(N, \mu^L) \right],$$

and

$$V^p(N, \mu^H, \tau^N = \hat{\tau}) =$$

$$y^p + (\hat{\tau}(\bar{y} - y^p) - C(\hat{\tau})\bar{y})$$

$$+ \beta \left[ qV^p(N, \mu^H, \tau^N = \hat{\tau}) + (1 - q)V^p(N, \mu^L) \right].$$

Intuition.
The best response of the citizens is

\[
\rho \begin{cases} 
0 & \text{if } V^p(R, \mu^H) \leq V^p(N, \mu^H, \tau^N = \hat{\tau}) \\
1 & \text{if } V^p(R, \mu^H) > V^p(N, \mu^H, \tau^N = \hat{\tau})
\end{cases}
\]  

(11)

We can also write:

\[
V^r(N, \mu^H) = \rho V^r(R, \mu^H) + (1 - \rho) V^r(N, \mu^H, \tau^N = \hat{\tau})
\]

(12)

\[
V^p(N, \mu^H) = \max_{\rho \in \{0,1\}} \rho V^p(R, \mu^H) + (1 - \rho) V^p(N, \mu^H, \tau^N = \hat{\tau})
\]
Preventing Revolution

- The elite would like to prevent revolution if they can.
- Will they be able to do so?
- To determine the answer to this question, we need to see what is the maximum value that the elite can promise to the citizens.
- Clearly this will be when they set the tax most preferred by the citizens, $\tau^p$, given by (3).
- Hence the relevant comparison is between $V^p(R, \mu^H)$ and $V^p(N, \mu^H, \tau^N = \tau^p)$.
- If $V^p(N, \mu^H, \tau^N = \tau^p) \geq V^p(R, \mu^H)$, then a revolution can be averted, but not otherwise.
Preventing Revolution (continued)

- Solving above equations

\[ V^p(N, \mu^H, \tau^N = \tau^p) = \frac{y^p + (1 - \beta(1 - q)) (\tau^p(\bar{y} - y^p) - C(\tau^p)\bar{y})}{1 - \beta}. \]

(13)

- \( V^p(N, \mu^H, \tau^N = \tau^p) \) crucially depends on \( q \), the probability that the state will be \( \mu^H \) in the future, since this is the extent to which redistribution will recur in the future (in some sense, how much future redistribution the rich can credibly promise).

- The revolution can be averted if \( V^p(N, \mu^H, \tau^N = \tau^p) \geq V^p(R, \mu^H) \), or if

\[ \frac{y^p + (1 - \beta(1 - q)) (\tau^p(\bar{y} - y^p) - C(\tau^p)\bar{y})}{1 - \beta} \geq \frac{(1 - \mu)\bar{y}}{(1 - \delta)(1 - \beta)}, \]

which can be simplified to

\[ \mu \geq \theta - (1 - \beta(1 - q)) (\tau^p(\theta - \delta) - (1 - \delta)C(\tau^p)) \cdot \]

(14)
Preventing Revolution (continued)

- If the above condition does not hold, even the maximum credible transfer to a citizen is not enough, and there will be a revolution along the equilibrium path.
- We can now use (14) to define a critical value of \( \mu^H \), again denoted \( \mu^* \) such that \( V^p(N, \mu^*, \tau^N = \tau^p) = V^p(R, \mu^*) \), or
  \[
  \mu^* = \theta - (1 - \beta(1 - q)) (\tau^p(\theta - \delta) - (1 - \delta) C(\tau^p)).
  \]

  where \( \mu^* < \theta \).
- When \( \mu \geq \mu^* \), \( V^p(N, \mu^H, \tau^N = \tau^p) \geq V^p(R, \mu^H) \), and the revolution is averted.
- When \( \mu < \mu^* \), \( V^p(N, \mu^H, \tau^N = \tau^p) < V^p(R, \mu^H) \), future transfers are expected to be sufficiently rare that even at the best possible tax rate for the citizens, there isn’t enough redistribution in the future, and the citizens prefer a revolution rather than to live under nondemocracy with political power in the hands of the elite.
Using (6) and (13), we have that $\hat{\tau}$ is given by:

$$\mu = \theta - (1 - \beta(1 - q)) (\hat{\tau}(\theta - \delta) - (1 - \delta)C(\hat{\tau})) .$$ \hspace{1cm} (16)

This analysis than leads to:

**Proposition:** There in a unique MPE $\{\tilde{\sigma}^r, \tilde{\sigma}^p\}$ of the game $G^\infty(\beta)$. Let $\mu^*$ and $\hat{\tau}$ be given by (15) and (16). Then in this equilibrium:

- If $\theta \leq \mu$, the elite never redistribute and the citizens never undertake a revolution.
- If $\theta > \mu$, then we have that:
  - If $\mu < \mu^*$, promises by the elite are insufficiently credible to avoid a revolution. In the low state, the elite do not redistribute and there is no revolution, but in the high state a revolution occurs whatever tax rate the elite set.
  - If $\mu \geq \mu^*$, the elite do not redistribute in the low state and set the tax rate $\hat{\tau}$ in the high threat state, just sufficient to stop a revolution. The citizens never revolt.
For discussion, suppose that $\theta > \mu$.

Then, starting with the elite in power, if $\mu < \mu^*$, they set a zero tax rate when $\mu_t = \mu^L$, but when the state transits to $\mu^H$, there is a revolution.

The problem here is that although the elite would like to stay in power by offering the citizens redistribution, they cannot offer today enough to make the present value of nondemocracy to the citizens as great as the present value of revolution.
Comparative Statics

- The threshold $\mu^*$ depends on $\theta$ and on $q$.
- $\mu^*$ is increasing in $\theta$, so that inequality makes revolution more likely (because the revolution constraint is “more binding”)
- $\mu^*$ is decreasing in $q$, because lower $q$ means “less credible commitments to future distribution”—because revolution constraints are rare events.
Incentive Compatible Promises

- MPE limit commitment power.
- What happens if we look at subgame perfect equilibria?
- Issue: “promises” by the elite must be *incentive compatible*, in the sense that when the revolution threats disappears, they should have no incentive to deviate.
- Suppose $\theta > \mu$ and $\mu < \mu^*$, so with the restriction to MPE, the unique equilibrium involves a revolution.
- Compute the maximum value that the elite can promise to the citizens to see whether this will prevent revolution.
Analysis

- First calculate the value to the elite if they redistribute at the rate $\tau^N = \tau^H \leq \tau^p$ in the state $\mu_t = \mu^H$ and at the rate $\tau^N = \tau^L \leq \tau^p$ in the state $\mu_t = \mu^L$.

- Since we are no longer looking at Markovian strategies, $\tau^L > 0$ is now possible.
Analysis (continued)

These values are

\( V^r(N, \mu^L, [\tau^L, \tau^H]) = \)

\[ y^r + \left( \tau^L (\bar{y} - y^r) - C(\tau^L) \bar{y} \right) \]

\[ + \beta \left[ qV^r(N, \mu^H, [\tau^L, \tau^H]) + (1 - q)V^r(N, \mu^L, [\tau^L, \tau^H]) \right] \]

\( V^r(N, \mu^H, [\tau^L, \tau^H]) = \)

\[ y^r + \left( \tau^H (\bar{y} - y^r) - C(\tau^H) \bar{y} \right) \]

\[ + \beta \left[ qV^r(N, \mu^H, [\tau^L, \tau^H]) + (1 - q)V^r(N, \mu^L, [\tau^L, \tau^H]) \right] \]
Analysis (continued)

- Combining the previous two expressions,

\[
V^r(\mathbf{N}, \mu^L, [\tau^L, \tau^H]) = \frac{y^r + (1 - \beta q) (\tau^L (\bar{y} - y^r) - C (\tau^L) \bar{y})}{1 - \beta} + \frac{\beta q (\tau^H (\bar{y} - y^r) - C(\tau^H) \bar{y})}{1 - \beta}
\]

as the value that the elite will receive if they stick to their “promised” behavior summarized by the tax vector \([\tau^L, \tau^H]\).

- The key is whether this behavior is “incentive compatible” for them, that is, whether they will wish to deviate from it now or in the future.
Deviation

- What happens if they deviate?
- Clearly, they will deviate when $\mu_t = \mu^L$
- Worst punishment: revolution the first time $\mu_t = \mu^H$.
- Thus, the deviation payoff for the elite is

$$V^r_d(N, \mu^L) = y^r + \beta \left[ qV^r(R, \mu^H) + (1 - q) V^r_d(N, \mu^L) \right],$$

- Since $V^r(R, \mu^H) = 0$,

$$V^r_d(N, \mu^L) = \frac{y^r}{1 - \beta (1 - q)}. \quad (19)$$
Incentive Compatibility

- The incentive competent at the constraint for the elite is
  \[ V^r(N, \mu^L, [\tau^L, \tau^H]) \geq V^r_d(N, \mu^L). \]  
  \hspace{1cm} (20)

- The subgame perfect equilibrium that is best for the elite, starting in the state \( \mu^L \) can be characterized as the solution to
  \[ \max_{\tau^L, \tau^H} V^r(N, \mu^L, [\tau^L, \tau^H]) \]  
  \hspace{1cm} (21)

subject to (20) and

\[ V^p(N, \mu^H, [\tau^L, \tau^H]) \geq V^p(R, \mu^H), \]  
\hspace{1cm} (22)

where \( V^p(N, \mu^H, [\tau^L, \tau^H]) \) is the value to the citizens starting in the state \( \mu^H \) from the tax vector \([\tau^L, \tau^H]\).

- If the constraints set is empty, then in the subgame perfect equilibrium, there will again be revolution.
- Otherwise, revolution can be averted.
Compute the values to the citizens as

\[ V^p(N, \mu^H, \left[ \tau^L, \tau^H \right]) = \]
\[ \frac{y^p + \beta (1 - q) \left( \tau^L (\bar{y} - y^p) - C(\tau^L) \bar{y} \right)}{1 - \beta} \]
\[ + \frac{(1 - \beta (1 - q)) \left( \tau^H (\bar{y} - y^p) - C(\tau^H) \bar{y} \right)}{1 - \beta} \]
Clearly, there will exist and minimum value of $\mu^H$ such that a revolution can be averted, say $\mu^{**}$.

This will be given by $\tau^H = \tau^p$ and $\tau^L$ the maximum value consistent with the incentive compatibility constraint of the elite, (20), as equality—say $\bar{\tau}'$.

Solving the incentive compatibility constraint, this is given by

$$\bar{\tau}' (\theta - \delta) + \delta C(\bar{\tau}') = \frac{\beta q}{(1 - \beta q)} \left[ \frac{\theta}{1 - \beta (1 - q)} - (\tau^p (\theta - \delta) + \delta C(\tau^p)) \right].$$  

(24)

Important point: $\bar{\tau}'$ can be significantly less than $\tau^p$ because the commitment problem is still present.
Incentive Compatibility (continued)

- Then, the threshold is

\[
\mu^{**} = \theta - \beta (1 - q) (\bar{\tau}' (\theta - \delta) - (1 - \delta) C (\bar{\tau}')) - (1 - \beta (1 - q)) (\tau^p (\theta - \delta) - (1 - \delta) C (\tau^p))
\]

where \(\bar{\tau}'\) is given by (24).

- As long as \(\bar{\tau}' > 0\),

\[
\mu^{**} < \mu^*.
\]

- Therefore:

**Proposition:** When we allow non-Markovian strategies, a revolution can be averted for all \(\mu \geq \mu^{**}\). Here \(\mu^{**} < \mu^*\), which means that greater redistribution is now possible, but \(\mu^{**} > 0\), which means that there are limits how much credible redistribution the elite can promise.
In addition, with SPE, taxes in the high state are not necessarily equal to $\tau^p$, because there is *tax smoothing*.

Because $C(\cdot)$ is convex, it is better to have taxes in the two states closer to each other.

Full tax smoothing is generally not always incentive compatible, however.
In the model presented so far, the only instrument that the elite have to prevent revolutions is fiscal redistribution within the existing system.

Alternative: changes in institutions.
Democratization: General Insights

- Why does this make sense?
- Revolution arises because the citizens have *de facto power* today, but have no power in the future.
- Therefore, they are willing to use an inefficient action, revolution, in order to obtain more in the future.
- De facto power is, by its nature, not always persistent.
- But *de jure power*, arising from formal institutions, more persistent.
- If there is a way of transforming the transit tree de facto power of the citizens into more durable de jure power, this might prevent revolution.
- Thus, democratization (more generally institutional change) as a commitment device.
Model

- Take the same model as before, augmented with two more actions by the elite:
  1. **Democratization:** at the beginning of each date, they can change the constitution, and from then on the society is democratic (and this is for now irreversible), and taxes are decided by majoritarian elections. Since citizens are in the majority, majoritarian elections will lead to their most preferred tax rate, $\tau^P$, in the future.
  2. **Repression:** the elite can also use repression in order to prevent revolution. Repression costly because it destroys a fraction of output at that time.

- **Question:** when will they use fiscal redistribution, when will they prefer repression and when will they go for democratization.
Intuition

- Democratization is costly: all power is allocated to citizens, and they can set their most preferred tax rate $\tau^p$.
- Fiscal redistribution within the existing system is cheaper, if it is credible.
- Therefore, democratization will only arise when fiscal redistribution within the existing system is not credible.
- Also, democratization needs to be preferred to repression, so repression needs to be sufficiently costly and democracy need not be too redistributive.
Sketch

- Income now is

\[ \hat{y}^i = \omega (1 - \kappa) y^i + (1 - \omega) \left( (1 - \tau) y^i + (\tau - C(\tau)) \bar{y} \right), \]  

(26)

- \( \kappa \) is the cost due to repression, with \( \omega = 0 \) denoting no repression and \( \omega = 1 \) denoting repression. We model the cost of repression as we did the costs of revolution.
Timing of Events

- The state $\mu_t \in \{\mu^L, \mu^H\}$ is revealed.
- The elite decide whether or not to use repression, $\omega \in \{0, 1\}$. If $\omega = 1$, the poor cannot undertake a revolution and the stage game ends.
- If $\omega = 0$, the elite decide whether or not to democratize, $\phi \in \{0, 1\}$. If they decide not to democratize, they set the tax rate $\tau^N$.
- The citizens decide whether or not to initiate a revolution, $\rho \in \{0, 1\}$. If $\rho = 1$ they share the remaining income forever. If $\rho = 0$ and $\phi = 1$ the tax rate $\tau^D$ is set by the median voter (a poor citizen). If $\rho = 0$ and $\phi = 0$, then the tax rate is $\tau^N$. 
Markov Perfect Equilibria

- Analysis identical to before.
- Democracy is an absorbing state and citizens are in the majority, thus

\[ V^p(D) = \frac{y^p + \tau^p (\bar{y} - y^p) - C(\tau^p)\bar{y}}{1 - \beta} \]

and

\[ V^r(D) = \frac{y^r + \tau^p (\bar{y} - y^r) - C(\tau^p)\bar{y}}{1 - \beta} . \]
Markov Perfect Equilibria (continued)

- We need to ensure that democracy prevented revolution, that is,

\[ V^p(D) \geq V^p(R, \mu^H). \]

- This is equivalent to

\[ \mu \geq \theta - (\tau^p(\theta - \delta) - (1 - \delta)C(\tau^p)). \] (28)

- The revolution constraint identical to before.

- Thus the same credibility issues.

- Then, revolution can be prevented by redistribution if \( \mu > \mu^* \in (0, 1) \)

where

\[ V^p(N, \mu^*, \tau^N = \tau^p) = V^p(R, \mu^*). \] (29)
Markov Perfect Equilibria (continued)

- Also, returns from using repression all the time:

\[
V^r(O, \mu^H | \kappa) = \frac{y^r - (1 - \beta(1 - q))\kappa y^r}{1 - \beta} \quad \text{and} \quad (30)
\]

\[
V^p(O, \mu^H | \kappa) = \frac{y^p - (1 - \beta(1 - q))\kappa y^p}{1 - \beta}.
\]

- When is it beneficial for the lead to use repression versus redistribute or concede democratization?
- The answer will depend on whether \( \kappa \) is greater than the thresholds

\[
\kappa^* = \frac{1}{\theta} (\delta C(\hat{\tau}) - \hat{\tau} (\delta - \theta)). \quad (31)
\]

\[
\bar{\kappa} = \frac{1}{\theta(1 - \beta(1 - q))} (\delta C(\tau^p) - \tau^p (\delta - \theta)). \quad (32)
\]
**Markov Perfect Equilibria (continued)**

**Proposition:** There is a unique MPE $\{\tilde{\sigma}^r, \tilde{\sigma}^p\}$ in the game $G^\infty(\beta)$, and it is such that:

- If $\theta \leq \mu$, then the revolution constraint does not bind and the elite can stay in power without repressing, redistributing or democratizing.
- If $\theta > \mu$, then the revolution constraint binds. In addition, let be $\mu^*$ defined by (29), and $\kappa^*$ and $\bar{\kappa}$ be defined by (31) and (32). Then:
  - If $\mu \geq \mu^*$ and $\kappa \geq \kappa^*$, repression is relatively costly and the elite redistribute income in state $\mu^H$ to avoid revolution.
  - If $\mu < \mu^*$ and $\kappa < \bar{\kappa}$, or $\kappa \geq \bar{\kappa}$ and (28) does not hold, or if $\mu \geq \mu^*$ and $\kappa < \kappa^*$, the elite use repression in state $\mu^H$.
  - If $\mu < \mu^*$, (28) holds, and $\kappa \geq \bar{\kappa}$, concessions are insufficient to avoid a revolution and repression is relatively costly. In this case, in state $\mu^H$ the elite democratize.
Discussion

- Democracy arises only if $\mu < \mu^*$, repression is relatively costly, i.e., $\kappa \geq \bar{\kappa}$ and if (28) holds.
- This critical threshold for the cost of repression, $\bar{\kappa}$, is increasing in inequality (increasing in $\theta$), that is,
  
  $$\frac{d\bar{\kappa}}{d\theta} > 0.$$  

- Intuitively, when inequality is higher, democracy is more redistributive, i.e., $\tau^p$ is higher, and hence more costly to the rich elite. They are therefore more willing to use repression.
- Democracy therefore emerges as an equilibrium outcome only in societies with intermediate levels of inequality.
  - Too high inequality makes democracy too costly for the elite, too low inequality makes nondemocracy sufficiently attractive for the citizens that the revolution threat does not materialize.
As above, the same insights hold with subgame perfect equilibria, but now fiscal redistribution within the existing regime can prevent democratization for a larger set of parameter values.
Discussion

**Key ideas:**
- Conflict and threat of revolution
- Commitment
- From de facto to de jure power

Are these reasonable?
Conflict

- Most instances of democratization amidst conflict and threat of revolution
- Though exceptions exist, most instances of democratization in 19th century Europe and 20th century Latin America in the midst of social unrest
  - democratization “partly taken” not just “given”
Commitment

- Commitment issues central to political economy as usual.
- Commitment to future redistribution in an existing system not truly difficult to maintain.
De Jure Power?

- Why is transition to democracy credible?
- Two aspects to this question:
  - what does a constitution or a formal institution mean?
  - why is the transition to democracy not reversed?
- To be discussed in the next lectures...
One More Question: De Facto Power of the Elite

- Why is the de jure power of the citizens in democracy sufficient?
- May or may not be
- To be discussed in the next lectures...