

Table 1:  $\tilde{R}_f^2 = .1$

| $n$ | $K$ | $\text{Cov}(\varepsilon, v_2)$ | (a)   | (b)   | (c)    | (d)    | (e)    | (f)   | (g)   | (h)   | (i)   | (j)    | (k)    | (l)      | (m)   | (n)   |
|-----|-----|--------------------------------|-------|-------|--------|--------|--------|-------|-------|-------|-------|--------|--------|----------|-------|-------|
| 100 | 5   | -0.9                           | 0.086 | 0.050 | -0.223 | -0.041 | -0.178 | 0.235 | 0.166 | 0.074 | 0.045 | 0.027  | 0.081  | 0.096    | 0.154 | 0.104 |
| 100 | 5   | -0.5                           | 0.084 | 0.054 | -0.123 | 0.312  | -0.398 | 0.116 | 0.056 | 0.073 | 0.048 | 0.106  | 0.058  | 0.206    | 0.096 | 0.045 |
| 100 | 5   | 0.5                            | 0.079 | 0.053 | 0.125  | -0.303 | 0.396  | 0.114 | 0.058 | 0.072 | 0.050 | -0.399 | -0.220 | 0.021    | 0.096 | 0.048 |
| 100 | 5   | 0.9                            | 0.078 | 0.045 | 0.219  | 0.027  | 0.502  | 0.233 | 0.161 | 0.067 | 0.041 | 0.080  | -0.061 | -0.158   | 0.153 | 0.100 |
| 100 | 10  | -0.9                           | 0.108 | 0.078 | -0.405 | -0.158 | -0.258 | 0.369 | 0.275 | 0.067 | 0.049 | -0.046 | 0.140  | -0.094   | 0.172 | 0.116 |
| 100 | 10  | -0.5                           | 0.079 | 0.049 | -0.228 | 0.417  | -0.630 | 0.117 | 0.059 | 0.070 | 0.045 | 0.168  | 0.520  | 0.074    | 0.082 | 0.040 |
| 100 | 10  | 0.5                            | 0.078 | 0.043 | 0.223  | -0.430 | 0.637  | 0.124 | 0.064 | 0.066 | 0.042 | 0.184  | 1.217  | -0.039   | 0.085 | 0.043 |
| 100 | 10  | 0.9                            | 0.099 | 0.070 | 0.405  | 0.163  | 0.248  | 0.360 | 0.266 | 0.064 | 0.043 | -0.097 | -0.175 | -0.107   | 0.164 | 0.115 |
| 100 | 30  | -0.9                           | 0.137 | 0.112 | -0.656 | -0.384 | -0.277 | 0.548 | 0.382 | 0.111 | 0.095 | -0.361 | 0.135  | 0.544    | 0.180 | 0.113 |
| 100 | 30  | -0.5                           | 0.110 | 0.081 | -0.361 | 0.662  | -1.035 | 0.098 | 0.036 | 0.083 | 0.061 | 0.870  | 0.116  | -216.133 | 0.053 | 0.017 |
| 100 | 30  | 0.5                            | 0.103 | 0.071 | 0.365  | -1.241 | 1.691  | 0.101 | 0.039 | 0.076 | 0.058 | 0.038  | 0.133  | -0.902   | 0.056 | 0.020 |
| 100 | 30  | 0.9                            | 0.142 | 0.115 | 0.655  | 0.380  | 0.280  | 0.539 | 0.383 | 0.113 | 0.094 | -1.737 | -0.232 | -0.344   | 0.176 | 0.107 |
| 250 | 5   | -0.9                           | 0.108 | 0.074 | -0.095 | -0.014 | -0.065 | 0.169 | 0.108 | 0.090 | 0.057 | 0.011  | 0.028  | 0.043    | 0.130 | 0.075 |
| 250 | 5   | -0.5                           | 0.112 | 0.077 | -0.055 | 0.094  | -0.118 | 0.107 | 0.056 | 0.094 | 0.065 | 0.004  | 0.041  | 0.021    | 0.097 | 0.050 |
| 250 | 5   | 0.5                            | 0.117 | 0.081 | 0.052  | -0.098 | 0.117  | 0.115 | 0.061 | 0.098 | 0.068 | -0.007 | -0.046 | -0.027   | 0.103 | 0.055 |
| 250 | 5   | 0.9                            | 0.105 | 0.071 | 0.094  | 0.016  | 0.064  | 0.162 | 0.100 | 0.085 | 0.057 | -0.011 | -0.025 | -0.038   | 0.120 | 0.072 |
| 250 | 10  | -0.9                           | 0.084 | 0.039 | -0.212 | -0.074 | -0.132 | 0.249 | 0.172 | 0.068 | 0.039 | 0.040  | 0.027  | 0.037    | 0.132 | 0.079 |
| 250 | 10  | -0.5                           | 0.079 | 0.045 | -0.112 | 0.177  | -0.269 | 0.118 | 0.062 | 0.076 | 0.049 | 0.019  | 0.052  | 0.036    | 0.092 | 0.045 |
| 250 | 10  | 0.5                            | 0.079 | 0.046 | 0.118  | -0.177 | 0.275  | 0.121 | 0.063 | 0.075 | 0.052 | -0.021 | -0.051 | -0.040   | 0.090 | 0.048 |
| 250 | 10  | 0.9                            | 0.081 | 0.037 | 0.209  | 0.067  | 0.137  | 0.250 | 0.173 | 0.063 | 0.035 | -0.043 | -0.038 | -0.048   | 0.127 | 0.070 |
| 250 | 30  | -0.9                           | 0.101 | 0.069 | -0.460 | -0.223 | -0.239 | 0.570 | 0.463 | 0.065 | 0.030 | -0.163 | 0.156  | 0.056    | 0.130 | 0.087 |
| 250 | 30  | -0.5                           | 0.090 | 0.051 | -0.256 | 0.389  | -0.640 | 0.145 | 0.068 | 0.063 | 0.032 | 0.067  | 0.095  | 0.040    | 0.080 | 0.038 |
| 250 | 30  | 0.5                            | 0.087 | 0.048 | 0.255  | -0.385 | 0.637  | 0.137 | 0.070 | 0.066 | 0.037 | -0.249 | -0.054 | 0.014    | 0.080 | 0.039 |
| 250 | 30  | 0.9                            | 0.103 | 0.069 | 0.460  | 0.224  | 0.238  | 0.565 | 0.464 | 0.062 | 0.030 | -0.207 | -0.050 | -0.052   | 0.141 | 0.084 |

- (a), (b): Actual sizes of the new test based on 2SLS with nominal sizes = 10%, and 5%  
(c), (d), (e): Mean biases of forward and reverse 2SLS, and mean of  $\hat{b}$   
(f), (g): Actual sizes of the tests based on  $nR^2$  of the residual of forward 2SLS with nominal sizes = 10%, and 5%  
(h), (i): Actual size of the new test based on Nagar with nominal size = 10%, and 5%  
(j), (k), (l): Mean biases of forward Nagar, reverse Nagar, and LIML  
(m), (n): Actual sizes of the tests based on  $nR^2$  of the residual of forward Nagar with nominal sizes = 10%, and 5%

**The reported numbers are based on 5000 Monte Carlo replications.**

Table 1 (Cont.):  $\tilde{R}_f^2 = .1$

| n      | K  | Cov( $\varepsilon, v_2$ ) | (a)   | (b)   | (c)    | (d)    | (e)    | (f)   | (g)   | (h)   | (i)   | (j)    | (k)    | (l)    | (m)   | (n)   |
|--------|----|---------------------------|-------|-------|--------|--------|--------|-------|-------|-------|-------|--------|--------|--------|-------|-------|
| 1,000  | 5  | -0.9                      | 0.131 | 0.095 | -0.026 | -0.006 | -0.015 | 0.118 | 0.061 | 0.102 | 0.068 | -0.002 | 0.003  | 0.007  | 0.108 | 0.055 |
| 1,000  | 5  | -0.5                      | 0.131 | 0.096 | -0.016 | 0.020  | -0.027 | 0.106 | 0.057 | 0.105 | 0.078 | -0.002 | 0.007  | 0.002  | 0.102 | 0.054 |
| 1,000  | 5  | 0.5                       | 0.137 | 0.099 | 0.016  | -0.021 | 0.027  | 0.107 | 0.053 | 0.108 | 0.073 | 0.002  | -0.007 | -0.002 | 0.104 | 0.050 |
| 1,000  | 5  | 0.9                       | 0.126 | 0.094 | 0.026  | 0.006  | 0.015  | 0.115 | 0.067 | 0.100 | 0.074 | 0.002  | -0.003 | -0.007 | 0.105 | 0.059 |
| 1,000  | 10 | -0.9                      | 0.097 | 0.064 | -0.062 | -0.020 | -0.038 | 0.138 | 0.083 | 0.085 | 0.058 | 0.001  | 0.005  | 0.008  | 0.106 | 0.062 |
| 1,000  | 10 | -0.5                      | 0.106 | 0.071 | -0.035 | 0.043  | -0.071 | 0.118 | 0.063 | 0.097 | 0.066 | -0.001 | 0.008  | 0.004  | 0.105 | 0.056 |
| 1,000  | 10 | 0.5                       | 0.103 | 0.070 | 0.035  | -0.043 | 0.071  | 0.113 | 0.062 | 0.093 | 0.064 | 0.000  | -0.008 | -0.004 | 0.101 | 0.054 |
| 1,000  | 10 | 0.9                       | 0.106 | 0.065 | 0.063  | 0.021  | 0.038  | 0.154 | 0.089 | 0.093 | 0.059 | 0.001  | -0.004 | -0.007 | 0.117 | 0.062 |
| 1,000  | 30 | -0.9                      | 0.094 | 0.046 | -0.183 | -0.073 | -0.108 | 0.306 | 0.214 | 0.089 | 0.042 | 0.004  | 0.007  | 0.010  | 0.117 | 0.066 |
| 1,000  | 30 | -0.5                      | 0.097 | 0.052 | -0.102 | 0.124  | -0.219 | 0.145 | 0.074 | 0.090 | 0.052 | 0.003  | 0.012  | 0.007  | 0.098 | 0.052 |
| 1,000  | 30 | 0.5                       | 0.097 | 0.049 | 0.101  | -0.124 | 0.219  | 0.145 | 0.078 | 0.094 | 0.051 | -0.003 | -0.012 | -0.007 | 0.101 | 0.051 |
| 1,000  | 30 | 0.9                       | 0.098 | 0.048 | 0.183  | 0.073  | 0.108  | 0.309 | 0.215 | 0.091 | 0.047 | -0.004 | -0.006 | -0.009 | 0.116 | 0.062 |
| 10,000 | 5  | -0.9                      | 0.135 | 0.096 | -0.002 | 0.000  | -0.002 | 0.099 | 0.053 | 0.102 | 0.075 | 0.000  | 0.001  | 0.001  | 0.098 | 0.052 |
| 10,000 | 5  | -0.5                      | 0.124 | 0.093 | -0.001 | 0.003  | -0.003 | 0.095 | 0.047 | 0.098 | 0.068 | 0.001  | 0.001  | 0.001  | 0.094 | 0.047 |
| 10,000 | 5  | 0.5                       | 0.134 | 0.100 | 0.001  | -0.003 | 0.003  | 0.102 | 0.049 | 0.106 | 0.076 | 0.000  | -0.001 | -0.001 | 0.102 | 0.049 |
| 10,000 | 5  | 0.9                       | 0.125 | 0.092 | 0.002  | 0.000  | 0.002  | 0.095 | 0.045 | 0.097 | 0.066 | -0.001 | -0.001 | -0.001 | 0.094 | 0.045 |
| 10,000 | 10 | -0.9                      | 0.101 | 0.065 | -0.007 | -0.003 | -0.004 | 0.102 | 0.051 | 0.088 | 0.056 | -0.001 | 0.000  | 0.000  | 0.096 | 0.048 |
| 10,000 | 10 | -0.5                      | 0.115 | 0.075 | -0.003 | 0.005  | -0.007 | 0.108 | 0.053 | 0.100 | 0.064 | 0.000  | 0.001  | 0.001  | 0.107 | 0.052 |
| 10,000 | 10 | 0.5                       | 0.103 | 0.067 | 0.004  | -0.004 | 0.007  | 0.098 | 0.050 | 0.089 | 0.058 | 0.001  | 0.000  | 0.000  | 0.097 | 0.049 |
| 10,000 | 10 | 0.9                       | 0.111 | 0.073 | 0.006  | 0.002  | 0.004  | 0.109 | 0.056 | 0.097 | 0.064 | 0.000  | -0.001 | -0.001 | 0.107 | 0.053 |
| 10,000 | 30 | -0.9                      | 0.103 | 0.055 | -0.022 | -0.008 | -0.014 | 0.122 | 0.066 | 0.100 | 0.051 | 0.000  | 0.000  | 0.001  | 0.102 | 0.052 |
| 10,000 | 30 | -0.5                      | 0.096 | 0.057 | -0.012 | 0.013  | -0.025 | 0.097 | 0.054 | 0.092 | 0.055 | 0.000  | 0.001  | 0.000  | 0.094 | 0.051 |
| 10,000 | 30 | 0.5                       | 0.099 | 0.054 | 0.013  | -0.013 | 0.025  | 0.109 | 0.053 | 0.096 | 0.053 | 0.000  | -0.001 | 0.000  | 0.102 | 0.050 |
| 10,000 | 30 | 0.9                       | 0.099 | 0.054 | 0.022  | 0.008  | 0.014  | 0.118 | 0.062 | 0.094 | 0.051 | 0.000  | -0.001 | -0.001 | 0.097 | 0.050 |

- (a), (b): Actual sizes of the new test based on 2SLS with nominal sizes = 10%, and 5%  
(c), (d), (e): Mean biases of forward and reverse 2SLS, and mean of  $\hat{b}$   
(f), (g): Actual sizes of the tests based on  $nR^2$  of the residual of forward 2SLS with nominal sizes = 10%, and 5%  
(h), (i): Actual size of the new test based on Nagar with nominal size = 10%, and 5%  
(j), (k), (l): Mean biases of forward Nagar, reverse Nagar, and LIML  
(m), (n): Actual sizes of the tests based on  $nR^2$  of the residual of forward Nagar with nominal sizes = 10%, and 5%

**The reported numbers are based on 5000 Monte Carlo replications.**

Table 2:  $\tilde{R}_f^2 = .01$

| n   | K  | Cov( $\epsilon, v_2$ ) | (a)   | (b)   | (c)    | (d)    | (e)    | (f)   | (g)   | (h)   | (i)   | (j)     | (k)     | (l)    | (m)   | (n)   |
|-----|----|------------------------|-------|-------|--------|--------|--------|-------|-------|-------|-------|---------|---------|--------|-------|-------|
| 100 | 5  | -0.9                   | 0.082 | 0.061 | -0.745 | -0.062 | -1.748 | 0.213 | 0.134 | 0.119 | 0.108 | 4.579   | -0.179  | -0.551 | 0.151 | 0.092 |
| 100 | 5  | -0.5                   | 0.067 | 0.052 | -0.407 | -5.226 | 3.170  | 0.080 | 0.040 | 0.106 | 0.084 | -0.504  | 0.785   | 1.807  | 0.057 | 0.026 |
| 100 | 5  | 0.5                    | 0.068 | 0.051 | 0.410  | -0.157 | -1.143 | 0.079 | 0.034 | 0.110 | 0.086 | 1.073   | -0.286  | 1.127  | 0.054 | 0.023 |
| 100 | 5  | 0.9                    | 0.087 | 0.066 | 0.739  | 0.253  | 1.207  | 0.211 | 0.131 | 0.123 | 0.110 | 1.780   | 0.569   | 1.211  | 0.148 | 0.089 |
| 100 | 10 | -0.9                   | 0.089 | 0.070 | -0.819 | -0.526 | -0.358 | 0.208 | 0.122 | 0.117 | 0.107 | -0.681  | -0.555  | 1.445  | 0.129 | 0.071 |
| 100 | 10 | -0.5                   | 0.085 | 0.062 | -0.457 | 5.292  | -7.591 | 0.077 | 0.035 | 0.112 | 0.089 | -0.380  | -1.332  | -0.769 | 0.050 | 0.022 |
| 100 | 10 | 0.5                    | 0.092 | 0.069 | 0.455  | -1.742 | 0.131  | 0.086 | 0.038 | 0.107 | 0.088 | 0.337   | -0.414  | 0.435  | 0.049 | 0.018 |
| 100 | 10 | 0.9                    | 0.087 | 0.066 | 0.816  | 0.525  | 0.353  | 0.213 | 0.123 | 0.116 | 0.104 | 1.094   | 0.618   | 0.994  | 0.125 | 0.064 |
| 100 | 30 | -0.9                   | 0.110 | 0.089 | -0.871 | -0.637 | -0.245 | 0.122 | 0.046 | 0.125 | 0.112 | -1.848  | -8.336  | -9.463 | 0.060 | 0.023 |
| 100 | 30 | -0.5                   | 0.130 | 0.102 | -0.480 | 1.124  | -1.652 | 0.065 | 0.021 | 0.128 | 0.102 | -1.012  | 3.453   | 0.667  | 0.026 | 0.009 |
| 100 | 30 | 0.5                    | 0.119 | 0.094 | 0.485  | -1.094 | 1.682  | 0.065 | 0.023 | 0.129 | 0.101 | 23.277  | -12.186 | 0.799  | 0.035 | 0.008 |
| 100 | 30 | 0.9                    | 0.107 | 0.086 | 0.869  | 0.633  | 0.247  | 0.126 | 0.052 | 0.130 | 0.116 | 0.935   | 0.059   | 3.031  | 0.060 | 0.022 |
| 250 | 5  | -0.9                   | 0.093 | 0.066 | -0.581 | 0.720  | -6.404 | 0.341 | 0.251 | 0.111 | 0.096 | -0.476  | -0.936  | 0.163  | 0.231 | 0.165 |
| 250 | 5  | -0.5                   | 0.068 | 0.049 | -0.328 | 0.971  | -1.427 | 0.091 | 0.046 | 0.084 | 0.062 | -0.323  | -2.610  | 0.065  | 0.067 | 0.034 |
| 250 | 5  | 0.5                    | 0.057 | 0.042 | 0.327  | -0.261 | 0.053  | 0.096 | 0.044 | 0.085 | 0.066 | 0.366   | 0.593   | 0.191  | 0.069 | 0.032 |
| 250 | 5  | 0.9                    | 0.086 | 0.066 | 0.572  | 0.205  | 0.466  | 0.326 | 0.240 | 0.115 | 0.102 | -13.996 | -0.119  | 0.233  | 0.225 | 0.156 |
| 250 | 10 | -0.9                   | 0.112 | 0.086 | -0.709 | -0.401 | -0.371 | 0.377 | 0.264 | 0.137 | 0.124 | -0.504  | 0.169   | -0.468 | 0.214 | 0.143 |
| 250 | 10 | -0.5                   | 0.088 | 0.066 | -0.389 | 2.396  | -3.260 | 0.091 | 0.044 | 0.096 | 0.073 | 0.187   | 0.319   | -0.282 | 0.057 | 0.027 |
| 250 | 10 | 0.5                    | 0.090 | 0.065 | 0.396  | -2.142 | 3.312  | 0.095 | 0.049 | 0.106 | 0.083 | 0.431   | 0.141   | 2.101  | 0.058 | 0.030 |
| 250 | 10 | 0.9                    | 0.116 | 0.095 | 0.716  | 0.401  | 0.379  | 0.372 | 0.267 | 0.144 | 0.131 | 0.129   | 0.220   | 0.784  | 0.210 | 0.139 |
| 250 | 30 | -0.9                   | 0.109 | 0.091 | -0.830 | -0.576 | -0.266 | 0.333 | 0.207 | 0.145 | 0.130 | -0.866  | 0.005   | 72.662 | 0.167 | 0.094 |
| 250 | 30 | -0.5                   | 0.123 | 0.094 | -0.462 | 1.169  | -1.729 | 0.089 | 0.037 | 0.116 | 0.095 | 1.454   | 2.040   | -1.142 | 0.041 | 0.014 |
| 250 | 30 | 0.5                    | 0.115 | 0.088 | 0.461  | -1.126 | 1.661  | 0.080 | 0.036 | 0.105 | 0.082 | -2.396  | -0.128  | 0.354  | 0.043 | 0.017 |
| 250 | 30 | 0.9                    | 0.113 | 0.096 | 0.830  | 0.577  | 0.264  | 0.322 | 0.208 | 0.146 | 0.134 | 0.806   | 1.358   | 1.300  | 0.159 | 0.094 |

- (a), (b): Actual sizes of the new test based on 2SLS with nominal sizes = 10%, and 5%  
(c), (d), (e): Mean biases of forward and reverse 2SLS, and mean of  $\hat{b}$   
(f), (g): Actual sizes of the tests based on  $nR^2$  of the residual of forward 2SLS with nominal sizes = 10%, and 5%  
(h), (i): Actual size of the new test based on Nagar with nominal size = 10%, and 5%  
(j), (k), (l): Mean biases of forward Nagar, reverse Nagar, and LIML  
(m), (n): Actual sizes of the tests based on  $nR^2$  of the residual of forward Nagar with nominal sizes = 10%, and 5%

**The reported numbers are based on 5000 Monte Carlo replications.**

Table 2 (Cont.):  $\tilde{R}_f^2 = .01$

| n      | K  | Cov( $\varepsilon, v_2$ ) | (a)   | (b)   | (c)    | (d)    | (e)    | (f)   | (g)   | (h)   | (i)   | (j)    | (k)    | (l)    | (m)   | (n)   |
|--------|----|---------------------------|-------|-------|--------|--------|--------|-------|-------|-------|-------|--------|--------|--------|-------|-------|
| 1,000  | 5  | -0.9                      | 0.075 | 0.043 | -0.242 | -0.043 | -0.209 | 0.248 | 0.177 | 0.064 | 0.040 | -0.096 | 0.064  | 0.115  | 0.156 | 0.104 |
| 1,000  | 5  | -0.5                      | 0.084 | 0.054 | -0.141 | 0.301  | -0.403 | 0.112 | 0.059 | 0.074 | 0.053 | 0.298  | 0.157  | -0.409 | 0.095 | 0.047 |
| 1,000  | 5  | 0.5                       | 0.087 | 0.055 | 0.139  | -0.287 | 0.380  | 0.120 | 0.062 | 0.079 | 0.052 | 0.635  | -0.150 | -0.006 | 0.100 | 0.053 |
| 1,000  | 5  | 0.9                       | 0.087 | 0.050 | 0.240  | 0.045  | 0.205  | 0.244 | 0.177 | 0.069 | 0.044 | -0.067 | -0.198 | -0.347 | 0.154 | 0.103 |
| 1,000  | 10 | -0.9                      | 0.116 | 0.079 | -0.424 | -0.174 | -0.267 | 0.388 | 0.304 | 0.073 | 0.052 | 0.266  | 0.222  | 0.309  | 0.165 | 0.120 |
| 1,000  | 10 | -0.5                      | 0.084 | 0.053 | -0.237 | 0.514  | -0.764 | 0.129 | 0.069 | 0.067 | 0.046 | -0.103 | -0.324 | 0.213  | 0.091 | 0.046 |
| 1,000  | 10 | 0.5                       | 0.083 | 0.053 | 0.235  | -0.384 | 0.584  | 0.127 | 0.075 | 0.069 | 0.046 | 6.848  | -0.151 | -0.180 | 0.094 | 0.051 |
| 1,000  | 10 | 0.9                       | 0.107 | 0.072 | 0.426  | 0.176  | 0.267  | 0.395 | 0.311 | 0.072 | 0.049 | 0.789  | -0.068 | -0.261 | 0.181 | 0.128 |
| 1,000  | 30 | -0.9                      | 0.155 | 0.134 | -0.671 | -0.396 | -0.285 | 0.678 | 0.575 | 0.116 | 0.096 | -0.519 | 0.003  | -2.470 | 0.203 | 0.153 |
| 1,000  | 30 | -0.5                      | 0.109 | 0.077 | -0.372 | 0.702  | -1.090 | 0.138 | 0.074 | 0.071 | 0.053 | -0.135 | -3.483 | 0.766  | 0.069 | 0.035 |
| 1,000  | 30 | 0.5                       | 0.114 | 0.078 | 0.372  | -0.724 | 1.119  | 0.136 | 0.072 | 0.069 | 0.049 | -0.098 | -0.254 | -1.195 | 0.077 | 0.039 |
| 1,000  | 30 | 0.9                       | 0.159 | 0.135 | 0.670  | 0.394  | 0.287  | 0.678 | 0.579 | 0.122 | 0.100 | 0.213  | -0.055 | -0.121 | 0.212 | 0.159 |
| 10,000 | 5  | -0.9                      | 0.127 | 0.089 | -0.026 | -0.004 | -0.017 | 0.118 | 0.066 | 0.097 | 0.070 | 0.001  | 0.007  | 0.010  | 0.103 | 0.058 |
| 10,000 | 5  | -0.5                      | 0.119 | 0.088 | -0.013 | 0.027  | -0.030 | 0.096 | 0.048 | 0.096 | 0.066 | 0.002  | 0.012  | 0.007  | 0.093 | 0.046 |
| 10,000 | 5  | 0.5                       | 0.128 | 0.096 | 0.013  | -0.027 | 0.030  | 0.104 | 0.053 | 0.105 | 0.074 | -0.002 | -0.012 | -0.007 | 0.101 | 0.050 |
| 10,000 | 5  | 0.9                       | 0.119 | 0.085 | 0.024  | 0.002  | 0.017  | 0.111 | 0.057 | 0.092 | 0.062 | -0.003 | -0.008 | -0.011 | 0.099 | 0.050 |
| 10,000 | 10 | -0.9                      | 0.095 | 0.056 | -0.069 | -0.023 | -0.042 | 0.146 | 0.084 | 0.082 | 0.052 | 0.000  | 0.004  | 0.007  | 0.107 | 0.056 |
| 10,000 | 10 | -0.5                      | 0.108 | 0.069 | -0.037 | 0.049  | -0.077 | 0.114 | 0.061 | 0.095 | 0.064 | 0.002  | 0.011  | 0.006  | 0.105 | 0.054 |
| 10,000 | 10 | 0.5                       | 0.096 | 0.065 | 0.039  | -0.047 | 0.078  | 0.107 | 0.058 | 0.084 | 0.059 | 0.001  | -0.009 | -0.004 | 0.096 | 0.050 |
| 10,000 | 10 | 0.9                       | 0.103 | 0.061 | 0.067  | 0.021  | 0.042  | 0.153 | 0.090 | 0.088 | 0.056 | -0.002 | -0.006 | -0.010 | 0.112 | 0.062 |
| 10,000 | 30 | -0.9                      | 0.096 | 0.045 | -0.199 | -0.081 | -0.116 | 0.337 | 0.239 | 0.092 | 0.044 | 0.004  | 0.006  | 0.009  | 0.119 | 0.066 |
| 10,000 | 30 | -0.5                      | 0.096 | 0.052 | -0.110 | 0.132  | -0.237 | 0.136 | 0.076 | 0.087 | 0.052 | 0.002  | 0.010  | 0.005  | 0.092 | 0.053 |
| 10,000 | 30 | 0.5                       | 0.097 | 0.049 | 0.111  | -0.133 | 0.238  | 0.147 | 0.081 | 0.093 | 0.052 | -0.002 | -0.011 | -0.006 | 0.101 | 0.052 |
| 10,000 | 30 | 0.9                       | 0.095 | 0.049 | 0.197  | 0.080  | 0.116  | 0.320 | 0.228 | 0.088 | 0.048 | -0.006 | -0.007 | -0.010 | 0.114 | 0.063 |

- (a), (b): Actual sizes of the new test based on 2SLS with nominal sizes = 10%, and 5%  
(c), (d), (e): Mean biases of forward and reverse 2SLS, and mean of  $\hat{b}$   
(f), (g): Actual sizes of the tests based on  $nR^2$  of the residual of forward 2SLS with nominal sizes = 10%, and 5%  
(h), (i): Actual size of the new test based on Nagar with nominal size = 10%, and 5%  
(j), (k), (l): Mean biases of forward Nagar, reverse Nagar, and LIML  
(m), (n): Actual sizes of the tests based on  $nR^2$  of the residual of forward Nagar with nominal sizes = 10%, and 5%

**The reported numbers are based on 5000 Monte Carlo replications.**

Table 3:  $\tilde{R}_f^2 = .001$

| n   | K  | Cov( $\epsilon, v_2$ ) | (a)   | (b)   | (c)    | (d)    | (e)    | (f)   | (g)   | (h)   | (i)   | (j)    | (k)      | (l)     | (m)   | (n)   |
|-----|----|------------------------|-------|-------|--------|--------|--------|-------|-------|-------|-------|--------|----------|---------|-------|-------|
| 100 | 5  | -0.9                   | 0.079 | 0.062 | -0.884 | -0.359 | -2.085 | 0.079 | 0.039 | 0.112 | 0.100 | -3.437 | -0.720   | -2.111  | 0.062 | 0.029 |
| 100 | 5  | -0.5                   | 0.077 | 0.061 | -0.484 | -0.528 | 4.529  | 0.067 | 0.033 | 0.117 | 0.092 | -0.757 | 1.651    | -5.630  | 0.049 | 0.021 |
| 100 | 5  | 0.5                    | 0.075 | 0.057 | 0.489  | -0.579 | 2.218  | 0.063 | 0.027 | 0.113 | 0.089 | 0.851  | 1.464    | 6.667   | 0.045 | 0.019 |
| 100 | 5  | 0.9                    | 0.084 | 0.068 | 0.877  | 0.603  | 0.249  | 0.085 | 0.041 | 0.113 | 0.102 | 1.262  | -168.415 | 0.834   | 0.060 | 0.029 |
| 100 | 10 | -0.9                   | 0.097 | 0.077 | -0.892 | -0.640 | -0.302 | 0.080 | 0.037 | 0.120 | 0.107 | -1.314 | -1.118   | -1.157  | 0.046 | 0.020 |
| 100 | 10 | -0.5                   | 0.091 | 0.070 | -0.497 | 3.495  | -4.726 | 0.068 | 0.031 | 0.119 | 0.096 | 0.108  | 1.644    | -0.008  | 0.046 | 0.019 |
| 100 | 10 | 0.5                    | 0.097 | 0.076 | 0.498  | -3.618 | 4.631  | 0.072 | 0.034 | 0.113 | 0.090 | 0.115  | -3.987   | -1.273  | 0.042 | 0.018 |
| 100 | 10 | 0.9                    | 0.090 | 0.070 | 0.892  | 0.635  | 0.313  | 0.089 | 0.041 | 0.112 | 0.098 | 0.859  | 0.796    | 0.046   | 0.053 | 0.024 |
| 100 | 30 | -0.9                   | 0.127 | 0.103 | -0.897 | -0.677 | -0.232 | 0.060 | 0.021 | 0.128 | 0.114 | -0.269 | -1.310   | -0.918  | 0.031 | 0.008 |
| 100 | 30 | -0.5                   | 0.128 | 0.102 | -0.495 | 1.667  | -2.498 | 0.062 | 0.020 | 0.127 | 0.104 | 1.516  | -0.945   | 0.209   | 0.027 | 0.009 |
| 100 | 30 | 0.5                    | 0.116 | 0.089 | 0.499  | -1.556 | 2.241  | 0.063 | 0.022 | 0.125 | 0.103 | 0.047  | 0.023    | -1.076  | 0.031 | 0.007 |
| 100 | 30 | 0.9                    | 0.121 | 0.098 | 0.895  | 0.672  | 0.234  | 0.067 | 0.025 | 0.131 | 0.111 | 1.589  | 2.212    | 0.968   | 0.035 | 0.012 |
| 250 | 5  | -0.9                   | 0.073 | 0.057 | -0.860 | -1.063 | 11.367 | 0.114 | 0.061 | 0.106 | 0.095 | -1.207 | -0.756   | -58.292 | 0.081 | 0.040 |
| 250 | 5  | -0.5                   | 0.065 | 0.051 | -0.488 | -0.056 | -0.417 | 0.065 | 0.032 | 0.106 | 0.083 | 0.203  | -1.664   | -0.927  | 0.046 | 0.022 |
| 250 | 5  | 0.5                    | 0.074 | 0.060 | 0.488  | -5.079 | 4.522  | 0.068 | 0.030 | 0.107 | 0.084 | 41.542 | 0.060    | 0.173   | 0.049 | 0.022 |
| 250 | 5  | 0.9                    | 0.077 | 0.057 | 0.856  | 0.499  | 0.456  | 0.114 | 0.061 | 0.107 | 0.096 | 3.040  | -0.011   | -7.534  | 0.085 | 0.045 |
| 250 | 10 | -0.9                   | 0.092 | 0.074 | -0.875 | -0.614 | -0.323 | 0.106 | 0.054 | 0.111 | 0.097 | -1.061 | 5.569    | -0.720  | 0.066 | 0.034 |
| 250 | 10 | -0.5                   | 0.099 | 0.078 | -0.482 | 1.951  | -2.368 | 0.071 | 0.032 | 0.123 | 0.098 | -0.106 | 0.715    | -0.206  | 0.044 | 0.018 |
| 250 | 10 | 0.5                    | 0.096 | 0.076 | 0.485  | -2.446 | 2.977  | 0.075 | 0.035 | 0.119 | 0.094 | 1.033  | -0.877   | 20.133  | 0.044 | 0.018 |
| 250 | 10 | 0.9                    | 0.102 | 0.079 | 0.878  | 0.621  | 0.307  | 0.105 | 0.049 | 0.114 | 0.105 | 0.252  | 0.051    | 0.802   | 0.068 | 0.032 |
| 250 | 30 | -0.9                   | 0.121 | 0.092 | -0.893 | -0.667 | -0.236 | 0.092 | 0.044 | 0.135 | 0.116 | -0.743 | 0.028    | -4.268  | 0.044 | 0.019 |
| 250 | 30 | -0.5                   | 0.125 | 0.099 | -0.497 | 1.132  | -1.607 | 0.075 | 0.030 | 0.121 | 0.098 | 1.404  | -1.071   | -1.118  | 0.037 | 0.012 |
| 250 | 30 | 0.5                    | 0.118 | 0.092 | 0.496  | -1.201 | 1.756  | 0.066 | 0.030 | 0.114 | 0.089 | -2.415 | 0.123    | 0.287   | 0.037 | 0.015 |
| 250 | 30 | 0.9                    | 0.124 | 0.102 | 0.893  | 0.668  | 0.234  | 0.093 | 0.043 | 0.128 | 0.113 | 1.225  | 1.253    | -2.604  | 0.047 | 0.022 |

- (a), (b): Actual sizes of the new test based on 2SLS with nominal sizes = 10%, and 5%  
(c), (d), (e): Mean biases of forward and reverse 2SLS, and mean of  $\hat{b}$   
(f), (g): Actual sizes of the tests based on  $nR^2$  of the residual of forward 2SLS with nominal sizes = 10%, and 5%  
(h), (i): Actual size of the new test based on Nagar with nominal size = 10%, and 5%  
(j), (k), (l): Mean biases of forward Nagar, reverse Nagar, and LIML  
(m), (n): Actual sizes of the tests based on  $nR^2$  of the residual of forward Nagar with nominal sizes = 10%, and 5%

**The reported numbers are based on 5000 Monte Carlo replications.**

Table 3 (Cont.):  $\tilde{R}_f^2 = .001$

| n      | K  | Cov( $\varepsilon, v_2$ ) | (a)   | (b)   | (c)    | (d)    | (e)    | (f)   | (g)   | (h)   | (i)   | (j)    | (k)    | (l)     | (m)   | (n)   |
|--------|----|---------------------------|-------|-------|--------|--------|--------|-------|-------|-------|-------|--------|--------|---------|-------|-------|
| 1,000  | 5  | -0.9                      | 0.078 | 0.062 | -0.750 | -0.175 | -1.376 | 0.221 | 0.145 | 0.112 | 0.100 | -0.552 | 2.395  | -2.964  | 0.152 | 0.096 |
| 1,000  | 5  | -0.5                      | 0.071 | 0.054 | -0.418 | 0.895  | 0.738  | 0.075 | 0.038 | 0.102 | 0.078 | -5.998 | 0.097  | -0.151  | 0.053 | 0.027 |
| 1,000  | 5  | 0.5                       | 0.063 | 0.047 | 0.422  | -0.917 | 1.382  | 0.088 | 0.043 | 0.102 | 0.076 | 0.290  | -0.059 | 1.123   | 0.063 | 0.028 |
| 1,000  | 5  | 0.9                       | 0.081 | 0.061 | 0.745  | 0.347  | 0.635  | 0.218 | 0.139 | 0.113 | 0.102 | 2.105  | 1.884  | 0.133   | 0.153 | 0.094 |
| 1,000  | 10 | -0.9                      | 0.100 | 0.077 | -0.816 | -0.528 | -0.350 | 0.221 | 0.140 | 0.125 | 0.115 | 0.595  | -0.346 | -0.152  | 0.132 | 0.079 |
| 1,000  | 10 | -0.5                      | 0.091 | 0.070 | -0.458 | 0.935  | -1.196 | 0.080 | 0.038 | 0.112 | 0.087 | -0.724 | -0.016 | 7.981   | 0.050 | 0.020 |
| 1,000  | 10 | 0.5                       | 0.091 | 0.072 | 0.450  | -0.436 | 1.358  | 0.080 | 0.043 | 0.120 | 0.092 | 0.526  | 2.132  | -2.410  | 0.054 | 0.025 |
| 1,000  | 10 | 0.9                       | 0.098 | 0.078 | 0.817  | 0.530  | 0.363  | 0.214 | 0.130 | 0.128 | 0.116 | 1.532  | 1.284  | 4.417   | 0.132 | 0.078 |
| 1,000  | 30 | -0.9                      | 0.106 | 0.085 | -0.871 | -0.636 | -0.245 | 0.186 | 0.100 | 0.134 | 0.119 | -0.849 | -0.940 | -2.584  | 0.100 | 0.046 |
| 1,000  | 30 | -0.5                      | 0.119 | 0.088 | -0.482 | 0.222  | -0.448 | 0.091 | 0.042 | 0.105 | 0.084 | 0.845  | -0.126 | -15.053 | 0.045 | 0.019 |
| 1,000  | 30 | 0.5                       | 0.127 | 0.095 | 0.484  | -1.280 | 1.860  | 0.088 | 0.044 | 0.108 | 0.085 | -0.144 | 0.427  | -4.637  | 0.048 | 0.021 |
| 1,000  | 30 | 0.9                       | 0.114 | 0.090 | 0.870  | 0.633  | 0.248  | 0.186 | 0.106 | 0.133 | 0.119 | 0.312  | 0.206  | -0.016  | 0.102 | 0.052 |
| 10,000 | 5  | -0.9                      | 0.078 | 0.043 | -0.236 | -0.039 | -0.206 | 0.256 | 0.179 | 0.067 | 0.039 | 0.466  | 0.041  | 0.172   | 0.157 | 0.105 |
| 10,000 | 5  | -0.5                      | 0.075 | 0.054 | -0.128 | 0.330  | -0.486 | 0.108 | 0.056 | 0.067 | 0.048 | 0.053  | 0.321  | 0.079   | 0.086 | 0.046 |
| 10,000 | 5  | 0.5                       | 0.080 | 0.051 | 0.132  | -0.605 | 0.738  | 0.115 | 0.064 | 0.074 | 0.051 | 0.061  | -0.152 | -0.437  | 0.097 | 0.053 |
| 10,000 | 5  | 0.9                       | 0.072 | 0.046 | 0.232  | 0.028  | 0.227  | 0.241 | 0.171 | 0.062 | 0.042 | -0.840 | -0.164 | -0.204  | 0.148 | 0.098 |
| 10,000 | 10 | -0.9                      | 0.112 | 0.085 | -0.425 | -0.176 | -0.269 | 0.385 | 0.306 | 0.071 | 0.052 | -0.024 | 0.346  | 0.165   | 0.171 | 0.118 |
| 10,000 | 10 | -0.5                      | 0.083 | 0.049 | -0.234 | 0.497  | -0.754 | 0.129 | 0.071 | 0.071 | 0.048 | -0.005 | 0.300  | -0.074  | 0.092 | 0.048 |
| 10,000 | 10 | 0.5                       | 0.073 | 0.043 | 0.239  | -0.418 | 0.642  | 0.117 | 0.060 | 0.063 | 0.043 | -0.031 | 0.189  | -0.047  | 0.083 | 0.042 |
| 10,000 | 10 | 0.9                       | 0.107 | 0.074 | 0.425  | 0.174  | 0.272  | 0.391 | 0.312 | 0.073 | 0.053 | -1.078 | 0.239  | -0.202  | 0.176 | 0.126 |
| 10,000 | 30 | -0.9                      | 0.151 | 0.121 | -0.673 | -0.398 | -0.285 | 0.692 | 0.598 | 0.116 | 0.098 | 0.100  | -1.022 | 0.165   | 0.213 | 0.159 |
| 10,000 | 30 | -0.5                      | 0.115 | 0.080 | -0.373 | 0.700  | -1.094 | 0.131 | 0.070 | 0.071 | 0.049 | -0.198 | 0.233  | 0.220   | 0.068 | 0.032 |
| 10,000 | 30 | 0.5                       | 0.117 | 0.085 | 0.375  | -0.740 | 1.143  | 0.132 | 0.070 | 0.068 | 0.049 | 0.721  | 0.293  | -0.148  | 0.068 | 0.033 |
| 10,000 | 30 | 0.9                       | 0.155 | 0.126 | 0.671  | 0.396  | 0.287  | 0.685 | 0.588 | 0.121 | 0.093 | -0.080 | -0.008 | -0.571  | 0.209 | 0.157 |

- (a), (b): Actual sizes of the new test based on 2SLS with nominal sizes = 10%, and 5%  
(c), (d), (e): Mean biases of forward and reverse 2SLS, and mean of  $\hat{b}$   
(f), (g): Actual sizes of the tests based on  $nR^2$  of the residual of forward 2SLS with nominal sizes = 10%, and 5%  
(h), (i): Actual size of the new test based on Nagar with nominal size = 10%, and 5%  
(j), (k), (l): Mean biases of forward Nagar, reverse Nagar, and LIML  
(m), (n): Actual sizes of the tests based on  $nR^2$  of the residual of forward Nagar with nominal sizes = 10%, and 5%

**The reported numbers are based on 5000 Monte Carlo replications.**

Table 4:  $\tilde{R}_f^2 = .3$

| n   | K  | Cov( $\epsilon, v_2$ ) | (a)   | (b)   | (c)    | (d)    | (e)    | (f)   | (g)   | (h)   | (i)   | (j)    | (k)    | (l)    | (m)   | (n)   |
|-----|----|------------------------|-------|-------|--------|--------|--------|-------|-------|-------|-------|--------|--------|--------|-------|-------|
| 100 | 5  | -0.9                   | 0.123 | 0.087 | -0.063 | -0.012 | -0.041 | 0.145 | 0.086 | 0.100 | 0.064 | 0.002  | 0.014  | 0.023  | 0.122 | 0.065 |
| 100 | 5  | -0.5                   | 0.124 | 0.086 | -0.036 | 0.059  | -0.073 | 0.106 | 0.053 | 0.099 | 0.071 | 0.001  | 0.025  | 0.013  | 0.100 | 0.051 |
| 100 | 5  | 0.5                    | 0.123 | 0.091 | 0.036  | -0.061 | 0.074  | 0.109 | 0.055 | 0.101 | 0.072 | 0.000  | -0.027 | -0.014 | 0.102 | 0.051 |
| 100 | 5  | 0.9                    | 0.117 | 0.081 | 0.062  | 0.011  | 0.041  | 0.141 | 0.084 | 0.094 | 0.063 | -0.004 | -0.015 | -0.024 | 0.116 | 0.066 |
| 100 | 10 | -0.9                   | 0.090 | 0.045 | -0.147 | -0.046 | -0.093 | 0.197 | 0.124 | 0.078 | 0.045 | 0.011  | 0.020  | 0.029  | 0.120 | 0.066 |
| 100 | 10 | -0.5                   | 0.094 | 0.056 | -0.084 | 0.117  | -0.180 | 0.113 | 0.059 | 0.088 | 0.059 | 0.003  | 0.031  | 0.018  | 0.097 | 0.047 |
| 100 | 10 | 0.5                    | 0.098 | 0.055 | 0.081  | -0.118 | 0.178  | 0.118 | 0.056 | 0.090 | 0.056 | -0.007 | -0.033 | -0.018 | 0.099 | 0.046 |
| 100 | 10 | 0.9                    | 0.091 | 0.045 | 0.150  | 0.050  | 0.091  | 0.195 | 0.123 | 0.077 | 0.047 | -0.005 | -0.014 | -0.024 | 0.118 | 0.067 |
| 100 | 30 | -0.9                   | 0.087 | 0.047 | -0.368 | -0.169 | -0.193 | 0.400 | 0.261 | 0.071 | 0.030 | 0.077  | 0.016  | 0.027  | 0.114 | 0.063 |
| 100 | 30 | -0.5                   | 0.086 | 0.041 | -0.201 | 0.279  | -0.466 | 0.111 | 0.045 | 0.072 | 0.037 | 0.133  | 0.047  | 0.027  | 0.070 | 0.028 |
| 100 | 30 | 0.5                    | 0.088 | 0.042 | 0.204  | -0.285 | 0.474  | 0.115 | 0.048 | 0.076 | 0.039 | -0.032 | -0.048 | -0.031 | 0.074 | 0.028 |
| 100 | 30 | 0.9                    | 0.089 | 0.050 | 0.365  | 0.166  | 0.194  | 0.397 | 0.261 | 0.063 | 0.027 | -0.038 | -0.019 | -0.030 | 0.111 | 0.057 |
| 250 | 5  | -0.9                   | 0.131 | 0.097 | -0.024 | -0.003 | -0.016 | 0.121 | 0.067 | 0.105 | 0.074 | 0.001  | 0.007  | 0.011  | 0.111 | 0.058 |
| 250 | 5  | -0.5                   | 0.130 | 0.096 | -0.015 | 0.023  | -0.029 | 0.103 | 0.053 | 0.102 | 0.072 | -0.001 | 0.009  | 0.004  | 0.100 | 0.050 |
| 250 | 5  | 0.5                    | 0.138 | 0.098 | 0.013  | -0.025 | 0.029  | 0.107 | 0.054 | 0.106 | 0.074 | -0.001 | -0.011 | -0.006 | 0.103 | 0.052 |
| 250 | 5  | 0.9                    | 0.129 | 0.092 | 0.025  | 0.005  | 0.016  | 0.117 | 0.062 | 0.099 | 0.069 | 0.000  | -0.005 | -0.009 | 0.107 | 0.054 |
| 250 | 10 | -0.9                   | 0.100 | 0.059 | -0.065 | -0.021 | -0.039 | 0.145 | 0.083 | 0.086 | 0.055 | 0.000  | 0.005  | 0.008  | 0.106 | 0.057 |
| 250 | 10 | -0.5                   | 0.096 | 0.060 | -0.032 | 0.049  | -0.073 | 0.105 | 0.051 | 0.085 | 0.056 | 0.004  | 0.013  | 0.008  | 0.092 | 0.047 |
| 250 | 10 | 0.5                    | 0.097 | 0.063 | 0.036  | -0.047 | 0.074  | 0.102 | 0.053 | 0.085 | 0.057 | -0.001 | -0.010 | -0.005 | 0.094 | 0.046 |
| 250 | 10 | 0.9                    | 0.092 | 0.055 | 0.061  | 0.017  | 0.040  | 0.139 | 0.072 | 0.079 | 0.050 | -0.005 | -0.009 | -0.012 | 0.100 | 0.052 |
| 250 | 30 | -0.9                   | 0.088 | 0.042 | -0.188 | -0.075 | -0.111 | 0.279 | 0.176 | 0.083 | 0.041 | 0.006  | 0.009  | 0.012  | 0.100 | 0.051 |
| 250 | 30 | -0.5                   | 0.098 | 0.048 | -0.104 | 0.130  | -0.227 | 0.128 | 0.062 | 0.092 | 0.048 | 0.004  | 0.014  | 0.008  | 0.088 | 0.042 |
| 250 | 30 | 0.5                    | 0.093 | 0.047 | 0.104  | -0.129 | 0.227  | 0.120 | 0.060 | 0.087 | 0.047 | -0.004 | -0.013 | -0.008 | 0.086 | 0.039 |
| 250 | 30 | 0.9                    | 0.092 | 0.046 | 0.189  | 0.075  | 0.111  | 0.291 | 0.186 | 0.086 | 0.044 | -0.005 | -0.008 | -0.011 | 0.102 | 0.054 |

- (a), (b): Actual sizes of the new test based on 2SLS with nominal sizes = 10%, and 5%  
(c), (d), (e): Mean biases of forward and reverse 2SLS, and mean of  $\hat{b}$   
(f), (g): Actual sizes of the tests based on  $nR^2$  of the residual of forward 2SLS with nominal sizes = 10%, and 5%  
(h), (i): Actual size of the new test based on Nagar with nominal size = 10%, and 5%  
(j), (k), (l): Mean biases of forward Nagar, reverse Nagar, and LIML  
(m), (n): Actual sizes of the tests based on  $nR^2$  of the residual of forward Nagar with nominal sizes = 10%, and 5%

**The reported numbers are based on 5000 Monte Carlo replications.**

Table 4 (Cont.):  $\tilde{R}_f^2 = .3$

| n      | K  | Cov( $\varepsilon, v_2$ ) | (a)   | (b)   | (c)    | (d)    | (e)    | (f)   | (g)   | (h)   | (i)   | (j)    | (k)    | (l)    | (m)   | (n)   |
|--------|----|---------------------------|-------|-------|--------|--------|--------|-------|-------|-------|-------|--------|--------|--------|-------|-------|
| 1,000  | 5  | -0.9                      | 0.138 | 0.098 | -0.007 | -0.002 | -0.004 | 0.105 | 0.053 | 0.106 | 0.072 | -0.001 | 0.000  | 0.001  | 0.103 | 0.051 |
| 1,000  | 5  | -0.5                      | 0.135 | 0.100 | -0.005 | 0.005  | -0.007 | 0.103 | 0.053 | 0.107 | 0.078 | -0.001 | 0.001  | 0.000  | 0.102 | 0.052 |
| 1,000  | 5  | 0.5                       | 0.136 | 0.101 | 0.005  | -0.005 | 0.007  | 0.103 | 0.050 | 0.109 | 0.074 | 0.001  | -0.001 | 0.000  | 0.102 | 0.049 |
| 1,000  | 5  | 0.9                       | 0.132 | 0.097 | 0.007  | 0.002  | 0.004  | 0.105 | 0.056 | 0.105 | 0.076 | 0.001  | 0.000  | -0.001 | 0.102 | 0.054 |
| 1,000  | 10 | -0.9                      | 0.102 | 0.069 | -0.017 | -0.005 | -0.010 | 0.109 | 0.062 | 0.090 | 0.063 | 0.000  | 0.001  | 0.002  | 0.099 | 0.054 |
| 1,000  | 10 | -0.5                      | 0.114 | 0.076 | -0.010 | 0.011  | -0.019 | 0.110 | 0.057 | 0.100 | 0.067 | -0.001 | 0.002  | 0.001  | 0.108 | 0.056 |
| 1,000  | 10 | 0.5                       | 0.106 | 0.073 | 0.010  | -0.011 | 0.019  | 0.104 | 0.054 | 0.094 | 0.064 | 0.000  | -0.002 | -0.001 | 0.101 | 0.052 |
| 1,000  | 10 | 0.9                       | 0.111 | 0.074 | 0.017  | 0.006  | 0.010  | 0.118 | 0.062 | 0.096 | 0.064 | 0.001  | -0.001 | -0.001 | 0.108 | 0.057 |
| 1,000  | 30 | -0.9                      | 0.099 | 0.050 | -0.055 | -0.020 | -0.034 | 0.160 | 0.087 | 0.094 | 0.049 | 0.000  | 0.002  | 0.003  | 0.106 | 0.052 |
| 1,000  | 30 | -0.5                      | 0.100 | 0.057 | -0.030 | 0.035  | -0.063 | 0.113 | 0.058 | 0.093 | 0.055 | 0.000  | 0.003  | 0.002  | 0.096 | 0.052 |
| 1,000  | 30 | 0.5                       | 0.103 | 0.055 | 0.030  | -0.035 | 0.063  | 0.115 | 0.059 | 0.096 | 0.052 | -0.001 | -0.003 | -0.002 | 0.100 | 0.050 |
| 1,000  | 30 | 0.9                       | 0.105 | 0.053 | 0.055  | 0.020  | 0.034  | 0.157 | 0.090 | 0.098 | 0.050 | 0.000  | -0.002 | -0.002 | 0.107 | 0.053 |
| 10,000 | 5  | -0.9                      | 0.136 | 0.096 | 0.000  | 0.000  | 0.000  | 0.098 | 0.052 | 0.102 | 0.075 | 0.000  | 0.000  | 0.000  | 0.098 | 0.052 |
| 10,000 | 5  | -0.5                      | 0.125 | 0.094 | 0.000  | 0.001  | -0.001 | 0.094 | 0.047 | 0.099 | 0.067 | 0.000  | 0.001  | 0.000  | 0.094 | 0.047 |
| 10,000 | 5  | 0.5                       | 0.134 | 0.101 | 0.000  | -0.001 | 0.001  | 0.102 | 0.049 | 0.108 | 0.076 | 0.000  | 0.000  | 0.000  | 0.102 | 0.049 |
| 10,000 | 5  | 0.9                       | 0.125 | 0.093 | 0.000  | 0.000  | 0.000  | 0.094 | 0.044 | 0.098 | 0.067 | 0.000  | 0.000  | -0.001 | 0.094 | 0.044 |
| 10,000 | 10 | -0.9                      | 0.101 | 0.066 | -0.002 | -0.001 | -0.001 | 0.096 | 0.048 | 0.088 | 0.057 | 0.000  | 0.000  | 0.000  | 0.095 | 0.047 |
| 10,000 | 10 | -0.5                      | 0.115 | 0.076 | -0.001 | 0.001  | -0.002 | 0.108 | 0.052 | 0.101 | 0.065 | 0.000  | 0.000  | 0.000  | 0.107 | 0.052 |
| 10,000 | 10 | 0.5                       | 0.103 | 0.067 | 0.001  | -0.001 | 0.002  | 0.098 | 0.049 | 0.089 | 0.059 | 0.000  | 0.000  | 0.000  | 0.098 | 0.049 |
| 10,000 | 10 | 0.9                       | 0.111 | 0.074 | 0.002  | 0.000  | 0.001  | 0.107 | 0.052 | 0.097 | 0.063 | 0.000  | 0.000  | 0.000  | 0.106 | 0.051 |
| 10,000 | 30 | -0.9                      | 0.104 | 0.056 | -0.006 | -0.002 | -0.004 | 0.106 | 0.053 | 0.100 | 0.052 | 0.000  | 0.000  | 0.000  | 0.100 | 0.050 |
| 10,000 | 30 | -0.5                      | 0.096 | 0.057 | -0.003 | 0.003  | -0.007 | 0.096 | 0.052 | 0.092 | 0.054 | 0.000  | 0.000  | 0.000  | 0.094 | 0.051 |
| 10,000 | 30 | 0.5                       | 0.100 | 0.055 | 0.003  | -0.003 | 0.007  | 0.104 | 0.050 | 0.096 | 0.053 | 0.000  | 0.000  | 0.000  | 0.103 | 0.049 |
| 10,000 | 30 | 0.9                       | 0.100 | 0.055 | 0.006  | 0.002  | 0.004  | 0.102 | 0.052 | 0.095 | 0.051 | 0.000  | 0.000  | 0.000  | 0.095 | 0.049 |

- (a), (b): Actual sizes of the new test based on 2SLS with nominal sizes = 10%, and 5%  
(c), (d), (e): Mean biases of forward and reverse 2SLS, and mean of  $\hat{b}$   
(f), (g): Actual sizes of the tests based on  $nR^2$  of the residual of forward 2SLS with nominal sizes = 10%, and 5%  
(h), (i): Actual size of the new test based on Nagar with nominal size = 10%, and 5%  
(j), (k), (l): Mean biases of forward Nagar, reverse Nagar, and LIML  
(m), (n): Actual sizes of the tests based on  $nR^2$  of the residual of forward Nagar with nominal sizes = 10%, and 5%

**The reported numbers are based on 5000 Monte Carlo replications.**



Table 5: Extreme Cases

| $n$   | $K$ | $\omega_{12}$ | $\tilde{R}_f^2$ | $\beta$ | (a)   | (b)   | (c)    | (d)     | (e)     | (f)   | (g)   | (h)   | (i)   | (j)     | (k)     | (l)      | (m)   | (n)   |
|-------|-----|---------------|-----------------|---------|-------|-------|--------|---------|---------|-------|-------|-------|-------|---------|---------|----------|-------|-------|
| 1000  | 30  | -0.9          | 0.001           | 5       | 0.056 | 0.047 | -5.711 | -7.739  | 2.281   | 0.996 | 0.994 | 0.173 | 0.150 | -6.324  | -21.806 | -11.574  | 0.607 | 0.560 |
| 100   | 30  | -0.9          | 0.010           | 5       | 0.043 | 0.034 | -5.713 | -7.774  | 2.281   | 0.993 | 0.984 | 0.172 | 0.146 | -5.613  | -16.686 | -12.761  | 0.590 | 0.529 |
| 250   | 30  | -0.9          | 0.010           | 5       | 0.086 | 0.075 | -5.444 | -18.456 | 15.504  | 0.993 | 0.989 | 0.208 | 0.182 | -4.063  | -8.329  | 30.184   | 0.492 | 0.437 |
| 1000  | 30  | 0.9           | 0.001           | 5       | 0.053 | 0.046 | -3.968 | -3.233  | -0.792  | 0.989 | 0.982 | 0.168 | 0.147 | -3.515  | 0.469   | -1.909   | 0.577 | 0.528 |
| 250   | 30  | 0.9           | 0.010           | 5       | 0.090 | 0.076 | -3.782 | -2.538  | -1.335  | 0.987 | 0.980 | 0.196 | 0.168 | -7.067  | 0.373   | -206.265 | 0.482 | 0.425 |
| 100   | 30  | 0.9           | 0.010           | 5       | 0.046 | 0.040 | -3.967 | -3.236  | -0.775  | 0.973 | 0.939 | 0.161 | 0.143 | -10.529 | -1.393  | -4.978   | 0.533 | 0.470 |
| 250   | 30  | -0.5          | 0.010           | 5       | 0.093 | 0.081 | -5.077 | -16.519 | 16.499  | 0.969 | 0.953 | 0.185 | 0.156 | -33.998 | -14.437 | -181.137 | 0.477 | 0.417 |
| 1000  | 30  | -0.9          | 0.010           | 5       | 0.164 | 0.145 | -4.399 | 3.468   | -8.535  | 0.959 | 0.942 | 0.158 | 0.117 | 0.591   | 1.264   | 0.747    | 0.265 | 0.215 |
| 10000 | 30  | -0.9          | 0.001           | 5       | 0.164 | 0.139 | -4.401 | -10.374 | 4.202   | 0.958 | 0.941 | 0.141 | 0.103 | 3.253   | 1.293   | 4.417    | 0.251 | 0.204 |
| 1000  | 30  | 0.9           | 0.010           | 5       | 0.161 | 0.143 | -3.059 | -1.184  | -1.943  | 0.957 | 0.940 | 0.113 | 0.080 | -3.988  | 1.095   | 0.943    | 0.252 | 0.207 |
| 10000 | 30  | 0.9           | 0.001           | 5       | 0.161 | 0.140 | -3.064 | -1.197  | -1.945  | 0.956 | 0.939 | 0.118 | 0.081 | 0.377   | 0.229   | 0.698    | 0.254 | 0.206 |
| 250   | 30  | -0.9          | 0.001           | 5       | 0.046 | 0.040 | -5.852 | -6.439  | 0.635   | 0.947 | 0.905 | 0.068 | 0.059 | -14.582 | -6.682  | 3.729    | 0.560 | 0.488 |
| 10000 | 30  | -0.5          | 0.001           | 5       | 0.162 | 0.138 | -4.102 | 1.893   | -6.970  | 0.943 | 0.923 | 0.137 | 0.096 | -5.156  | 1.373   | 1.047    | 0.243 | 0.193 |
| 1000  | 30  | -0.5          | 0.010           | 5       | 0.160 | 0.134 | -4.100 | 7.585   | -10.363 | 0.942 | 0.921 | 0.143 | 0.097 | -1.881  | 0.572   | 0.996    | 0.259 | 0.209 |
| 250   | 30  | 0.5           | 0.010           | 5       | 0.095 | 0.082 | -4.154 | -1.537  | -2.652  | 0.940 | 0.905 | 0.171 | 0.130 | -1.067  | -8.462  | 4.416    | 0.449 | 0.383 |
| 10000 | 30  | 0.5           | 0.001           | 5       | 0.161 | 0.138 | -3.362 | -0.356  | -3.100  | 0.936 | 0.908 | 0.116 | 0.073 | -0.990  | 0.779   | 0.714    | 0.246 | 0.194 |
| 250   | 30  | 0.0           | 0.010           | 5       | 0.088 | 0.078 | -4.615 | 2.629   | -8.799  | 0.934 | 0.899 | 0.140 | 0.092 | -0.906  | 0.078   | 2.272    | 0.443 | 0.381 |
| 10000 | 30  | 0.0           | 0.001           | 5       | 0.164 | 0.140 | -3.732 | 0.965   | -4.838  | 0.932 | 0.902 | 0.122 | 0.078 | -1.398  | 4.593   | 0.963    | 0.240 | 0.190 |
| 1000  | 30  | 0.5           | 0.010           | 5       | 0.165 | 0.141 | -3.355 | -0.358  | -3.070  | 0.929 | 0.901 | 0.124 | 0.079 | -11.288 | 0.684   | 1.076    | 0.245 | 0.196 |
| 1000  | 30  | 0.0           | 0.010           | 5       | 0.159 | 0.136 | -3.728 | -0.064  | -4.001  | 0.928 | 0.896 | 0.135 | 0.088 | 3.761   | 0.945   | 0.943    | 0.249 | 0.197 |
| 1000  | 30  | -0.5          | 0.001           | 5       | 0.071 | 0.060 | -5.323 | -9.849  | 2.004   | 0.926 | 0.879 | 0.173 | 0.149 | -12.138 | -6.498  | 13.322   | 0.517 | 0.446 |
| 100   | 30  | -0.9          | 0.100           | 5       | 0.142 | 0.124 | -4.303 | 7.817   | -12.307 | 0.920 | 0.877 | 0.167 | 0.125 | 9.616   | 1.320   | 1.048    | 0.242 | 0.180 |
| 1000  | 30  | -0.9          | 0.010           | 1       | 0.163 | 0.140 | -1.417 | -3.825  | 2.785   | 0.918 | 0.889 | 0.264 | 0.238 | 0.369   | -0.015  | 0.201    | 0.247 | 0.204 |
| 10000 | 30  | -0.9          | 0.001           | 1       | 0.161 | 0.140 | -1.417 | -3.965  | 3.080   | 0.915 | 0.884 | 0.244 | 0.218 | 1.292   | 1.183   | 0.714    | 0.243 | 0.196 |
| 100   | 30  | 0.9           | 0.100           | 5       | 0.142 | 0.124 | -2.990 | -1.138  | -1.863  | 0.910 | 0.858 | 0.114 | 0.085 | -1.431  | 0.560   | 0.499    | 0.239 | 0.182 |
| 100   | 30  | -0.5          | 0.100           | 5       | 0.143 | 0.123 | -4.005 | 6.504   | -10.517 | 0.897 | 0.836 | 0.155 | 0.106 | -0.881  | 1.255   | 0.935    | 0.240 | 0.174 |
| 250   | 30  | -0.9          | 0.010           | 1       | 0.100 | 0.086 | -1.753 | -2.364  | 0.662   | 0.886 | 0.824 | 0.047 | 0.039 | -1.199  | -13.265 | -3.013   | 0.411 | 0.345 |
| 100   | 30  | 0.5           | 0.100           | 5       | 0.144 | 0.125 | -3.278 | -0.272  | -3.026  | 0.873 | 0.804 | 0.121 | 0.087 | 10.961  | 0.546   | 1.531    | 0.225 | 0.161 |
| 100   | 30  | 0.0           | 0.100           | 5       | 0.149 | 0.130 | -3.639 | 0.345   | -4.030  | 0.871 | 0.805 | 0.140 | 0.090 | -1.074  | 0.653   | 0.323    | 0.233 | 0.164 |
| 250   | 10  | -0.9          | 0.001           | 5       | 0.058 | 0.049 | -5.768 | -7.567  | 2.579   | 0.863 | 0.823 | 0.115 | 0.100 | -8.002  | 9.639   | 7.835    | 0.540 | 0.485 |

Note:  $\omega_{12}$  denotes the covariance between  $v_1$  and  $v_2$ . Columns (a) – (n) denote same objects as in previous tables.

Table 6: Comparison of 2SLS and LIML

| $(\sigma_{\varepsilon_2}, \beta, \sigma_\varepsilon^2)$ |                               | (Forward) 2SLS | LIML     |
|---------------------------------------------------------|-------------------------------|----------------|----------|
| (-0.1, 0.1, 1.01)                                       | Mean Bias                     | -0.09633       | -0.45529 |
|                                                         | Median Bias                   | -0.09545       | -0.0786  |
|                                                         | Standard Deviation            | 0.188187       | 40.32329 |
|                                                         | 75 percentile – 25 percentile | 0.254975       | 1.828275 |
|                                                         | 90 percentile – 10 percentile | 0.47662        | 5.41373  |
| (-0.01, 0.01, 1.0001)                                   | Mean Bias                     | -0.00922       | 0.065113 |
|                                                         | Median Bias                   | -0.00845       | -0.0063  |
|                                                         | Standard Deviation            | 0.188241       | 20.9529  |
|                                                         | 75 percentile – 25 percentile | 0.25485        | 1.8313   |
|                                                         | 90 percentile – 10 percentile | 0.47805        | 5.39492  |
| (0.01, -0.01, 1.0001)                                   | Mean Bias                     | 0.010141       | 1.618553 |
|                                                         | Median Bias                   | 0.0107         | 0.0088   |
|                                                         | Standard Deviation            | 0.188259       | 103.4206 |
|                                                         | 75 percentile – 25 percentile | 0.25465        | 1.831725 |
|                                                         | 90 percentile – 10 percentile | 0.47745        | 5.37822  |
| (0.1, -0.1, 1.01)                                       | Mean Bias                     | 0.097252       | -0.18974 |
|                                                         | Median Bias                   | 0.0977         | 0.08535  |
|                                                         | Standard Deviation            | 0.188368       | 37.93867 |
|                                                         | 75 percentile – 25 percentile | 0.2552         | 1.8266   |
|                                                         | 90 percentile – 10 percentile | 0.47512        | 5.43348  |

Note: The reported numbers are based on 5000 Monte Carlo repetitions. For every parameter combination, we set  $n = 1000$ ,  $K = 30$ , and  $\tilde{R}_f^2 = .001$ .