

# THE LIFE-CYCLE OF CONCENTRATED INDUSTRIES

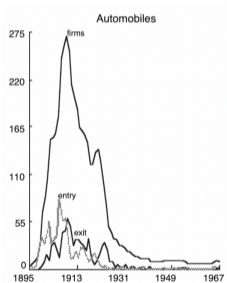
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Martin Beraja (MIT)

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# MOTIVATION

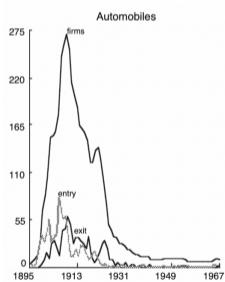
- ▶ Firms in cutting-edge industries often engage in *dynamic competition for the market*
- ▶ Many such industries have had a life-cycle: **Entry** → **Shakeout** → **Concentration**



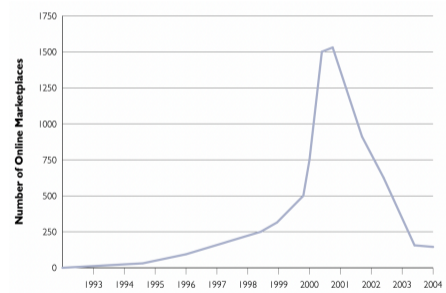
Source: Klepper and Simons (2005)

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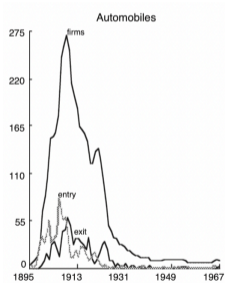
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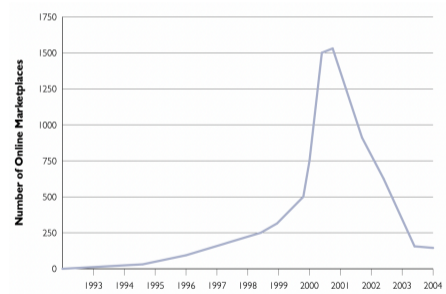
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- ▶ Also, OS or search engine industries. Windows or Google far ahead in a decade...

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## Questions

- ▶ Are **policies** geared towards industries where competition is primarily static also appropriate for **innovative** industries, where firms compete *for the market*?
- ▶ How should **policies to promote competition** over the life-cycle differ?

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- ▶ How should **policies to promote competition** over the life-cycle differ?
  - ▶ **Common belief in policy circles:** for digital / AI industries, gov'ts should intervene preemptively and early on in the life-cycle, before concentration becomes “irreversible”

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1. Equilibrium and (constrained) optimal policy over the life-cycle
2. **Application:** Digital and AI industries in the US (dataset from VentureScanner)



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**Assumption 1:** **Flow profit** function is:

- decreasing in  $\underline{N}$  and  $\bar{N}$ ,
- increasing in  $z$ ,
- converges to fixed cost  $-f$  as  $z \rightarrow 0$  and  $\bar{N} \rightarrow \infty$ , and
- such that at least one firm enters  $\pi(1, 0; \underline{z}) + \lambda \pi(0, 1; \bar{z}) / r > 0$ .

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### Special case:

- Cost function:  $\Gamma(q; z) = \frac{1}{z}q + f$
- Inverse demand function:

$$p_i = \frac{\sigma - 1}{\sigma} \left[ \sum_{j=1}^{\underline{N}_t + \bar{N}_t} (q_j)^{\frac{\epsilon - 1}{\epsilon}} \right]^{\frac{\epsilon}{\epsilon - 1} \frac{\sigma - 1}{\sigma} - 1} (q_i)^{-\frac{1}{\epsilon}}$$

- Cournot competition in  $q$



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## Households

$$V(\underline{N}_t, \bar{N}_t) = \mathbb{E}_t \left[ \int_t^\infty e^{-r(s-t)} U(\underline{N}_s, \bar{N}_s) ds \right]$$

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Special case:

$U = Q_t + X_t$ , with quantity  $Q_t$  and outside good  $X_t$ ,

$$\text{and } Q_t = \left[ \sum_{i=1}^{\underline{N}_t + \bar{N}_t} (q_{it})^{\frac{\epsilon-1}{\epsilon}} \right]^{\frac{\epsilon}{\epsilon-1}} \frac{\sigma-1}{\sigma}$$

Solve backward (recursively) for value functions and exit/entry policies

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► A long-run concentrated industry equilibrium  $(0, \bar{N}_\infty^{LF})$  is given by  $\bar{N}_\infty^{LF}$ :

1. **Large** firms don't exit in the long-run  $\iff J(0, \bar{N}_\infty^{LF}; \bar{z}) = \frac{\pi(0, \bar{N}_\infty^{LF}; \bar{z})}{r} \geq 0$ ,

2. **Small** firms don't enter in the long-run  $\iff J(1, \bar{N}_\infty^{LF}; \bar{z}) = \frac{\pi(1, \bar{N}_\infty^{LF}; \bar{z}) + \lambda \times J(0, \bar{N}_\infty^{LF} + 1; \bar{z})}{r + \lambda} < 0$ ,

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**Lemma 1.** The equilibrium number of large firms  $\bar{N}_\infty^{LF}$  in a concentrated industry state  $(0, \bar{N}_\infty^{LF})$  is uniquely determined by (1)-(3).

Intuition: profit functions decreasing in  $\bar{N}$ , and hence so is value function  $J(1, \bar{N}; \bar{z})$

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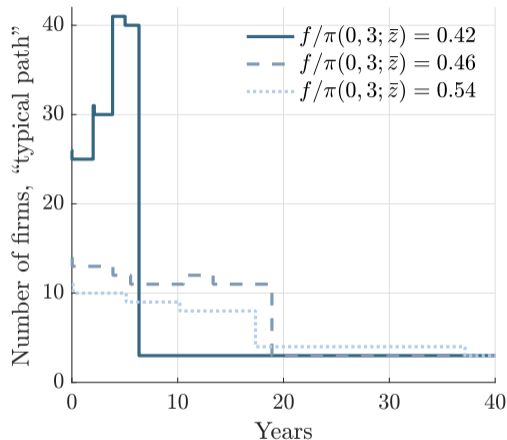
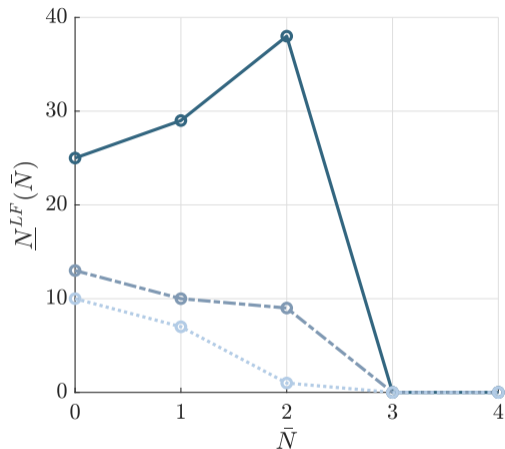
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**Lemma 2.** Equilibrium  $\underline{N}^{\text{LF}}(\bar{N})$  and  $\eta^{\text{LF}}(\bar{N})$  are uniquely pinned down by (1)-(2).

Intuition: profit functions decreasing in  $\underline{N}$ , and hence so is value function  $J(\underline{N}, \bar{N}; \underline{z})$

# ENTRY, SHAKEOUT, AND CONCENTRATION: A NUMERICAL ILLUSTRATION



► In a competitive industry, the life-cycle is monotonic. **Why the non-monotonicity?**

► Cost of delaying entry: more large firms present; e.g.,  $\pi(\underline{N}, 1; \underline{z}) - \pi(\underline{N}, 0; \underline{z}) < 0$

► Benefit: Large gains right before the shakeout; e.g.,  $\pi(0, 3; \bar{z}) - \pi(\underline{N}, 3; \bar{z}) > 0$

► Intuition

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- ▶ **Relative scale** → nature of competition (static v. dynamic) and **optimal policy**
- ▶ **Scale economies** key driver of US concentration/markups (Autor et al, Philippon et al)
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1.  $\bar{z}/\underline{z} \rightarrow \infty$  with  $\underline{z} \rightarrow 0$ . Innovation leads to large scale diffs. Competition for the market
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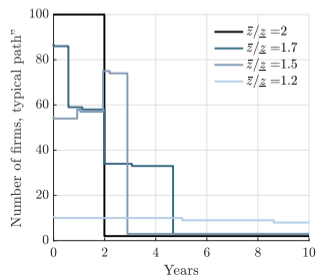
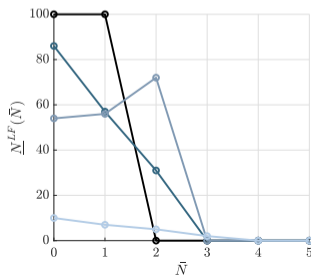


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  - ▶ That is, it cannot directly address quantity distortions due to imperfect competition
- ▶ Such interventions would implement a **first best** but are seldom used in practice
- ▶ Governments favor policies that **promote competition** via **firm entry** or **antitrust**
  - ▶ These are the type of policies currently being discussed for digital/AI industries (Khan, 2016; Philippon, 2019; Tirole, 2023; Varian, 2018)

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- ▶ **Goal**: analyze how **nature of competition** affects **optimal policy** over the life-cycle
  1. Are subsidies designed for promoting competition in static industries also appropriate for innovative industries where **dynamic competition for the market** is key?
  2. If not, how should subsidies over the life-cycle **differ**?



Theoretical results in two limit cases:

1.  $\bar{z}/\underline{z} \rightarrow \infty$ , with  $\underline{z} \rightarrow 0$ . Innovation leads to large scale diffs; competition for the market
  
2.  $\bar{z}/\underline{z} = 1$ . Small scale differences; static competition in the market

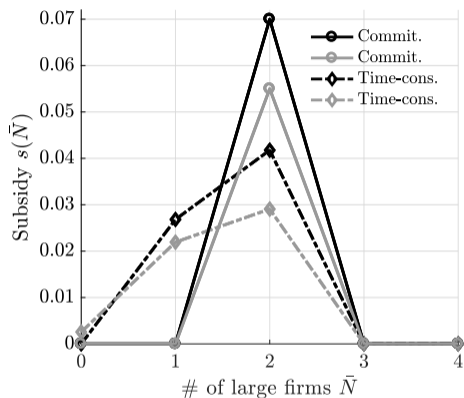
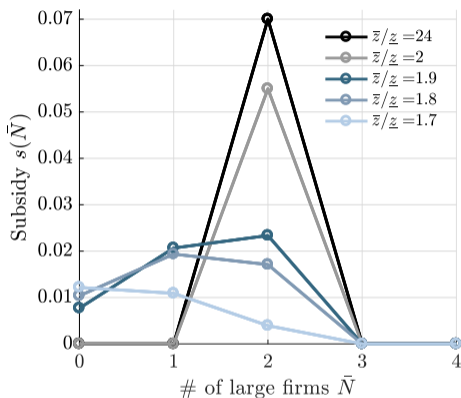
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  - ▶ The government must subsidize firms in a nascent industry too
  - ▶ Subsidies are uniform over the life-cycle

## RELATIVE SCALE AND OPTIMAL POLICY



- ▶ Firm entry/exit mostly driven by option value of taking over the market  
⇒ Governments can [wait to intervene](#) later in the life-cycle
- ▶ If the government cannot commit, the time-consistent policy must subsidize earlier

## HOW DO THESE RESULTS HELP INFORM COMPETITION POLICY DEBATES?

**Established belief in policy circles:** innovative industries are “harder” to regulate

- ▶ For digital / AI industries, many argue that gov'ts should intervene preemptively and early on, before concentration becomes irreversible

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  - ▶ Instead, gov't must **subsidize early on** when static competition in the market is important

1. Collusion and antitrust

$$\pi(\underline{N}, \bar{N}; \bar{z}) = \frac{1}{\bar{N}} \pi^{\text{Cartel}}(\underline{N}, \bar{N}; \bar{z})$$

2. Blocking competitors and antitrust

Large firms pay  $c$  to lower profits of small firms  $\pi(\underline{N}, \bar{N}; \bar{z})$

3. Endogenous Rate of Innovation  $\lambda$  at cost  $c(\lambda)$  ▶ numerical example

$$J(\underline{N}^{LF}(\bar{N} + 1), \bar{N} + 1; \bar{z}) - J(\underline{N}, \bar{N}; \bar{z}) = c'(\lambda(\underline{N}, \bar{N}))$$

4. Innovation spillovers from large firms  $\lambda(\bar{N})$

## APPLICATION: DIGITAL & AI INDUSTRIES IN THE US

The question of how to regulate an industry in practice can be understood as:

Are firm choices mostly driven by dynamic competition for the market?  
Or, is competition in the market important too?

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Analyze Digital and AI industries in the US using dataset from Venture Scanner

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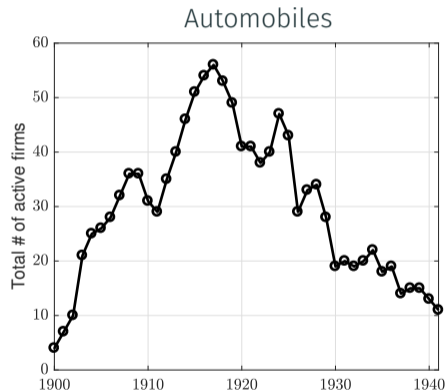
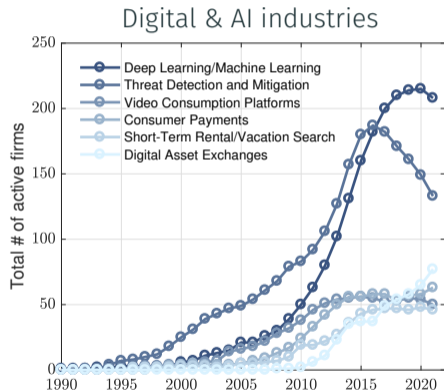
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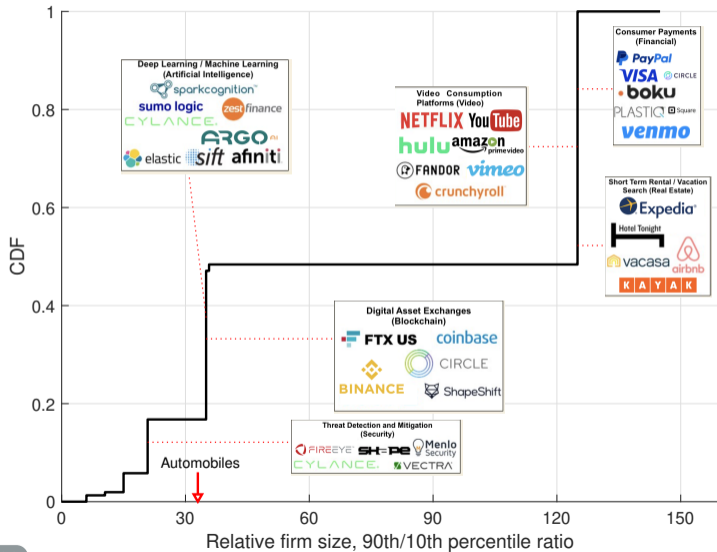
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As a comparison, look at Automobile industry using The 100 Year Almanac

# LIFE-CYCLE ACROSS INDUSTRIES



# RELATIVE SCALE ACROSS INDUSTRIES



▶ output-productivity model

## INTUITION FOR NON-MONOTONIC LIFE-CYCLE

- ▶ In a **competitive** industry (Jovanovic-MacDonald), the life-cycle is **always monotonic**  
No firms exit when quantities are low (price is high). A mass of firms exit once they are high (price is low)
- ▶ In an **oligopolistic** industry (our model), the life-cycle may be **non-monotonic**
- ▶ Incentives to **delay entry**, from  $\bar{N} = 1 \rightarrow 2$ , given  $\underline{N}$ :

$$J(\underline{N}, 2; \underline{z}) - J(\underline{N}, 1; \underline{z}) = \overbrace{\pi(\underline{N}, 2; \underline{z}) - \pi(\underline{N}, 1; \underline{z})}^{\text{cost of competing with an additional large firm } < 0} + \frac{\lambda}{r + \lambda \underline{N}} [\pi(\underline{N}, 3; \bar{z}) - \pi(\underline{N}, 2; \bar{z})] \\ + \underbrace{\frac{\lambda}{r + \lambda \underline{N}} [\pi(0, 3; \bar{z}) - \pi(\underline{N}, 3; \bar{z})]}_{\text{benefits of entering closer to the shakeout } > 0} .$$

- ▶ “Business stealing” gains at shakeout occur closer to the time of entry



# SOURCES OF INEFFICIENCY

Constrained Planner's value of an additional firm (SB) v. Equilibrium value of staying (LF)

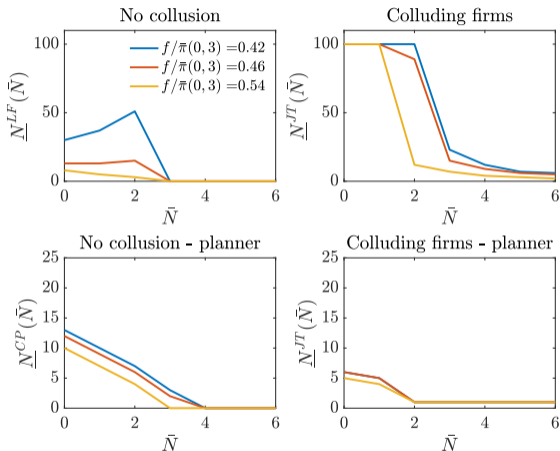
$$\text{SB: } U(\underline{N}, \bar{N}) - U(\underline{N} - 1, \bar{N}) + \lambda (V(\underline{N}(\bar{N} + 1), \bar{N} + 1) - V(\underline{N}, \bar{N}))$$

$$\text{LF: } \pi(\underline{N}, \bar{N}; \underline{z}) + \lambda J(\underline{N}(\bar{N} + 1), \bar{N} + 1; \bar{z}) + \eta(\bar{N})(\underline{N} - 1)J(\underline{N} - 1, \bar{N}; \underline{z})$$

1. **Source of inefficiency I:** Firms care about profits, not surplus  $\Rightarrow \uparrow$  # firms
2. **Source of inefficiency II:** Firms do not internalize surplus destruction  $\Rightarrow \downarrow$  # firms
3. **Source of inefficiency III:** War of attrition  $\Rightarrow \downarrow$  # firms

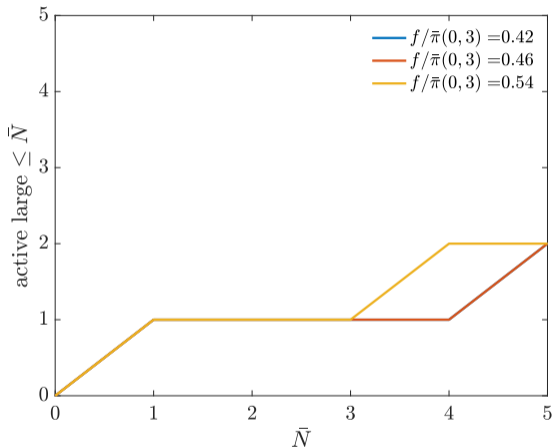
▶ [Jump back](#)

# COLLUSION AND ANTITRUST



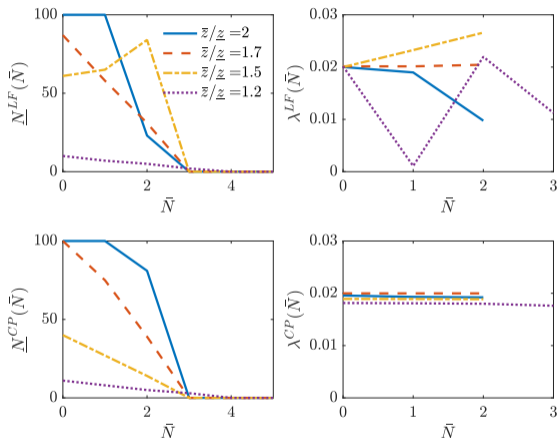
- ▶ More incentives to entry, to participate in the cartel
- ▶ Planner wants to break the cartel, or less entry if it can't

# COLLUSION AND ANTITRUST, INNACTIVE PRODUCTIVE FIRMS



► The cartel may not operate all firms/goods

# INTENSIVE MARGIN OF INNOVATION, $\lambda$ ENDOGENOUS



- ▶  $c(\lambda) = c_0 \lambda^{1.1}$ ,  $c_0$  calibrated so that  $\lambda(\underline{N}(0), 0) = 0.02$
- ▶ Life cycle of entry and exit virtually unaffected

# RELATIVE OUTPUT VS. RELATIVE PRODUCTIVITY, $\epsilon = 7.5$

