

# Problem Set 1

Due: Wednesday September 28<sup>th</sup>

These questions are from: Acemoglu, Daron (2008) “Introduction to Modern Economic Growth”

1. 13.13
2. 14.15
3. Optimal State Dependent IPR in a Partial Equilibrium Framework:

Let assume there are only two firms ( $i \in \{1, 2\}$ ) in one industry, maximizing their expected present discounted value of net profits. Moreover we assume:

- maximum number of gaps between two firms is two ( $n \in \{-2, -1, 0, 1, 2\}$ )
- the profit of each firm (without taking into account expenditure on R&D) is only a function of the number of the gaps in the quality of the firm and its rival.  $\pi^i = \pi_n \in \{\pi_{-2}, \pi_{-1}, \pi_0, \pi_1, \pi_2\}$
- R&D results to step by step innovation and the cost of R&D is linear in the arrival rate of innovation.  $\Phi(x^i) = \phi x^i$
- interest rate is constant.  $r = r_0$

In this framework, intellectual property right policy is modeled as the rate at which a technology becomes available for the rival firm for free and it is only a function of number of gaps between the leader and follower.

$$\eta = \begin{cases} \eta_1 & n = 1 \\ \eta_2 & n = 2 \\ \rightarrow \infty & n > 2 \end{cases}$$

Throughout this question we are focusing on the Markov Perfect Equilibrium in which strategies of firms are only function of the number of gaps between the firm and its rival.  $x^i = x_n \in \{x_{-2}, x_{-1}, x_0, x_1, x_2\}$

- (a) Write down the value function for a firm that is  $n$  step ahead (behind) its rival.
- (b) Solve the system of the equations for the optimal R&D decisions:  $x_n$

- (c) Let assume we are restricted to the policy  $\eta_1 = \eta_2 = \eta$ . Can  $\eta > 0$  increase R&D ? interpret the result.
- (d) If we relax the above restriction, can we have IPR policy which results to more R&D than the case  $\eta_1 = \eta_2 = 0$ ? interpret the result and give an intuition why  $\eta_1 > 0$  can increase R&D.