

# Confidence and the Propagation of Demand Shocks

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- Household deleveraging or other AD shocks
  - ⇒ Consumers spend less
  - ⇒ Firms produce and hire less
  - ⇒ Consumers lose confidence and spend even less
  - ⇒ Firms produce and hire even less
  - ⇒ ...
  - ⇒ The Great Recession!

# Does It Make Sense?

Basic RBC: **no**

- In GE, interest rates adjust, offsetting AD shock
- $N$ ,  $Y$ , and  $I$  move in opposite direction than  $C$

Basic NK: **perhaps**

- Only when MP does not replicate flexible price outcomes
- Translates any AD shock to a monetary expansion/contraction
- Inflation and output must co-move
- Also, hard to get  $C$  and  $I$  to comove

# This Paper: Demand-driven fluctuations with flexible prices

Element 1: **variable utilization** + adjustment cost for  $K$

⇒ intertemporal substitution in production

⇒ **AS responds to AD** along flexible-price outcomes

Element 2: **confusion** between idiosyncratic & agg. income fluctuations

⇒ **confidence multiplier**

(feedback loop b/w  $y$ , consumer sentiment, & investor sentiment)

1+2 ⇒:

*$u, y, h, c, i$  comove without TFP &  $\pi$*

1. Start with FIRE (full-info, rational expectations) and no investment margin variable utilization  $\Rightarrow$  **AS responds to AD**
2. Add info friction (or bounded rationality)  $\Rightarrow$  **confidence multiplier**
3. Comovement and other implications
  - Gov spending (crowding in, front-loading vs back-loading)
  - Comovement between savers and borrowers
  - Comovement between consumption and investment
  - TFP/AS shocks vs AD shocks

## Preferences and AD Curve

- Preferences (representative agent & complete info)

$$\mathcal{U}(c_t, n_t) + \beta_t \mathcal{U}(c_{t+1}, n_{t+1}) + \beta_t \beta_{t+1} \mathcal{U}(c_{t+2}, n_{t+2}) + \dots,$$

$$\mathcal{U}(c, n) = \frac{c^{1-\frac{1}{\sigma}}}{1-\frac{1}{\sigma}} - \frac{n^{1+\frac{1}{\nu}}}{1+\frac{1}{\nu}}$$

$$\log \beta_t = (1 - \rho_\beta) \log \beta + \rho_\beta \log \beta_{t-1} - \underbrace{\log \eta_t}_{\text{AD shock}}$$

- Positive  $\eta_t$  shock = urge to consume = real AD shock
- AD curve (log-linearized, complete info):

$$y_t = -\sigma (R_t + \beta_t) + \mathbb{E}_t [y_{t+1}]$$

# Technology and AS Curve

- Technology

$$y_t = (l_t)^\alpha (u_t k_t)^{1-\alpha}$$

$$k_{t+1} = (1 - \delta(u_t) + \Psi(l_t)) k_t,$$

- Tentatively: shut down  $l_t$  margin (infinite adjustment cost:  $\Psi(0) = 0$  and  $\Psi'(0) \rightarrow \infty$ )

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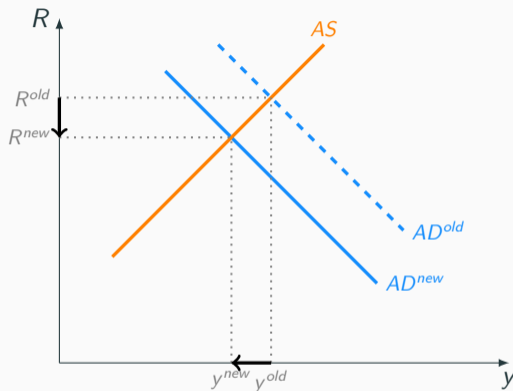
- Tentatively: shut down  $l_t$  margin (infinite adjustment cost:  $\Psi(0) = 0$  and  $\Psi'(0) \rightarrow \infty$ )
- AS curve (log-linearized):

$$y_t = (1 - \tilde{\alpha})(u_t + k_t),$$
$$u_t = \frac{\beta}{\tilde{\alpha} + \beta\phi} R_t + \beta \mathbb{E}_t [u_{t+1}],$$
$$k_{t+1} = k_t - \kappa u_t,$$

where  $\tilde{\alpha} \equiv 1 - \frac{(1-\alpha)(1+\frac{1}{\nu})}{1+\frac{1}{\nu}-\alpha+\frac{\alpha}{\sigma}}$  and  $\phi \equiv \frac{\delta''(u^*)u^*}{\delta'(u^*)}$ .



# Equilibrium without Info Frictions



- Resembles NK, but:  $R$  vs  $P$  in vertical axis, and  $y^{natural}$  vs  $y^{gap}$  on horizontal axis
- Flexible-price core of NK: vertical  $AS$ ,  $y^{natural}$  invariant to  $AD$
- Here: Intertemporal “Econ 101”

## Prop. Demand-driven fluctuations without nominal rigidity

$$\frac{\partial y_t}{\partial \eta_t} = \gamma \equiv \frac{\varsigma \sigma \beta}{\sigma + \varsigma} \frac{1}{1 - \rho \beta} > 0$$

where  $\sigma$  and  $\varsigma \equiv \frac{1 - \tilde{\alpha}}{\tilde{\alpha} + \beta \phi}$  parameterize the elasticities of AD and AS, respectively.

- $\varsigma$  and hence  $\gamma$  increase with flexibility of  $u$  (decrease with  $\phi \equiv \frac{\delta''(u^*)u^*}{\delta'(u^*)}$ )

# Full Model with Information Frictions

## Supply side

- Complete info, same as above

## Demand side

- Islands & idiosyncratic shocks
- Knowledge of own discount rate, own income & own interest rates
- **Incomplete info** about, or inattention to, aggregate conditions
- **(Rational) confusion** of idiosyncratic & agg. income fluctuations

## Prop. The AD Curve

$$y_t = -\sigma \{R_t + \beta_t\} + \mathbb{E}_t [y_{t+1}] + (\mathcal{B}_t + \mathcal{G}_t).$$

- $\mathcal{B}_t$  captures avg misperception of permanent income

$$\mathcal{B}_t \equiv \frac{1-\beta}{\beta} \sum_{k=0}^{+\infty} \beta^k \int (E_t^h [y_{h,t+k}] - \mathbb{E}_t [y_{h,t+k}]) dh,$$

where  $y_{h,t} = y_t + \xi_{h,t}$  is local/idiosyncratic income at  $t$ .

- $\mathcal{G}_t$  captures avg misperception of future interest rates

$$\mathcal{G}_t \equiv -\sigma \sum_{k=1}^{+\infty} \beta^k \int (E_t^h [R_{t+k}] - \mathbb{E}_t [R_{t+k}]) dh$$

# Our Hulten's Theorem

To understand  $\mathcal{B}_t$ , let's study first the true aggregate permanent income

## Prop. Our Hulten's Theorem

Aggregate permanent income is **invariant to the AD shock**  $\eta_t$ . Instead, it is instead pinned down by technology/capital alone:

$$\sum_{k=0}^{+\infty} \beta^k \int \mathbb{E}_t [y_{t+k}] = \frac{1-\tilde{\alpha}}{1-\beta} k_t$$

- Standard Hulten's theorem: static. Here: dynamic
- Key assumption: efficient production (both within and across periods)
- Note: current agg output/income *does* move
  - intertemporal substitution without altering present discounted value

## $\mathcal{B}_t$ : Misperception of Permanent Income

Our Hulten's theorem implies that  $\mathcal{B}_t$  is procyclical

Mechanism: current aggregate income  $y_t$  drops

⇒ local income  $y_{h,t} = y_t + \xi_{h,t}$  drops

⇒ rationally confused as drop in idiosyncratic income  $\xi_{h,t}$

⇒ drop in perceived permanent income

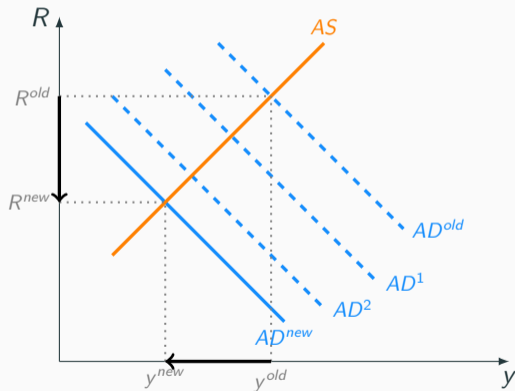
### Prop. Pro-cyclical misperception of permanent income

$$\frac{\partial \mathcal{B}_t}{\partial \eta_t} = \frac{1-\beta}{\beta(1-\beta\rho_\xi)} (1-\lambda) \frac{\partial y_t}{\partial \eta_t} > 0$$

where  $1 - \lambda$  measures degree of confusion of idiosyncratic & agg income fluctuations

# Confidence Multiplier

$AD$  drops  $\Rightarrow y$  drops  $\Rightarrow$  perceived permanent income drops even though actual doesn't  
 $\Rightarrow AD$  drops further  $\Rightarrow y$  drops further  $\Rightarrow \dots$



# Confidence Multiplier

Focus on the impact of  $\mathcal{B}_t$  (as if  $\mathcal{G}_t = 0$ )

## Prop. Equilibrium Impact of Confidence Multiplier

$$\frac{\partial y_t}{\partial \eta_t} = \gamma \cdot m^{\text{conf}}(\lambda, \rho_\xi),$$

where the “confidence multiplier” is given by

$$m^{\text{conf}}(\lambda, \rho_\xi) \equiv \frac{\varsigma + \sigma}{\varsigma + \sigma - \varsigma \frac{1-\beta}{1-\beta\rho_\xi} (1-\lambda)} > 1;$$

increases with the degree of confusion,  $1 - \lambda$ ; increases with the persistence of idiosyncratic income,  $\rho_\xi$ ; is invariant to the persistence of AD shock  $\rho_\beta$ ; and increases with the MPC.



## $\mathcal{G}_t$ : Discounting GE Adjustment in Interest Rate

Consider now the role of  $\mathcal{G}_t$

### Prop. Discounting GE

$$\frac{\partial \mathcal{G}_t}{\partial \eta_t} = (1 - \lambda) \frac{\sigma^2}{\sigma + \varsigma} \frac{\beta \rho_\beta}{1 - \beta \rho_\beta} > 0$$

- Neoclassical GE: interest rates  $R_{t+k}$  drop
  - discourages consumption
  - goes against the direct impact of the AD shock
- Here: cannot fully perceive  $R_{t+k}$  drop
  - arrests the Neoclassical GE effect
  - i.e., amplifies the impact of the AD shock
- Bottom line: this mechanism reinforces confidence multiplier

## Prop. Two Multipliers

The equilibrium response of aggregate output is given by

$$\frac{\partial y_t}{\partial \eta_t} = \gamma \cdot m^{\text{conf}}(\lambda, \rho_\xi) \cdot m^{\text{GE}}(\lambda, \rho_\beta),$$

where

$$m^{\text{GE}}(\lambda, \rho_\beta) \equiv 1 + \beta \rho_\beta \frac{\sigma}{\sigma + \varsigma} (1 - \lambda) \geq 1$$

increases with degree of confusion,  $1 - \lambda$ , and with persistence of AD shock,  $\rho_\beta$ .

Element 1: variable utilization  $\Rightarrow$  **AS responds to AD**

Element 2: info friction  $\Rightarrow$  **amplification**

In the paper: signal extraction, endogeneity/uniqueness of  $\lambda$

Next:

- Bounded rationality interpretations
- Comovement (savers & borrowers; investment & consumption)
- Other shocks (fiscal, TFP)

# Bounded Rationality

So far: agents are imperfectly informed but super rational

Broader interpretation of confidence multiplier  $B_t$

- Key: the response of  $c_{h,t}$  to  $y_{h,t}$  independent from idio. vs agg.
- Rule of thumb (Kahneman, 2011)
- Extrapolation (Barberis, Greenwood, Jin, Shleifer, 2014)
- One-factor representation (Molavi, 2019)

Broader interpretation of GE discounting  $G_t$

- Lack of common knowledge (Angeletos & Lian, 18)
- Level-k thinking (Farhi & Werning, 19; Garcia-Schmidt & Woodford, 19)
- Cognitive discounting (Gabaix, 20)
- There: GE discounting of future output gaps = attenuation of current gaps
- Here: GE discounting of future natural  $R$  = amplification of current natural  $y$

# Government Spending

- Same AS as above
- Only shut down wealth effect of  $G$  on labor supply (for simplicity)
- No confusion about tax burden (Ricardian equiv still holds)
- AD with  $G$  shocks:

$$y_t = -\sigma R_t + G_t - E_t[G_{t+1}] + E_t[y_{t+1}] + (\mathcal{B}_t + \mathcal{G}_t)$$

**Front-loading**  $G_t \implies$  positive AD shock  $\implies$  confidence multiplier

## Prop. Front-loading government spending

With strong enough info friction,  $G_t$  can crowd in  $c_t$

**Back-loading**  $G_t \implies$  negative AD shock  $\implies$  negative multiplier

Credit crunch:

$$c_t^b = -\sigma R_t + \mathbb{E}_t [c_{t+1}^b] + \mathcal{B}_t + \mathcal{G}_t - \sigma \beta_t$$

$$c_t^s = -\sigma R_t + \mathbb{E}_t [c_{t+1}^s] + \mathcal{B}_t + \mathcal{G}_t$$

With FIRE, as  $R_t$  adjusts,  $c_t^s$  moves in the opposite direction than  $c_t^b$

## Prop. Borrowers and Savers

With enough noise/bounded rationality,  $(c_t^s, c_t^b, y_t)$  **positively co-move**.

# Investment

Allow for investment, with positive but non-infinite adjustment cost

$$k_{t+1} = [1 - \delta(u_t) + \Psi(\iota_t)] k_t.$$

Complete info (with small wealth effect on labor supply)

- Positive comovement between  $c$  and  $y$ 
  - non-vertical AS thanks to the forward-looking  $u$
- Negative comovement between  $i$  and  $c$ 
  - negative AD shock,  $c \downarrow$ ,  $R \downarrow$ ,  $i \uparrow$

Our resolution:

- **Investment** subject to **confidence multiplier** too
- Feedback between  $y_t$  & investor expectations of returns

## Prop. Investment-consumption comovement

There exist  $\bar{\lambda}, \bar{\phi}, \underline{\nu}, \underline{\psi} > 0$ . If  $\lambda < \bar{\lambda}$ ,  $\phi < \bar{\phi}$ ,  $\nu > \underline{\nu}$  and  $\psi > \underline{\psi}$ ,

$(c_t, i_t, y_t, n_t, u_t)$  **positively co-move**.

- Large confidence multiplier (small  $\lambda$ )
- Elastic utilization (small  $\phi$  and large  $\psi$ )
- Elastic labor supply (large  $\nu$ )



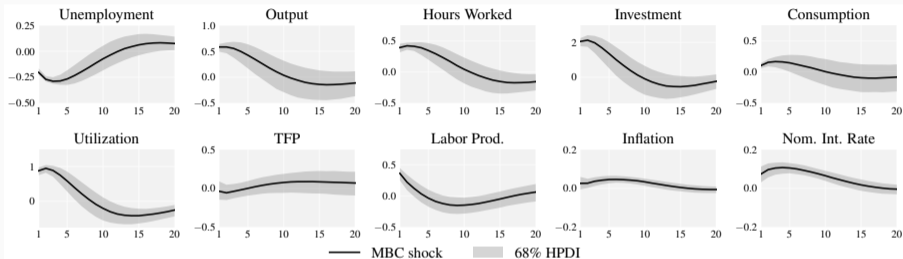
- Replace  $\beta$  shock with **aggregate TFP shock**
- Confidence multiplier: basically absent
  - Actual permanent income moves with aggregate TFP
  - Confusion of idio and agg shocks  $\Rightarrow$  ambiguous  $B_t$
  - Useful benchmark  $B_t \approx 0$  ( $\rho_\xi \approx \rho_A$ )
- GE discounting: reversed
  - With FIRE: positive TFP Shock  $\Rightarrow$  reduces  $R \Rightarrow$  encourages AD
  - Without:  $R$  adjustment is discounted  $\Rightarrow$  AD moves less  $\Rightarrow$   $y$  also moves less

## Prop. AS vs AD Shock

Friction **dampens AS shocks** at the same time it **amplifies AD shocks**

# Circling Back to Motivating Facts

- Main Business Cycle Shock (Angeletos, Collard & Dellas, 2020)



- Not only:  $u$ ,  $y$ ,  $h$ ,  $c$ ,  $i$  comove without TFP &  $\pi$
- But also: **evidence of intertemporal substitution in utilization/production**
- Plus: Utilization accounts for pro-cyclicality in labor prod
- And: non-accommodative MP and procyclical real  $R$

- Evidence calls for theories that make room for Keynesian narrative, and let AD drive business cycles, without strict reliance on sticky prices and Phillips curves
- This echoes the older literature on coordination failures and multiple equilibria
- Newer literature shifts focus on belief, financial, and other frictions on the demand side
- More to be done on both the empirical and theoretical front!